



# Rapid Aerial Photographic Target Recognition

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**Customer:** Lockheed Martin - Ben Mihevc, Tim Moon, Eileen Liu, Theresa Brown

**Advisor:** Dr. Dennis Akos

# Project Purpose and Objectives

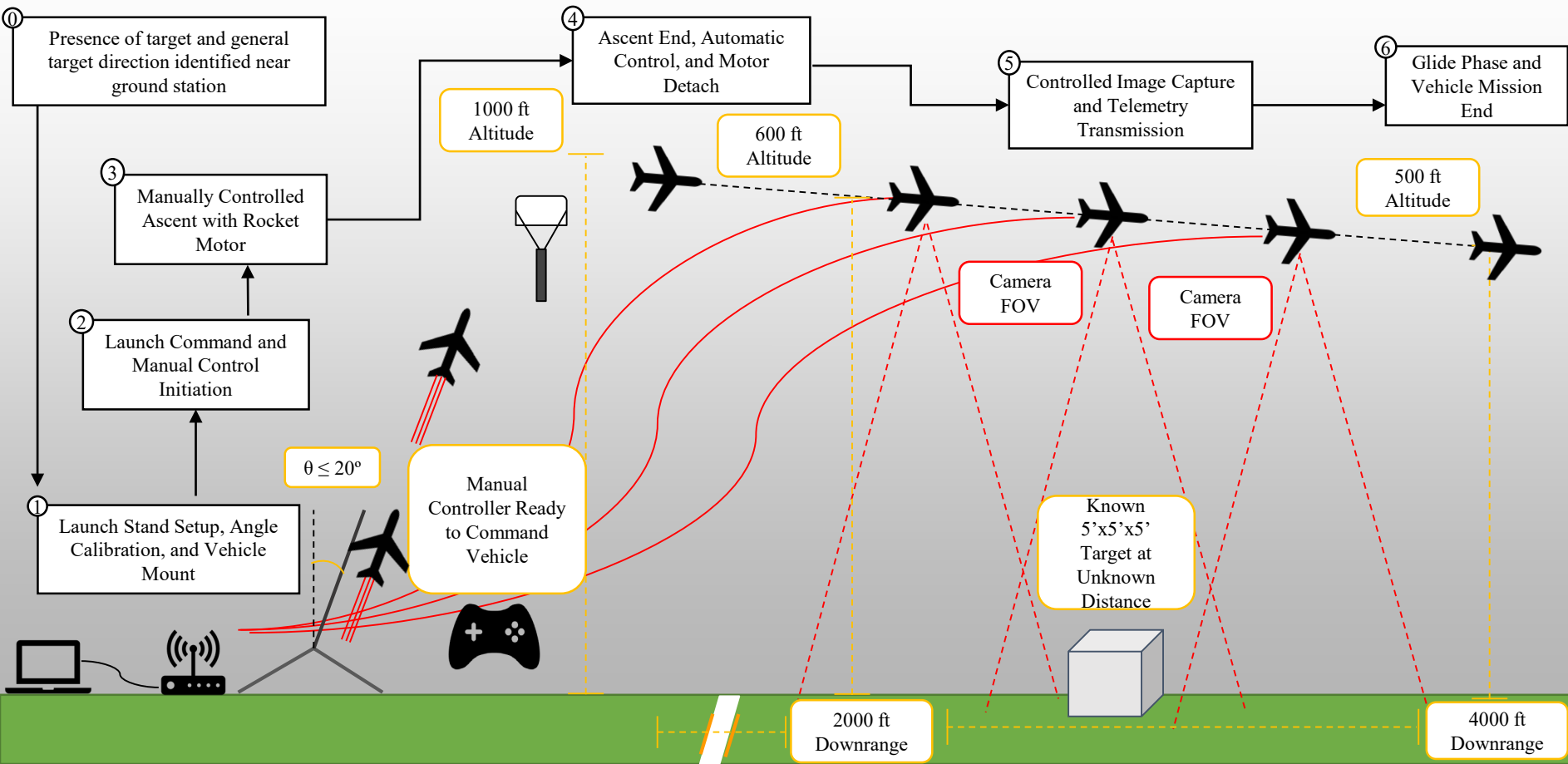
# Project Motivation

The purpose of this project is to design, manufacture, and test a portable, user-deployable system that can image and identify ground targets of interest and provide real time threat location and classification of said targets to a ground station within three minutes of initial system deployment.



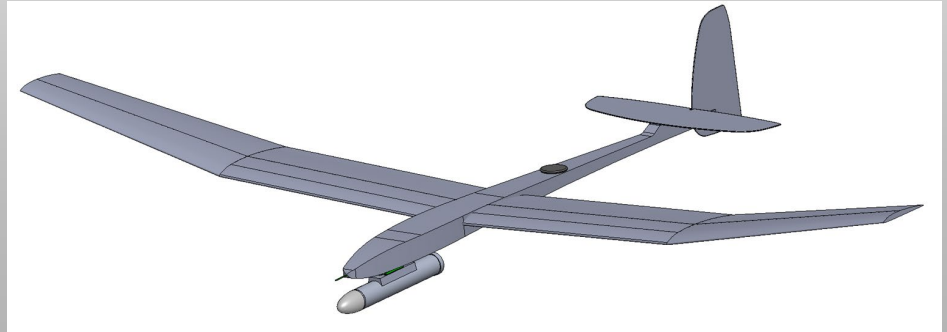
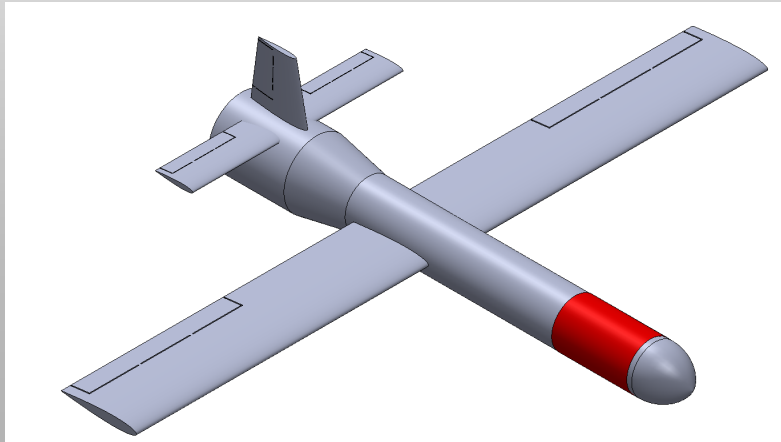
# RAPTR CONOPs

Objective: Image and locate target within area of interest



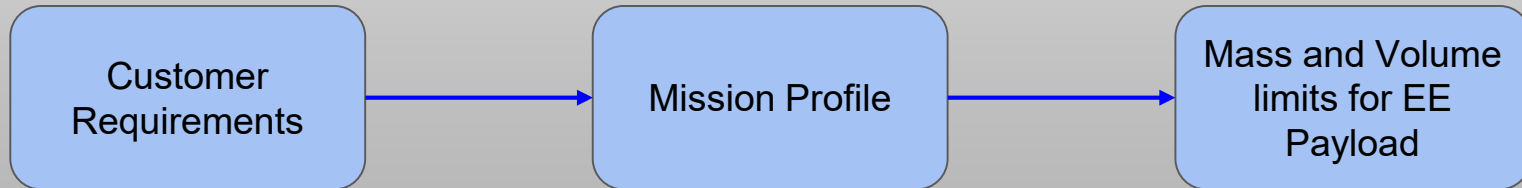
# Major Changes From PDR

- Modify a COTS Hyperflight AndREaS glider instead of building vehicle
- Rocket motor changed from 5 F-class to single I-class
- Approval to fly conforming to NAR regulations
- Detachable motor with parachute
- Manually controlled ascent



# ASEN/ECEN Responsibility Division

ASEN	ECEN
Vehicle (6"x2.5"x1.5" payload volume)	Image Capturing Payload (1.5 lb max)
Transmission and Reception of Commands and Flight Data	Transmission and Reception of Image Data
Target Recognition/Geo-location Software	Target Classification Software



# Functional Requirements

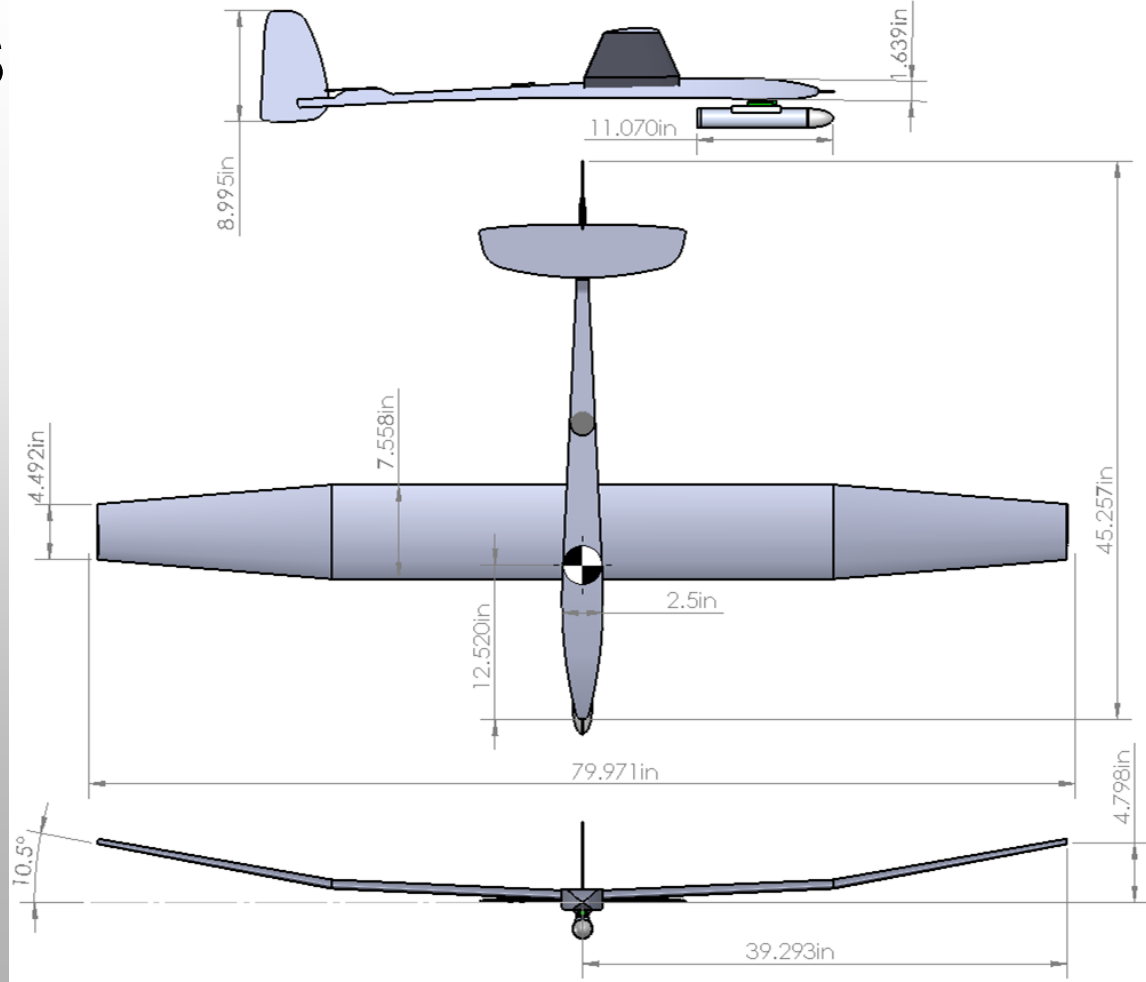
FR 1	The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.
FR 2	The system shall be man portable.
FR 3	The system shall transmit images to a ground station.
FR 4	The system shall identify a distinctly colored target and relay the target's latitude and longitude.
FR 5	The system shall complete its mission (launch to images processed) within 3 minutes.
FR 6	The system shall comply with all federal and state laws regarding testing and functionality.

# Design Solution

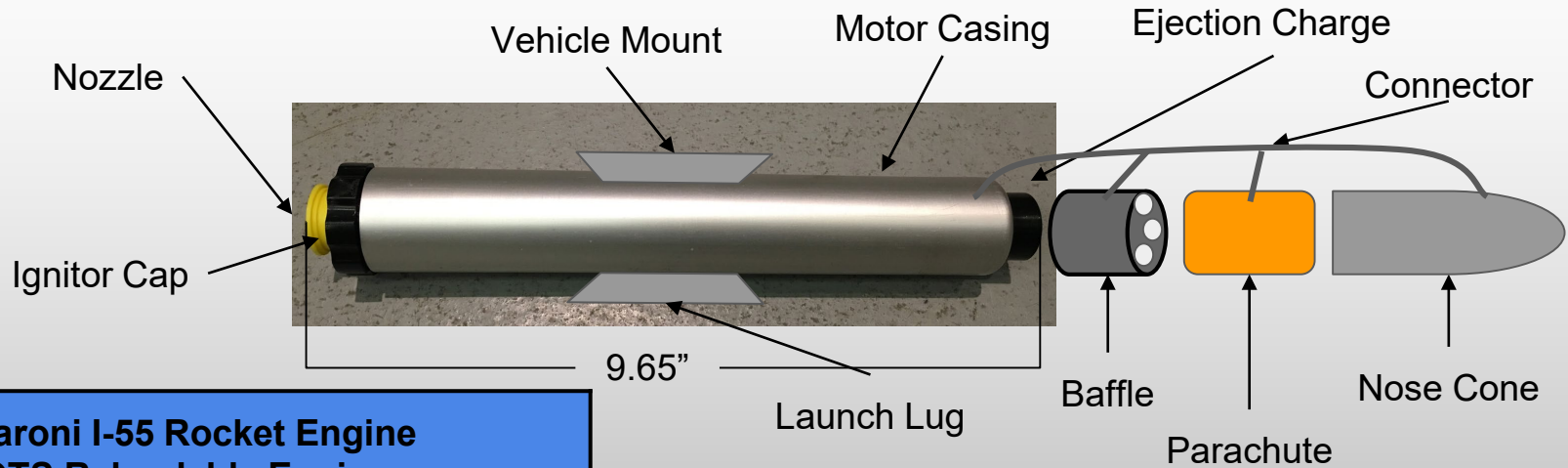


# Hyperflight AndREaS

Item(s)	Mass [lb]
Airframe	1.14
Motor and Mount	1.50
Electronics	0.48
Payload	1.10
<b>Total</b>	<b>4.22</b>



# Propulsion Overview

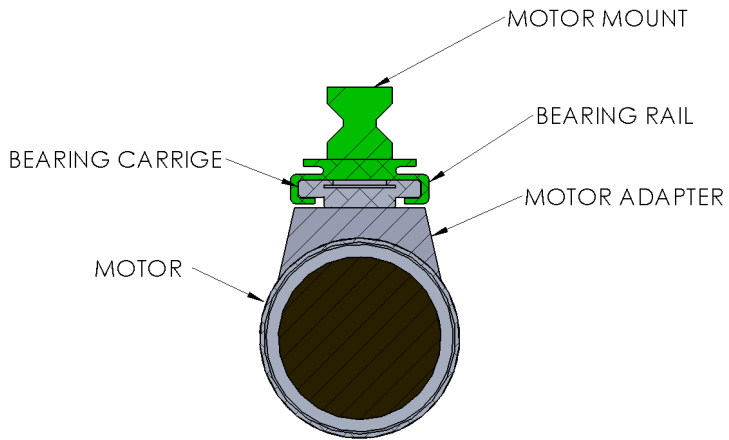
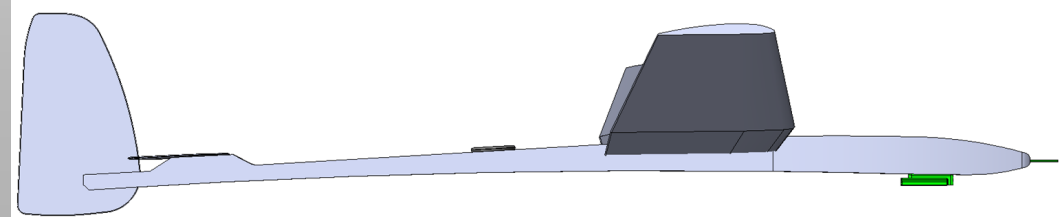
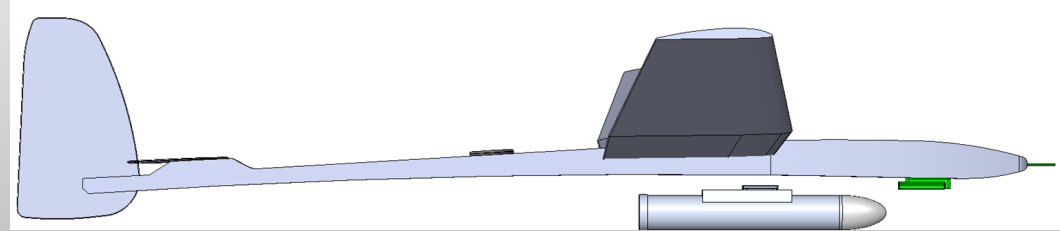
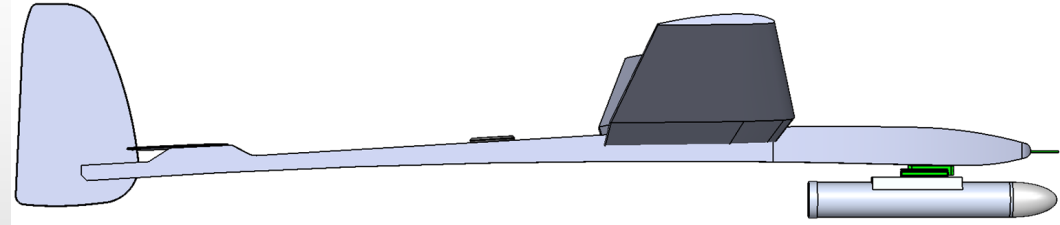


## Cesaroni I-55 Rocket Engine COTS Reloadable Engine

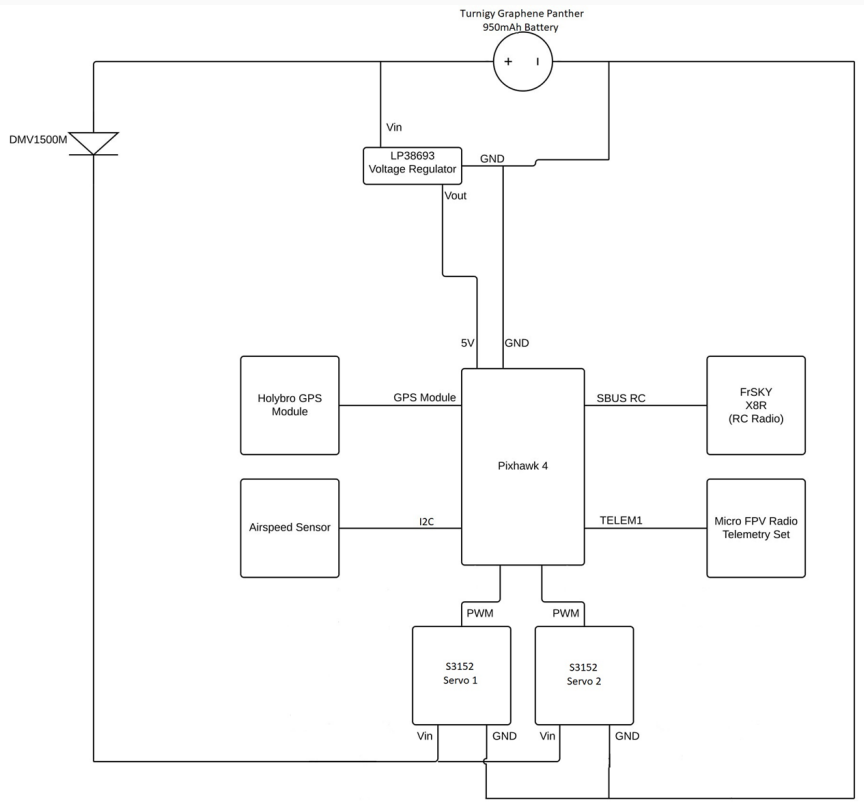
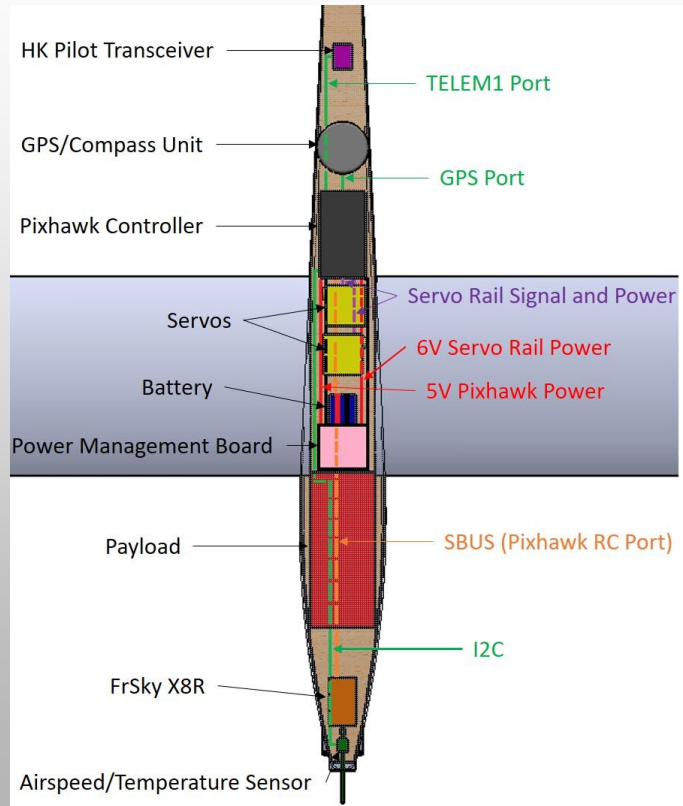
Maximum Thrust	21.25 lbf
Average Thrust	12.41 lbf
Burn Time	7.25 sec
Black Powder Ejection Charge	9 sec

# Motor Mounting and Separation

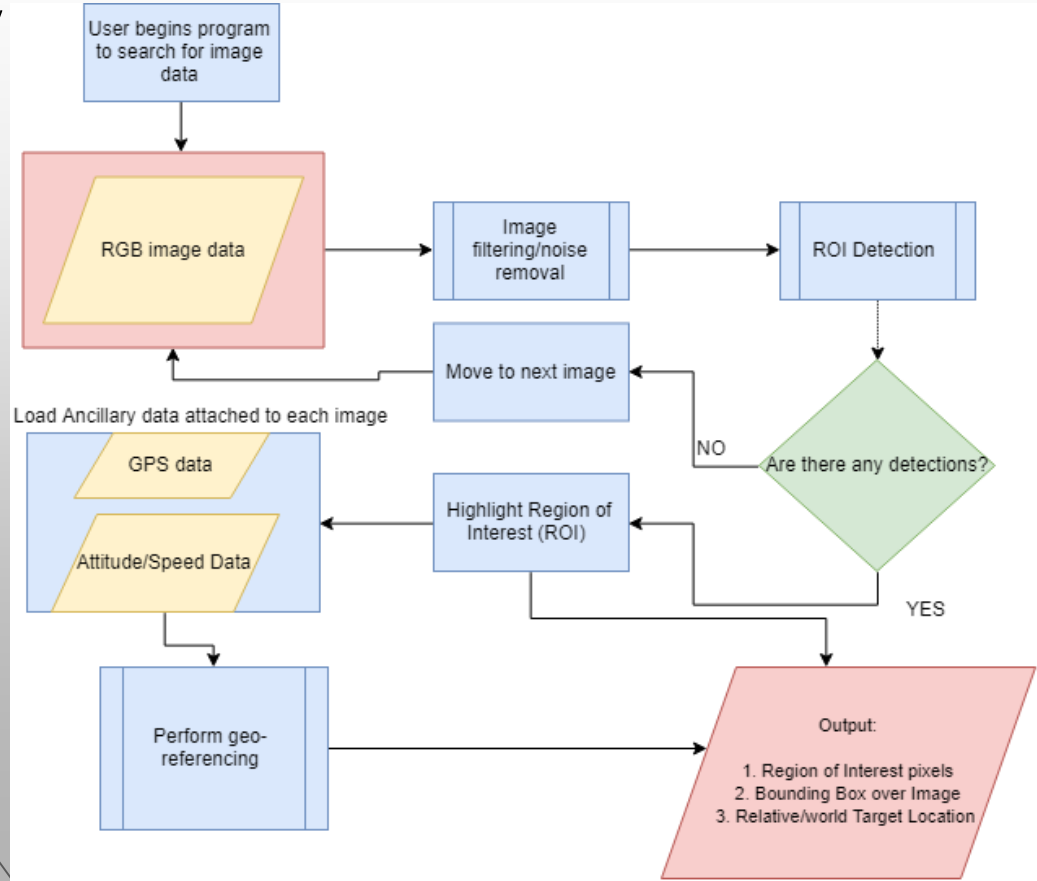
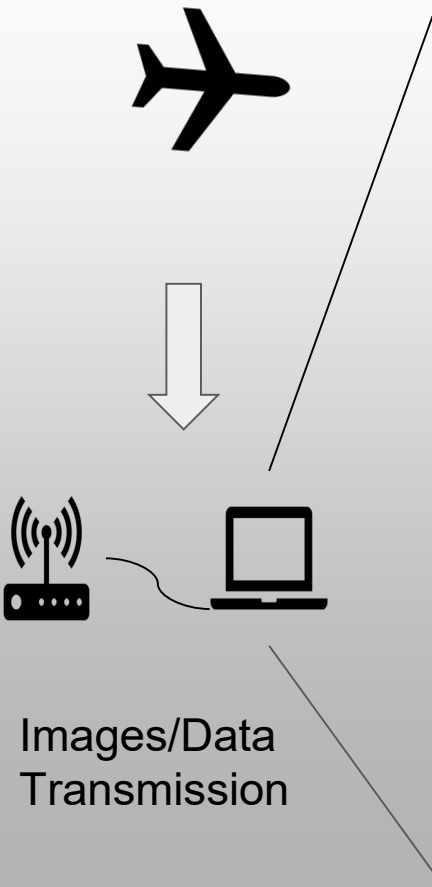
- Motor to be mounted below the airframe
- Low Profile Linear Bearing
- Small torsion spring to hold during launch



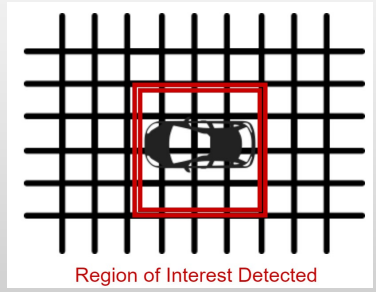
# Electronics



# Ground Processing: Region of Interest Detection and Location During Glide

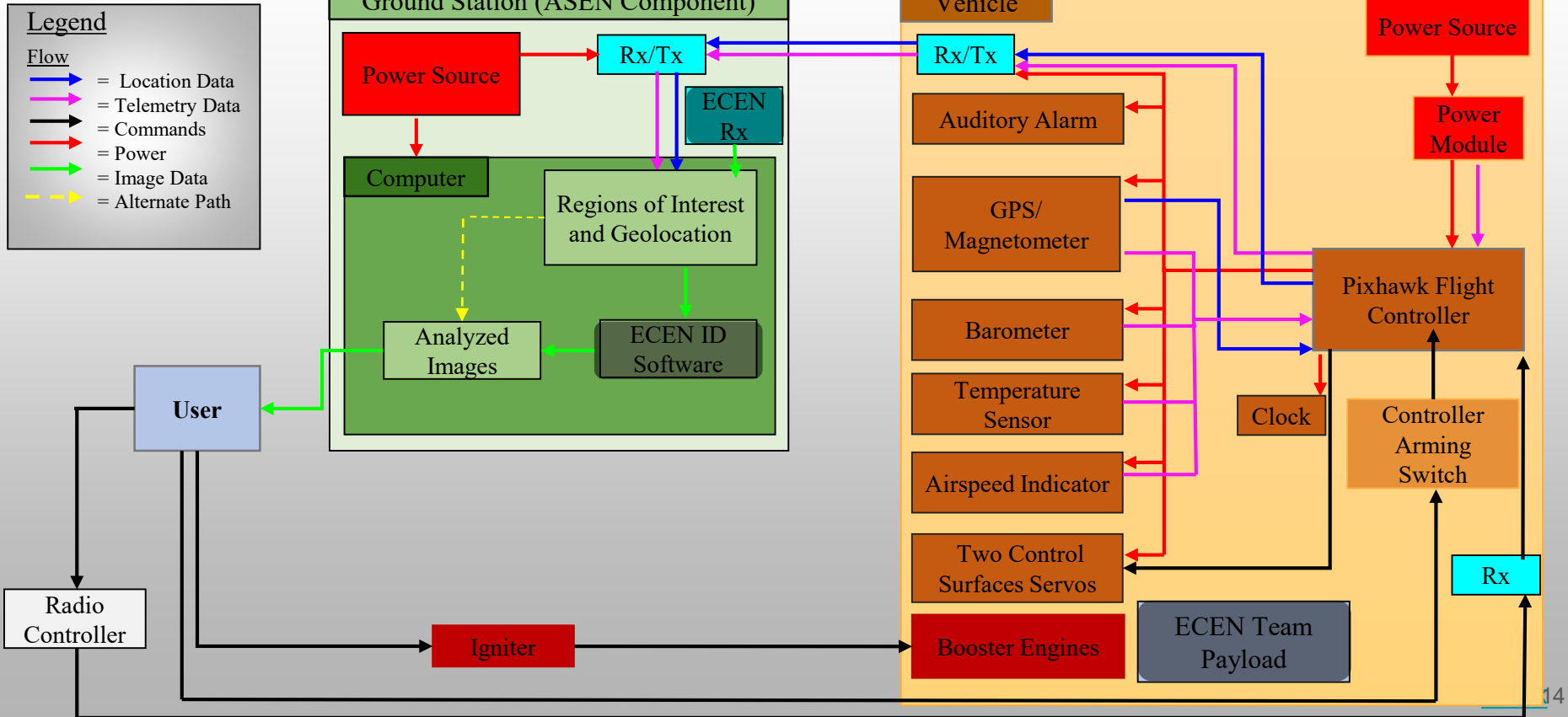


## Output



Latitude:	
Longitude:	
Distance:	

# RAPTR Functional Block Diagram



# Critical Project Elements

# CPE Selection

Aerial Vehicle Design

Vehicle and Payload Integration

Vehicle Electronics

Transmission and Reception

FAA compliance

Target Recognition/GeoLocation Software

Propulsion System

Control

**Intense Performance Requirements (FR1)**

**Complex Theory (FR5)**

**High Risk Propulsion System (FR4)**

**High Speeds (FR1 & FR4)**



# Design Requirements and Satisfaction

# Structural Requirements

Derived Requirements	Description
FR 1	The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.
DR 1.4	The vehicle shall withstand the forces of the launch and glide phases.

Structural  
Integrity  
(DR 1.4)

# Structural Requirements

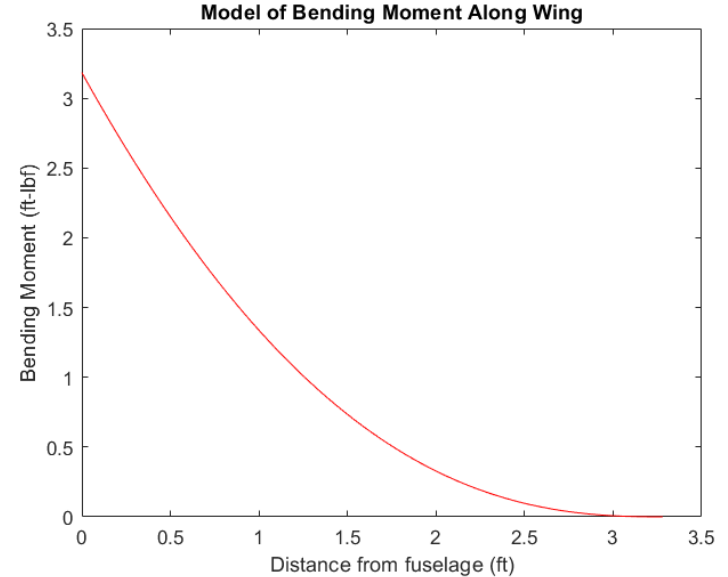
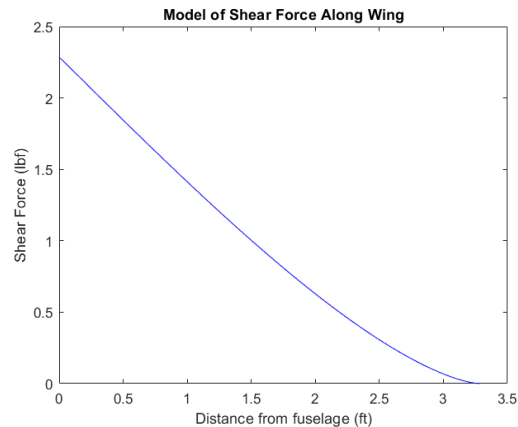
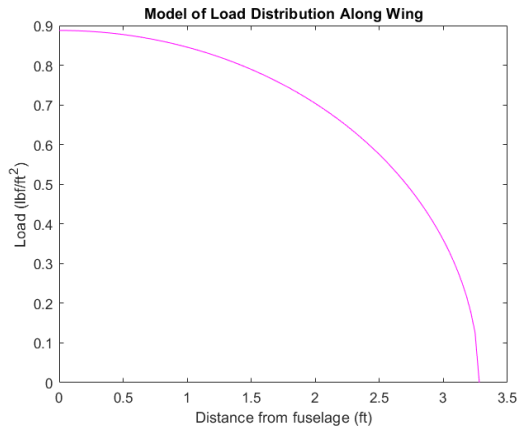
Derived Requirements	Description
DR 1.4	The vehicle shall withstand the forces of the launch and glide phases.

A Matlab model of shear force and bending moment along the wing.

Flexure Formula for 0.25" diameter rod → slight climb  $\sigma_{\max} = 12,457$  psi

Material	$\sigma_y$ [psi]	FOS (slight climb)
Balsa	2,828	0.227
Al-6061	40,000	3.211
Steel	53,700	4.310
Carbon Fiber	82,762	6.643

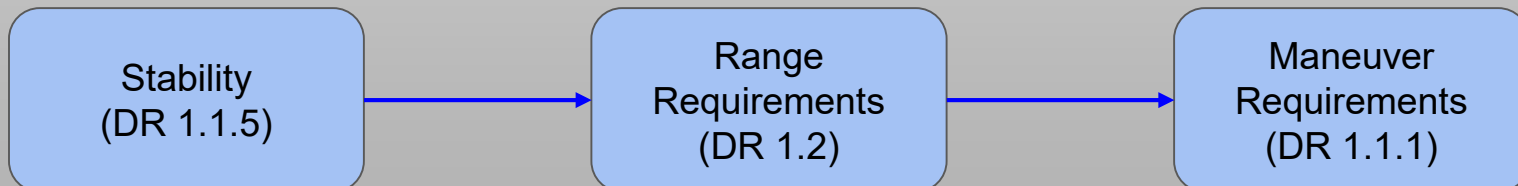
# Structural Requirements



Structural Integrity  
(DR 1.4) ✓

# Vehicle Performance Requirements

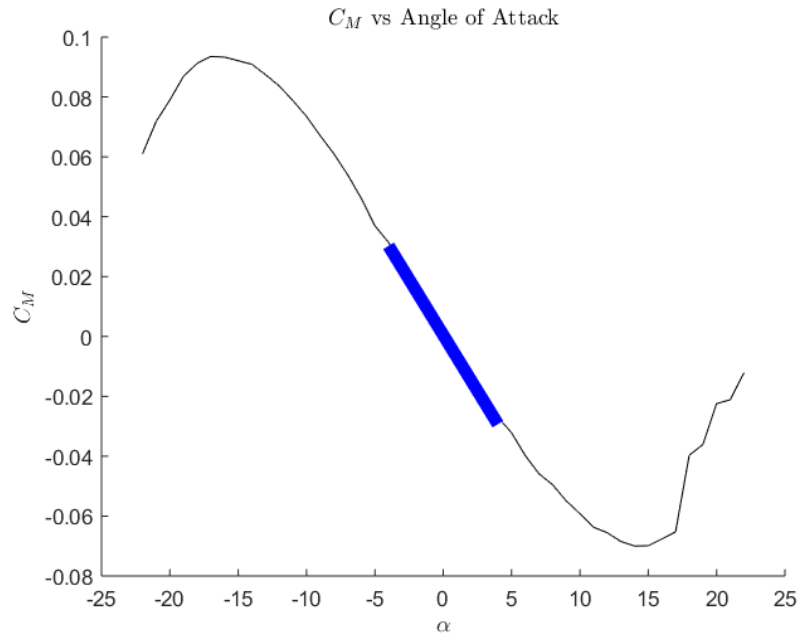
Requirement	Description
FR 1	The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.
DR 1.1.5	The vehicle shall exhibit natural stability in all phases of flight.
DR 1.1.1	The vehicle shall be capable of a turn radius of 350 feet.
DR 1.2	The vehicle shall achieve a glide slope less than or equal to 5.7 degrees.



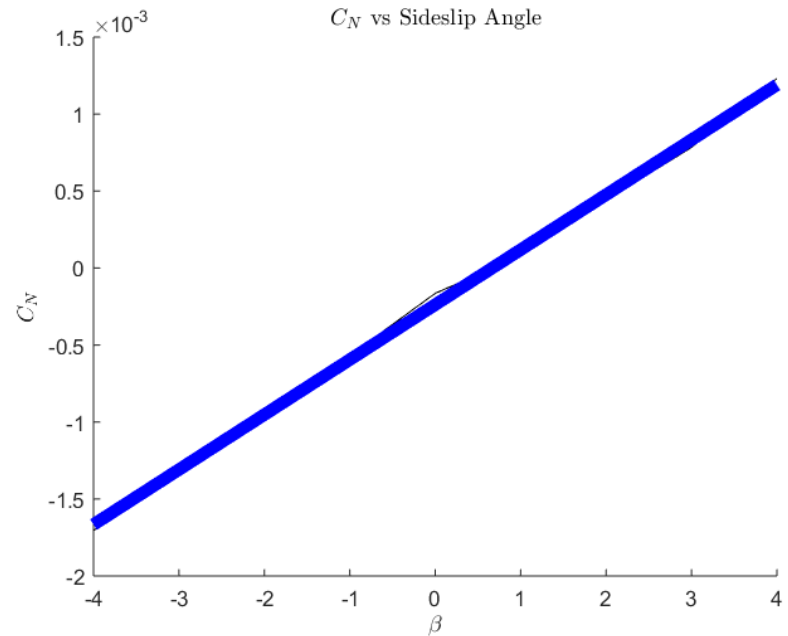
# Aerodynamics - Stability Analysis

CFD Analysis	Datcom Analysis
Solidworks model imported to ANSYS Fluent	Input file containing geometry information
Vary angle of attack, sideslip angle, and velocity	Calculates most stability derivatives
Calculate [X,Y,Z] forces and [l,m,n] moments for each case	Used in conjunction with CFD to confirm and improve results

# Stability Results



$$C_{m_\alpha} = -0.4143$$



$$C_{n_\beta} = 0.0248$$

# Thrust and Glide Phase Stability

	Static Margin
Glide Phase	0.90
Thrust Phase	1.45

- Calculated values of static margin
- Margin decreases after dropping motor but remains stable in both phases

	$C_{n\beta}$
Glide Phase	0.0248
Thrust Phase	0.0283

- Calculated values of yaw stiffness
- Margin decreases after dropping motor but remains stable in both phases

Stability  
(DR 1.1.5) ✓

Range Requirements  
(DR 1.2)

Maneuver Requirements  
(DR 1.1.1)



# Range Requirements

Derived Requirements	Description
DR 1.2	The vehicle shall achieve a glide slope less than or equal to 5.7 degrees.

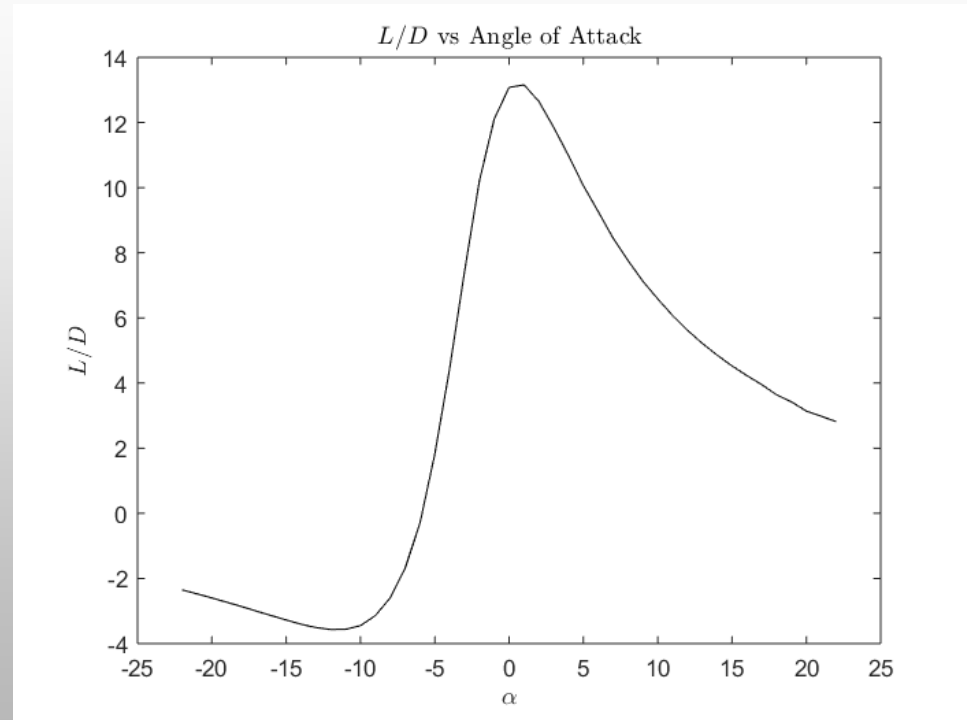
- Mission range: 3,000 foot glide with less than 300 foot drop

## Satisfaction of DR 1.2

$$L/D_{max} = 13$$

$$\gamma = \tan^{-1} \left( \frac{1}{L/D} \right)$$

$$\gamma = 4.4^\circ$$



Launch Error Correction  
(DR 1.1)

Range Requirements  
(DR 1.2) ✓

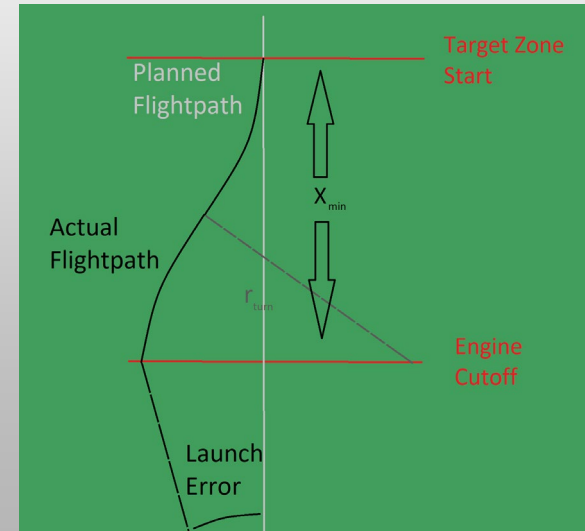
Maneuver Requirements  
(DR 1.1.1)

# Maneuver Requirements

Derived Requirements	Description
DR 1.1.1	The vehicle shall be capable of a turn radius of 350 feet.

- Course correction - After engine cut-off
- Roughly 1000 feet of downrange to correct

$$r_{turn} = X_{min} \left[ 2 \sin \left( \arctan \frac{1000 \tan \sigma_{launch}}{X_{min}} \right) \right]^{-1}$$



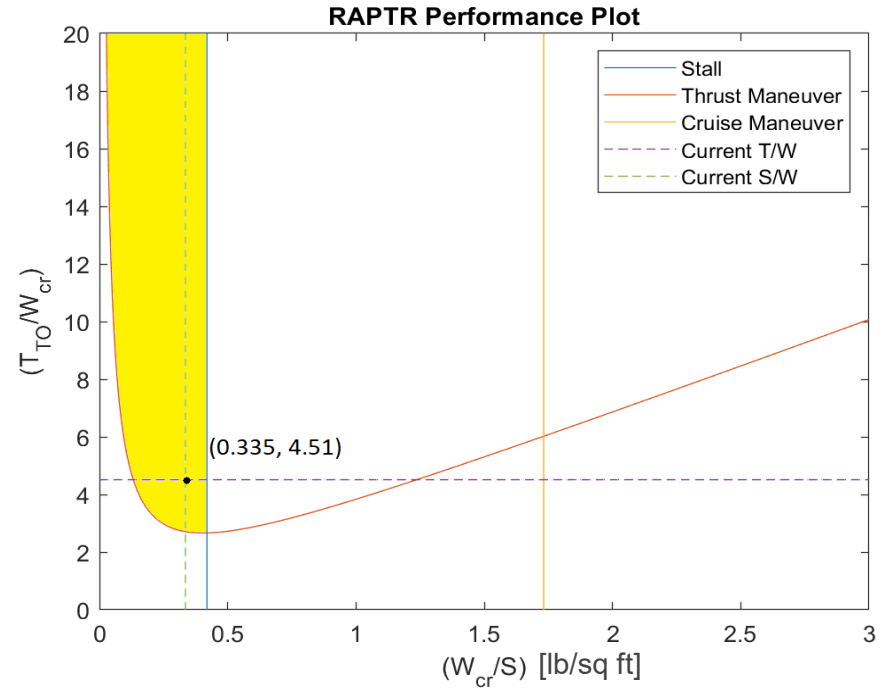
Launch Error Correction  
(DR 1.1)

Range Requirements  
(DR 1.2)

Maneuver Requirements  
(DR 1.1.1)

# Satisfaction of DR 1.1.1

Requirement: Capable of executing 350 foot radius turn



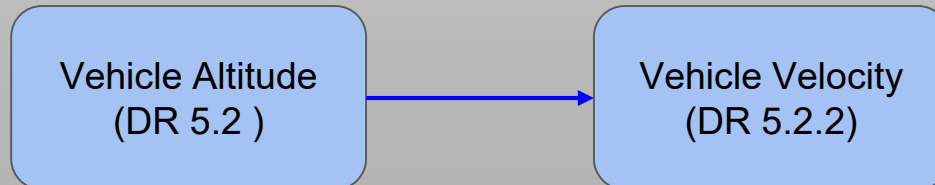
Launch Error Correction  
(DR 1.1)

Range Requirements  
(DR 1.2)

Maneuver Requirements  
(DR 1.1.1) ✓

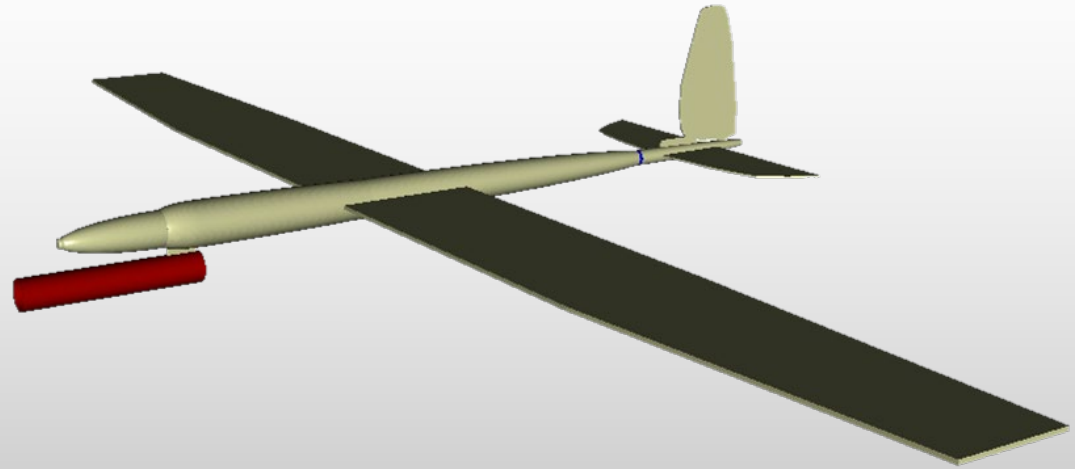
# Propulsion Requirements

Requirement	Description
FR 5	The system shall complete its mission (launch to images processed) within 3 minutes.
DR 5.2	The vehicle shall take 35 seconds to travel 2000 ft laterally and 700 ft vertically.
DR 5.2.1	The vehicle shall utilize a rocket engine propulsion system.
DR 5.2.2	The vehicle shall attain a speed of at least 100 feet per second.



# Propulsion Model

- Three Models
  - RockSim: 3D CAD model
  - **OpenRocket**: 3D CAD model
  - MATLAB: Point -mass model
- Structural Differences
  - Cylindrical Frame
  - No Rocket Nose Cone
  - No Polyhedral Wings

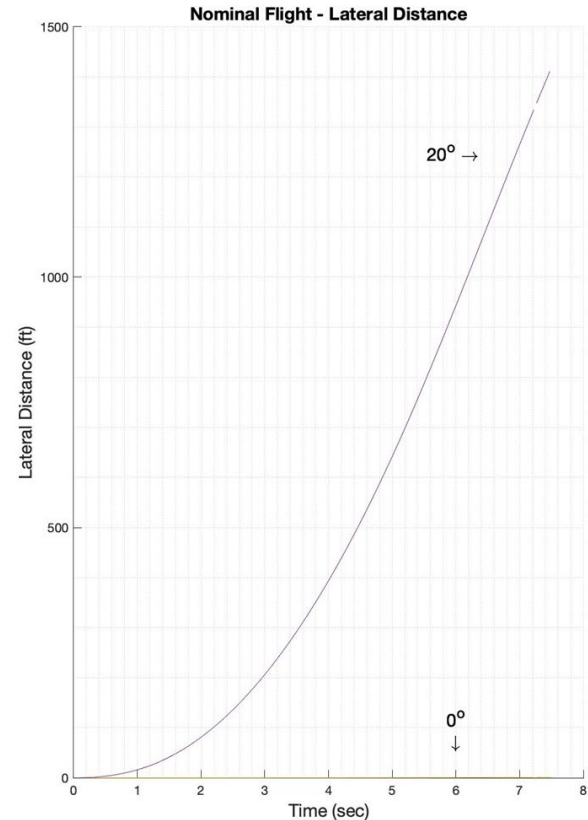
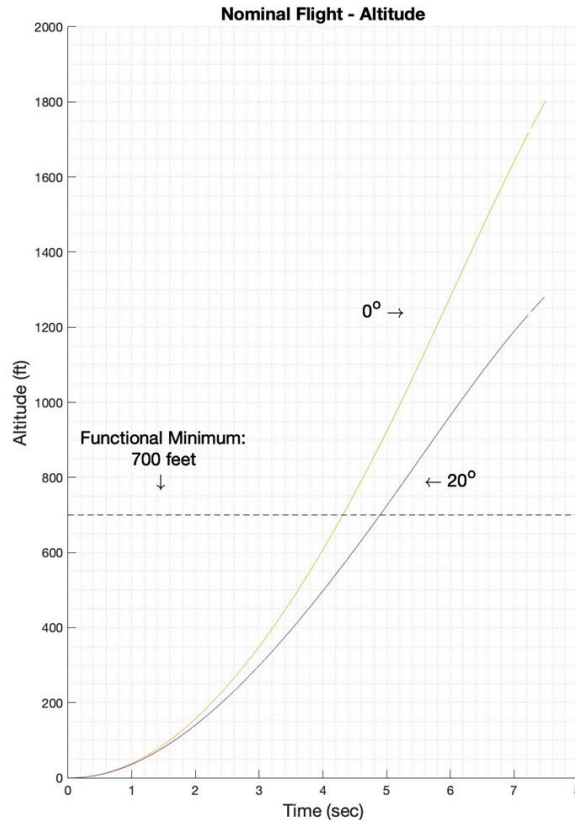


Initialization → Atmospheric Conditions → Flight Parameters → **Aerodynamic Forces and Moments** → **Thrust and Gravitational Forces** → Mass and Moment of Inertia → **Runge-Kutta 4th Order Numerical Integration**

Vehicle Altitude  
(DR 5.2)

Vehicle Velocity  
(DR 5.2.2)

# Nominal Propulsion Model

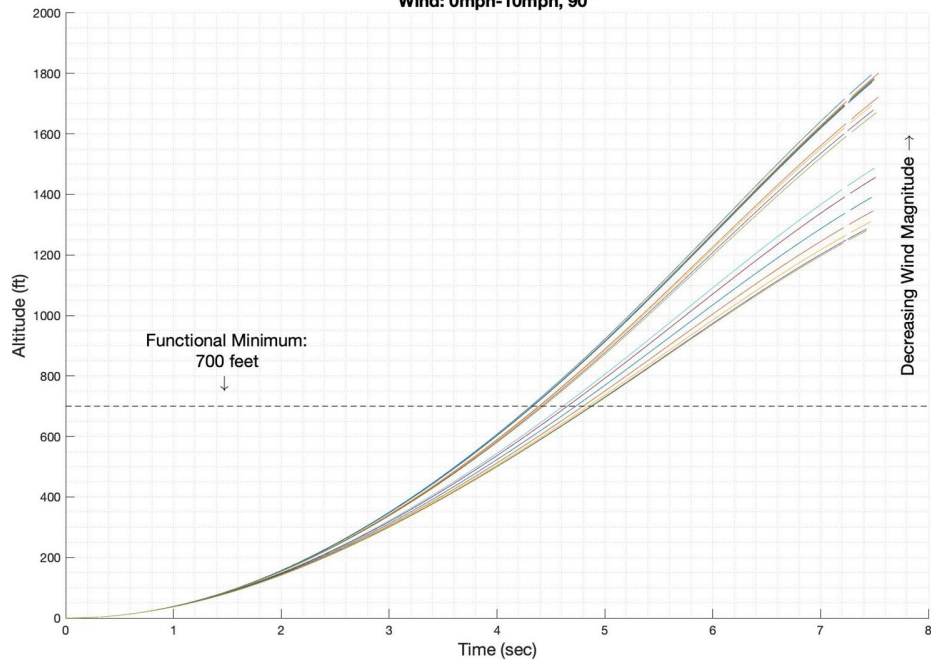


Vehicle Altitude  
(DR 5.2)

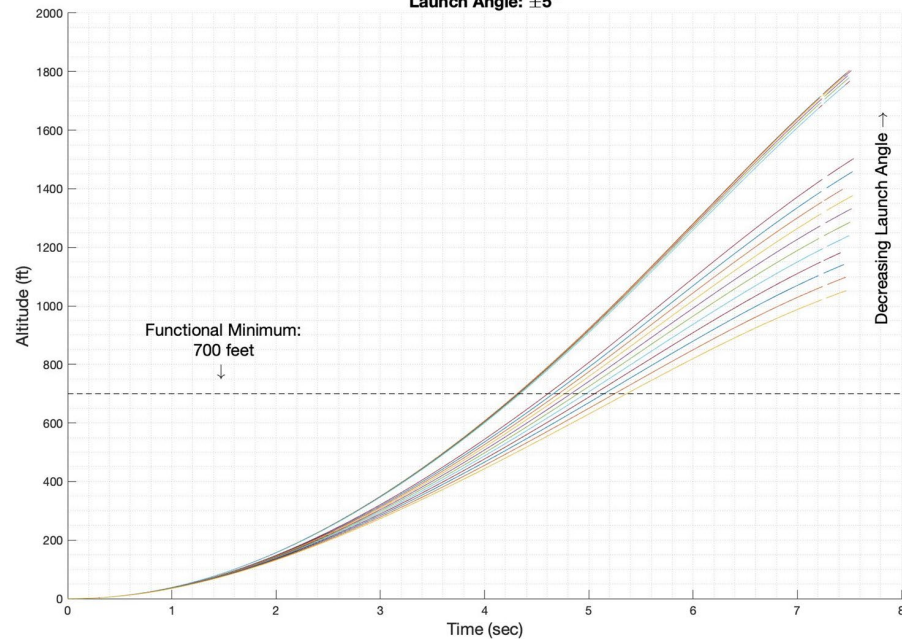
Vehicle Velocity  
(DR 5.2.2)

# Propulsion: Monte-Carlo

2D Trajectory  
Wind: 0mph-10mph, 90°



2D Trajectory  
Launch Angle:  $\pm 5^\circ$



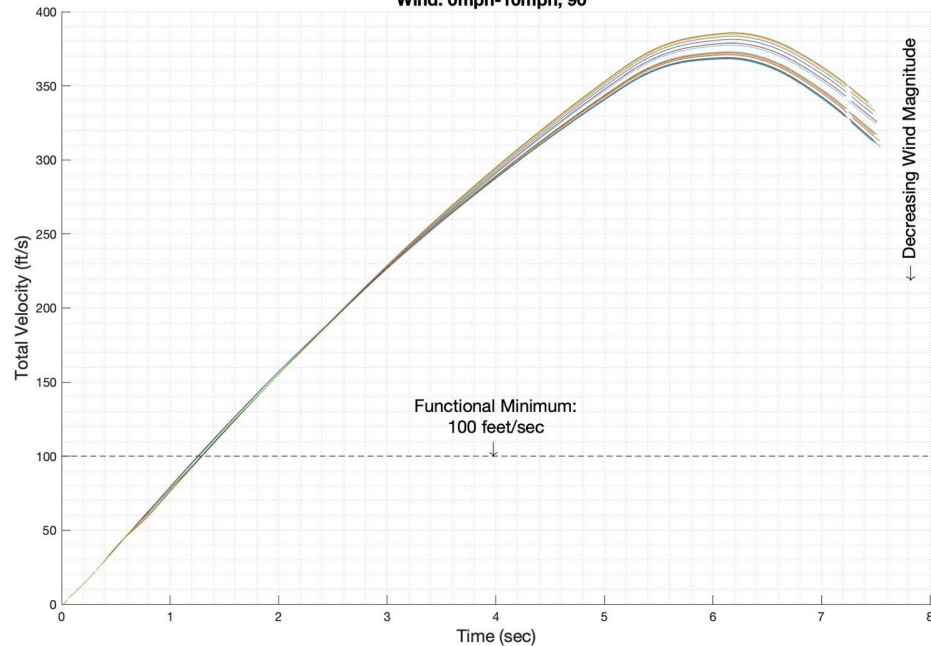
Vehicle Altitude  
(DR 5.2) ✓

Vehicle Velocity  
(DR 5.2.2)

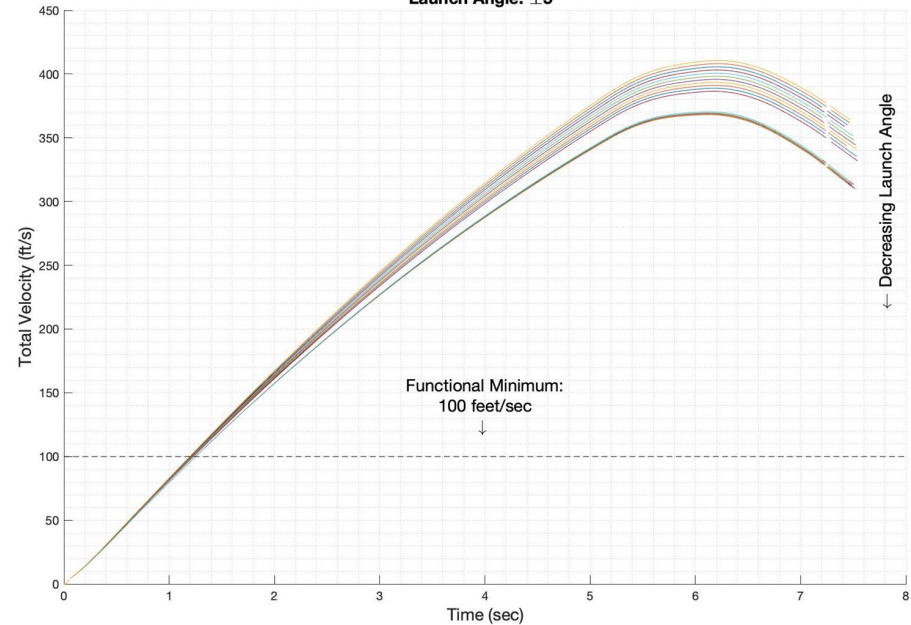


# Propulsion: Monte-Carlo

Propulsive Phase  
Total Velocity vs. Time  
Wind: 0mph-10mph, 90°



Propulsive Phase  
Total Velocity vs. Time  
Launch Angle:  $\pm 5^\circ$



Vehicle Altitude  
(DR 5.2)

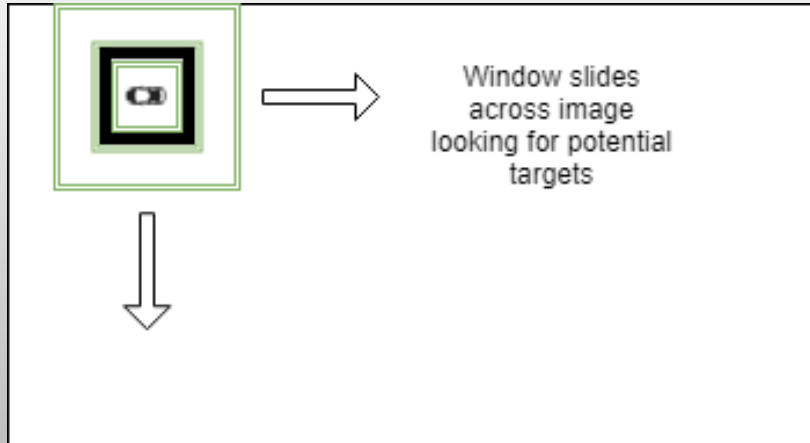
Vehicle Velocity  
(DR 5.2.2) ✓

# Target Recognition/Geolocation Software

Requirement	Description
FR 4	The system shall identify a distinctly colored target and relay the target's latitude and longitude.
DR 4.1	The ground station shall output a bounding box over potential targets.
DR 4.2	The ground station shall compute local relative coordinates of the target as well as global latitude and longitude of the target within 150 feet of its true location.

# Software: Target Detection

Compare statistics between windows using T-test:



Highlight regions of interest for classification and geolocation



$$T = \frac{|\bar{X}_1 - \bar{X}_2|}{\sqrt{s_1^2 + s_2^2}}$$

$\bar{X}$  = mean,  $s$  = variance

# Detection

## Identify Potential Target Pixels



## Output Bounding Box over ROI

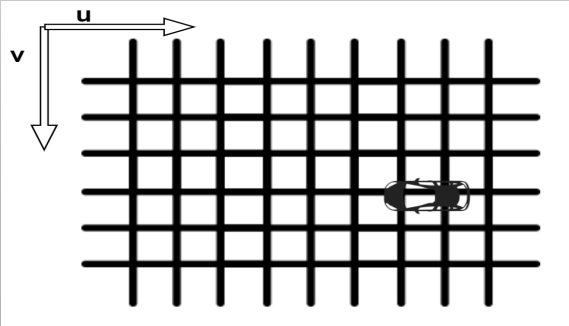


Output Bounding Box  
(DR 4.1) ✓

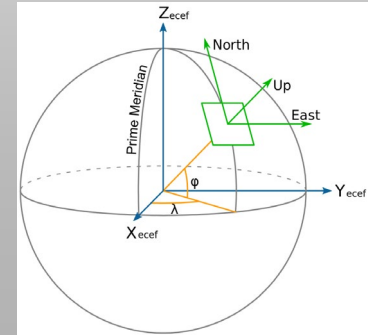
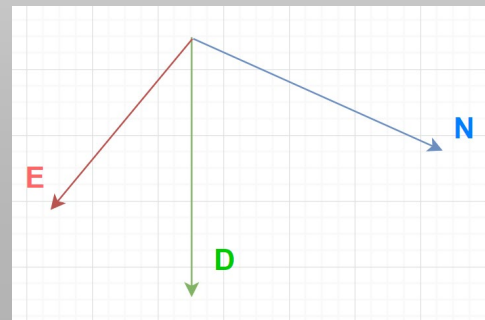
Determine Location of ROI  
(DR 4.2)

# Pixel to World Transformation

**Knowns: Pixels and altitude**

$$\begin{bmatrix} u \\ v \\ R \text{ (range)} \end{bmatrix}$$


**Unknown: World Coordinates**

$$\begin{bmatrix} N \text{ (north)} \\ E \text{ (east)} \\ D \text{ (down)} \end{bmatrix}$$


# Pixel to World Transformation

**Problem to solve:**

$$\tilde{P} \tilde{p}_w = x_s$$

$$x_s = \begin{bmatrix} u \\ v \\ 1 \\ R(\text{range}) \end{bmatrix}$$

$$\tilde{p}_w = \begin{bmatrix} N(\text{north}) \\ E(\text{east}) \\ D(\text{down}) \\ 1 \end{bmatrix}$$

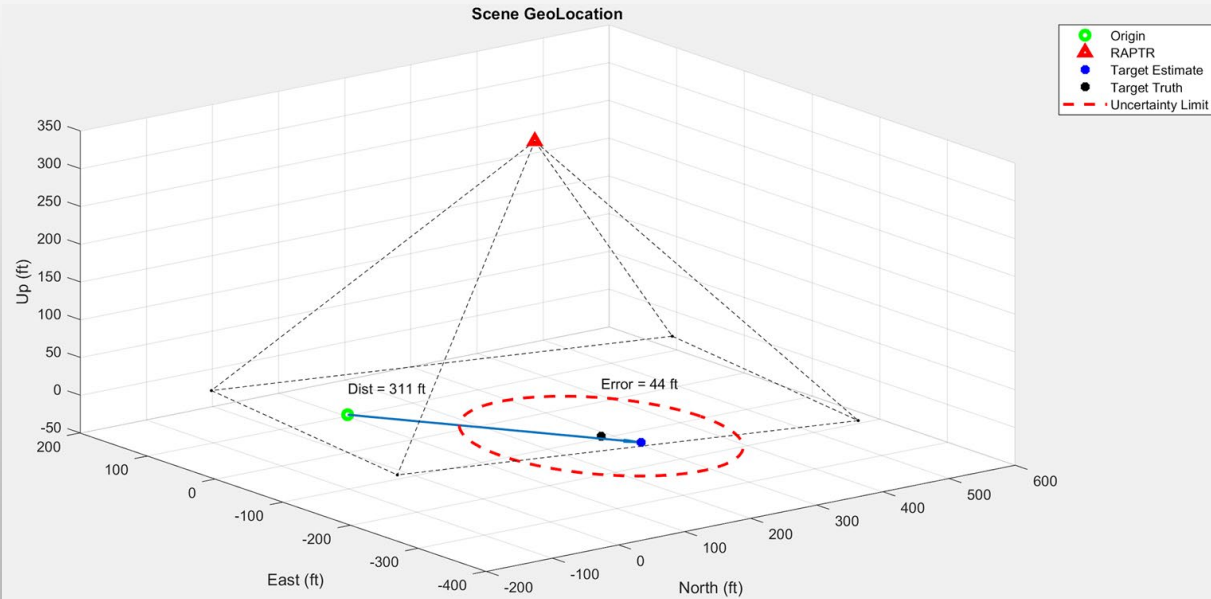
$$P = K(R|t) \quad \tilde{P} = \begin{pmatrix} K & 0 \\ \mathbf{0}^T & 1 \end{pmatrix} \begin{pmatrix} R & t \\ \mathbf{0}^T & 1 \end{pmatrix}$$

$K \equiv$  Camera Matrix

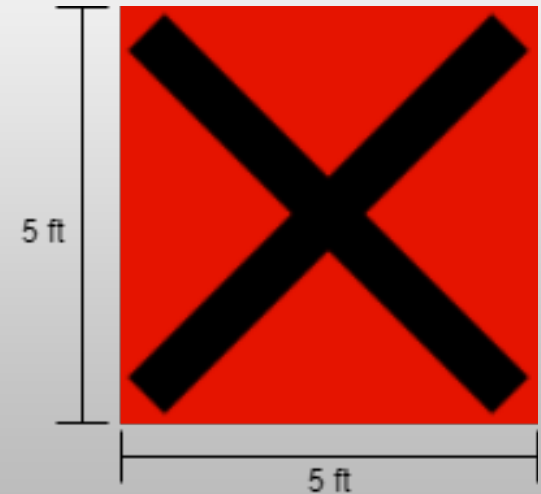
$R \equiv$  world to camera rotation

$t \equiv$  world to camera translation

# Geo-Location Preliminary Testing



## Example Target:



Output Bounding Box  
(DR 4.1)

Determine Location of ROI  
(DR 4.2) ✓

# Vehicle Control Requirements

Derived Requirements	Description
FR 1	The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.
FR 4	The system shall identify a distinctly colored target and relay the target's latitude and longitude.
DR 1.1.2	The vehicle shall be capable of being controlled by the user.
DR 4.2.1	The vehicle shall use a sensor suite to quantify its location.

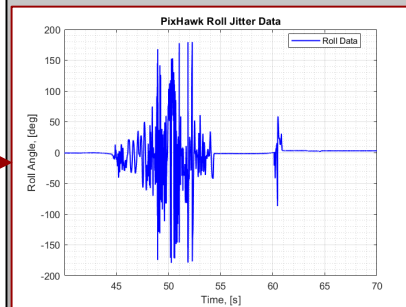
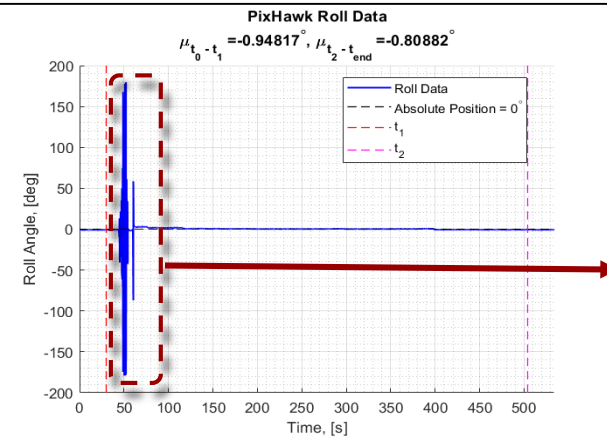
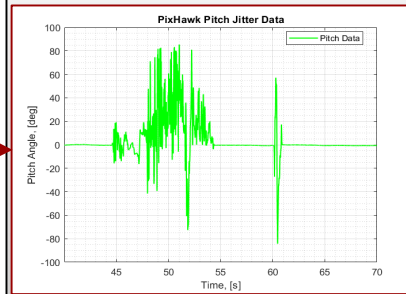
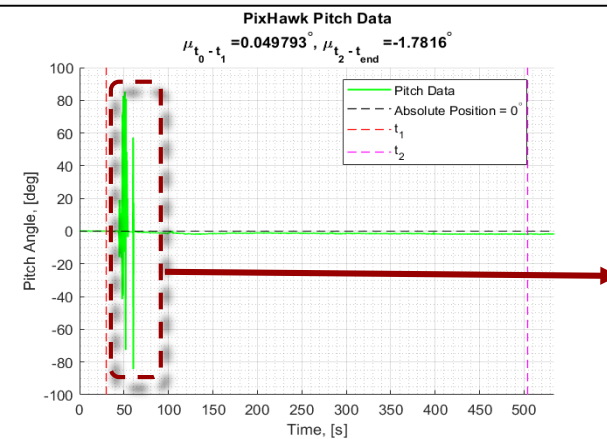
Sensor Attitude  
Determination  
(DR 4.2.1)



Capable Vehicle  
Control  
(DR 1.1.2)



# Sensor Attitude Determination



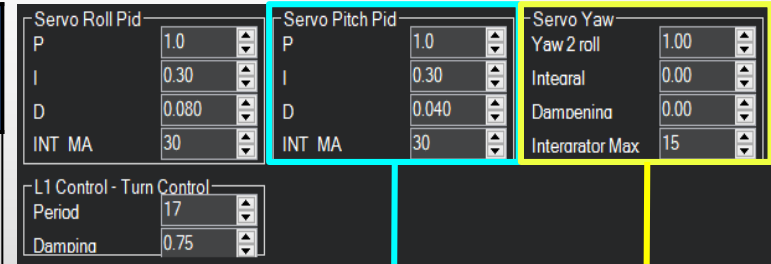
Measurement	Accuracy of Measurement
GPS Position	Within 2.5 meters
GPS Velocity	+/- 0.164 ft/s
Airspeed	+/- 0.82 ft/s
Magnetic Heading	+/- 0.3 degrees

Sensor Attitude Determination  
(DR 4.2.1) ✓

Capable Vehicle Control  
(DR 1.1.2)

# Vehicle Control

Control Surface	Function
<b>Rudder</b>	Enable both yaw and roll control due to RAPTR's dual dihedral. Enables lateral stability
<b>Elevator</b>	Enables pitch control and longitudinal stability



Elevator

Rudder

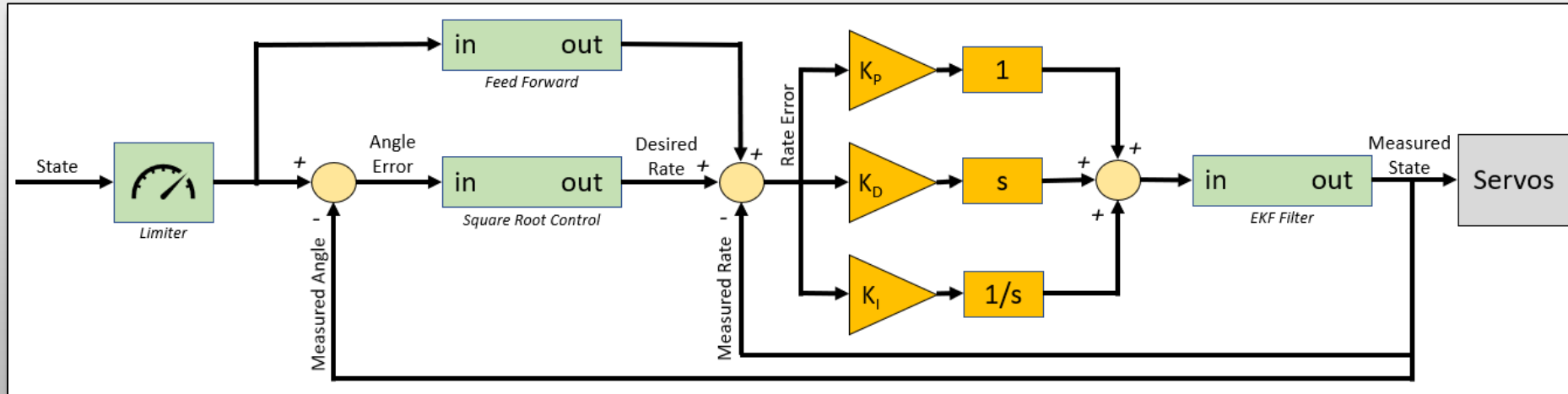
RAPTR does not have ailerons so servo roll gains are irrelevant.

Sensor Attitude Determination  
(DR 4.2.1)

Capable Vehicle Control  
(DR 1.1.2)

# Vehicle Control

## Pixhawk Control Architecture



Sensor Attitude Determination  
(DR 4.2.1)

Capable Vehicle Control  
(DR 1.1.2)

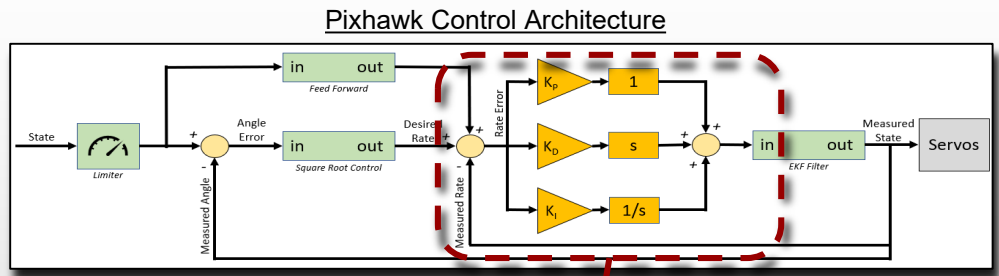
# Vehicle Control

## Fundamental Equations

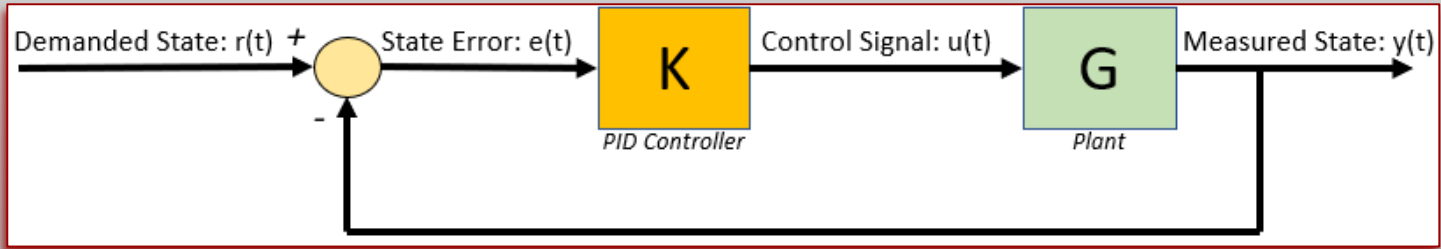
$$\dot{\vec{x}} = A\vec{x} + B\vec{u} \quad y = C\vec{x} + D\vec{u}$$

$$X(s) = \underbrace{C(sI - A)^{-1}B}_{G(s)}\vec{u}$$

$$K(s) = K_P + K_D s + K_I \frac{1}{s}$$



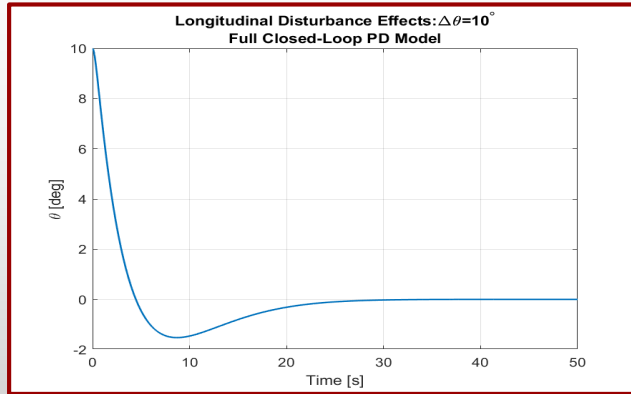
## PID Gain Approximation Architecture



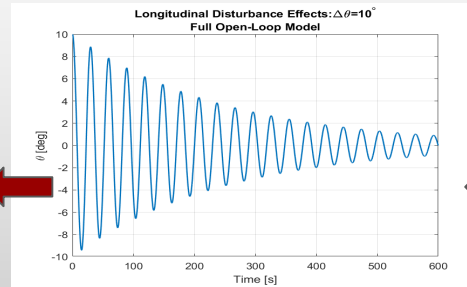
Sensor Attitude Determination (DR 4.2.1)

Capable Vehicle Control (DR 1.1.2)

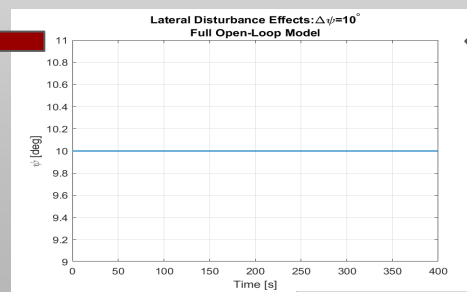
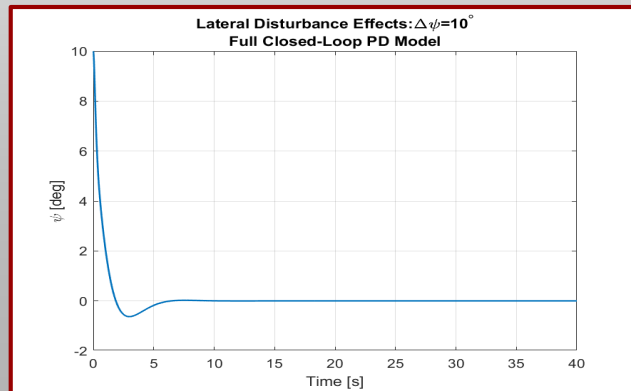
# Vehicle Control



**Closed-Loop Dynamics**



**Open-Loop Dynamics**



Dynamic Modes	PID Servo Gains
<b>Pitch</b>	$K_P = 0.0154$ $K_D = 0.0069$ $K_I = 0$ , assumption
<b>Yaw</b>	$K_P = 0.178$ $K_D = 0.075$ $K_I = 0$ , assumption

Sensor Attitude Determination  
(DR 4.2.1)

Capable Vehicle Control  
(DR 1.1.2) ✓

# Project Risks

# Risk Matrix

		Impact				
		L		M		H
Probability	H		6	10		
				11		
	M		7	8	13	3
		12	9			
	L	1		5	2	4

Risks
1. Uneven Rocket Engine Moments
2. Wing Integrity on Launch
3. Ascent Pitch Control Authority
4. Autopilot Adaptation
5. NAR Certification/FAA Testing Permission
6. Communication System Interference
7. Payload Weight
8. Payload Volume
9. Physical Payload/Vehicle Integration
10. Rocket Thermal Effects
11. Data Transmission Rate
12. Data Synchronization
13. Image Processing Time

# Risk Mitigation

		Impact				
		L		M		H
Probability	H		6	10		
				11		
	M		7	8	13	3
		12	9	10	3	
	L	1		5	2	4

Risk	Mitigation	Off-Ramp
3. Ascent Pitch Control Authority	Short Motor Mount	Utilize Smaller Rocket Motor or Electric Propeller System
10. Rocket Thermal Effects	Coat Vehicle Belly with Thermal Tape	Electric Propeller System



# Verification and Validation

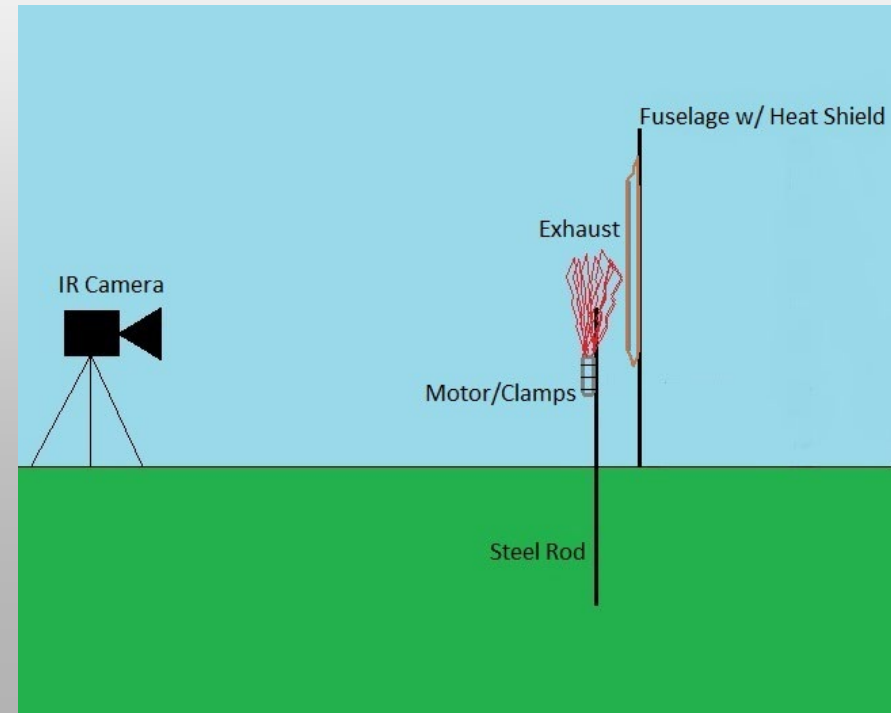
# Test Overview

Software	FR 4	The system shall identify a distinctly colored target and determine the unique target shape and relay the target's latitude and longitude.
Structures	DR 1.4	The vehicle shall withstand the forces of the launch and glide phases.
Thermal	DR 5.2.1	The vehicle shall utilize a rocket engine propulsion system
Aerodynamics	DR 1.2	The vehicle shall achieve a glide slope less than or equal to 5.7 degrees.
Controls	DR 1.1.2	The vehicle shall be capable of being controlled by the user.
Full Systems	FR's 1-6	

# Thermal Testing

FR 1 The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.

<b>Purpose</b>	Verify no damage to vehicle during engine burn
<b>Methods</b>	Static burn of motor positioned near fuselage
<b>Location</b>	Boulder East Campus
<b>Key Equipment</b>	Aluminum tape, Lava Heat Shield, I55 Motor, IR camera
<b>Measurements</b>	Temperature of exhaust, Dimensions of exhaust

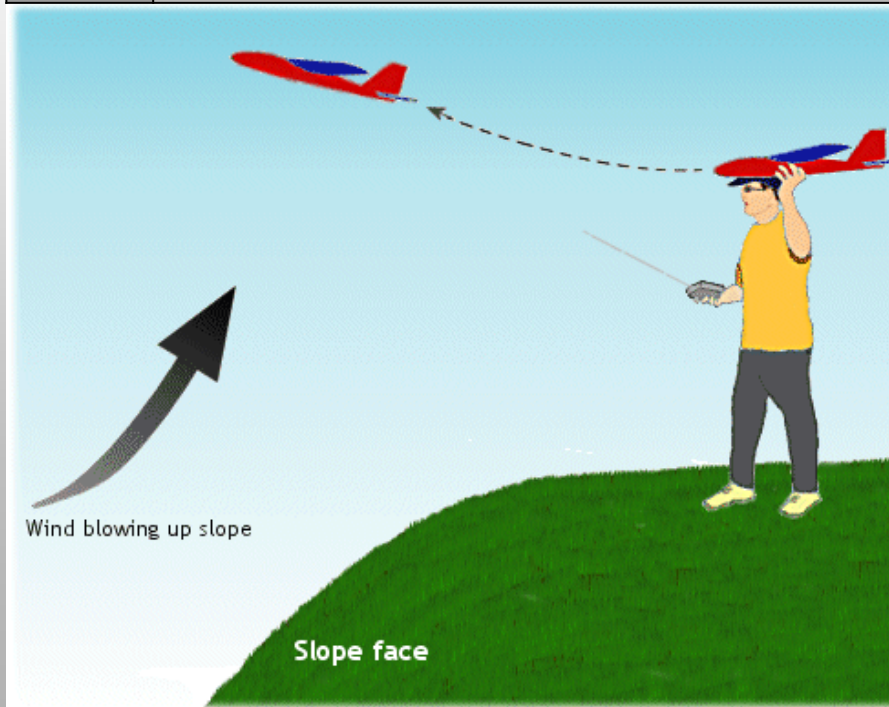


# Controls/Pixhawk

<b>Purpose</b>	Verify accurate control and authority over vehicle
<b>Methods</b>	Slope soar glider in AUTOTUNE mode of ArduPilot
<b>Location</b>	South NCAR
<b>Key Equipment</b>	Fully built AndREaS glider with transmitter controller
<b>Measurements</b>	Roll, Pitch, Yaw, Airspeed of glider

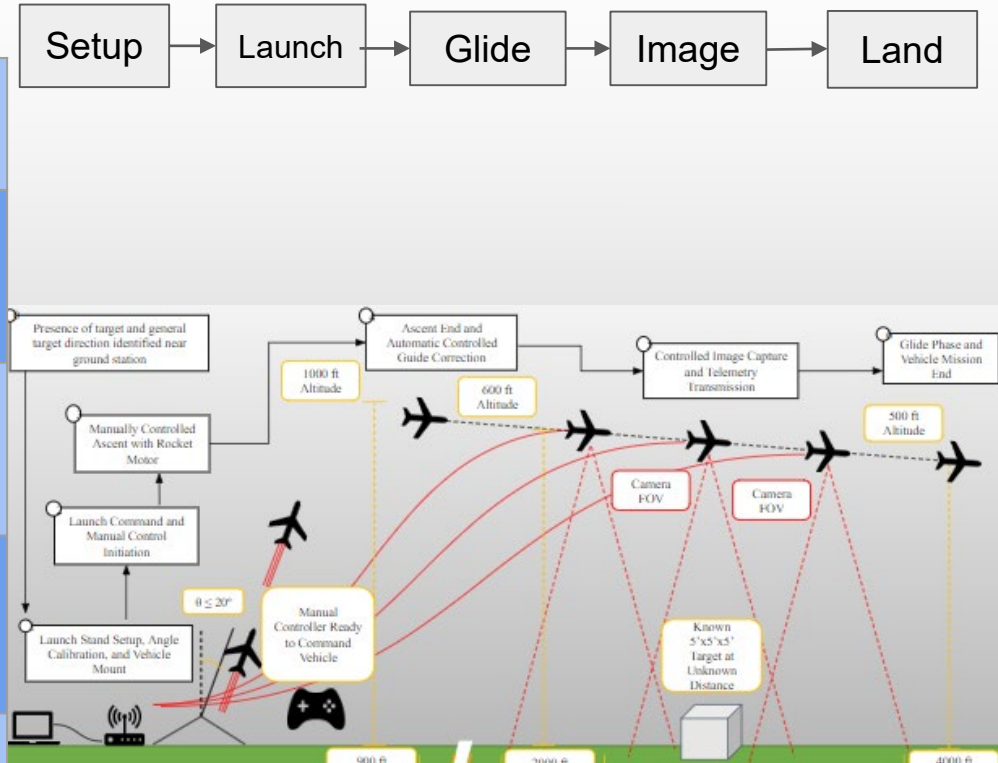
FR 1

The system shall survey a 2,000 foot long and at least 400 foot wide corridor beginning 2,000 feet from the user and aligned with a user defined heading.



# Full systems testing

<b>Purpose</b>	Validate success criteria of project are met
<b>Methods</b>	Full systems launch through NCR with and without payload
<b>Location</b>	Atlas Site, North Site (West of Pawnee Grasslands)
<b>Key Equipment</b>	Fully built AndREaS vehicle, launch rails, test target
<b>Measurements</b>	Vehicle position, velocity, attitude, time for setup/detection, images of target



# Project Planning

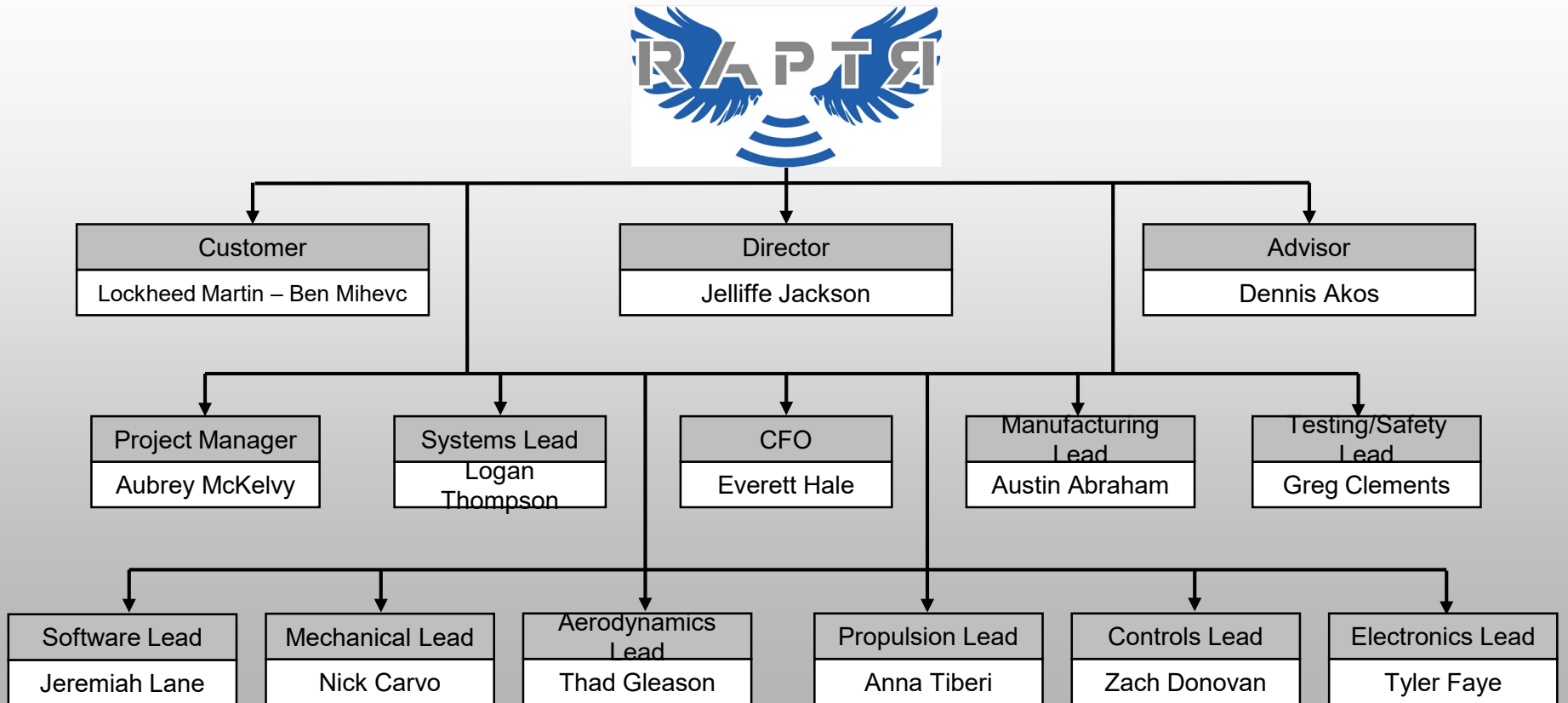
# Test Plan

**Thermal Testing:** Access to IR camera and static launch site

**Vehicle/Full Systems Testing:** Access to high powered rocket launch site

<b>Test Imaging (Software)</b>	11/19/18 (Additional Tests TBD)	Capture images for software testing	Boulder North Park
<b>Structural Test</b>	12/01/18	Verify structural integrity	ITLL
<b>Thermal Test</b>	01/14/19 - 02/01/19 (Exact Date TBD)	Verify thermal protection	East Campus
<b>Wind Tunnel Testing</b>	01/28/19 - 02/01/19 (Exact Date TBD)	Verify CFD Analysis	ITLL
<b>Communications Integration Test</b>	02/04/19 - 02/08/19 (Exact Date TBD)	Verify comm. systems	ITLL
<b>Controls Testing/Tuning</b>	02/04/19 - 02/15/19 (Exact Date TBD)	Tune PixHawk and verify controllability	South NCAR
<b>Vehicle Systems Testing</b>	03/02/19 03/09/19 03/30/19	Test launch vehicle without payload	Northern Colorado
<b>Full Systems Testing</b>	04/06/19 04/13/19 05/03/19	Test launch vehicle with payload	Northern Colorado

# Organizational Chart





# Work Breakdown



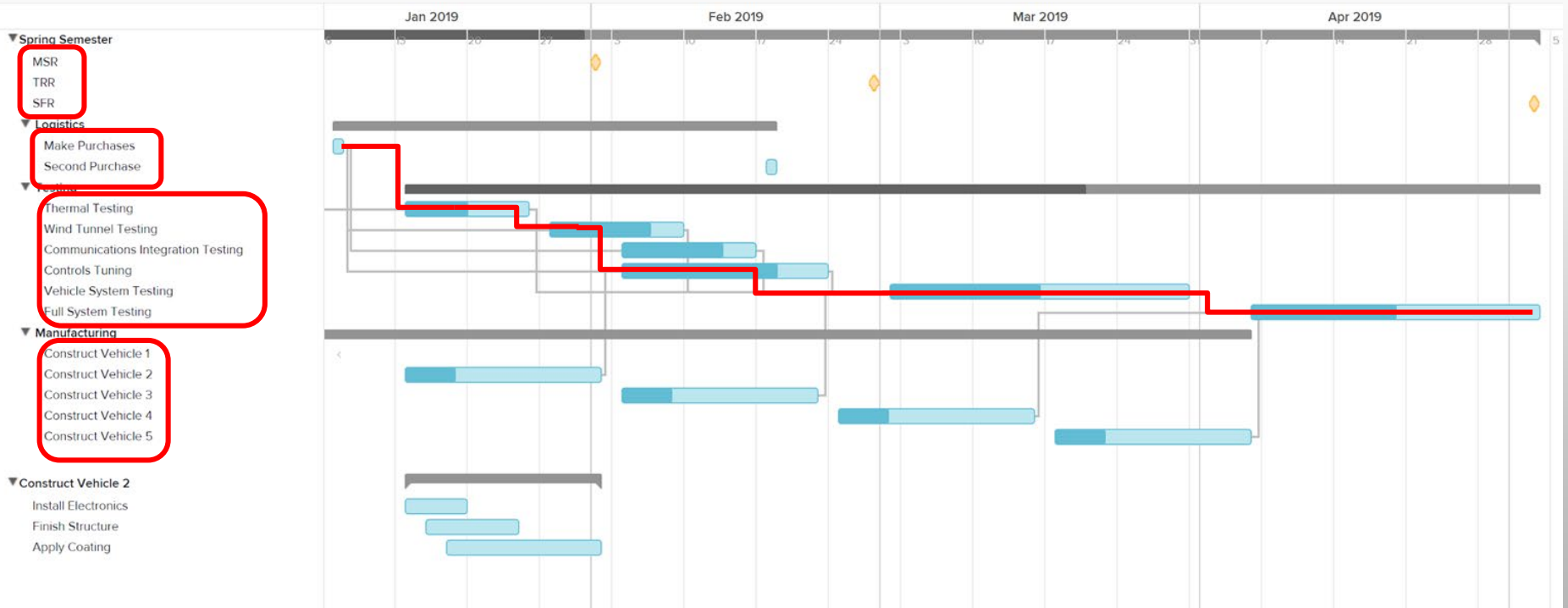
## Legend



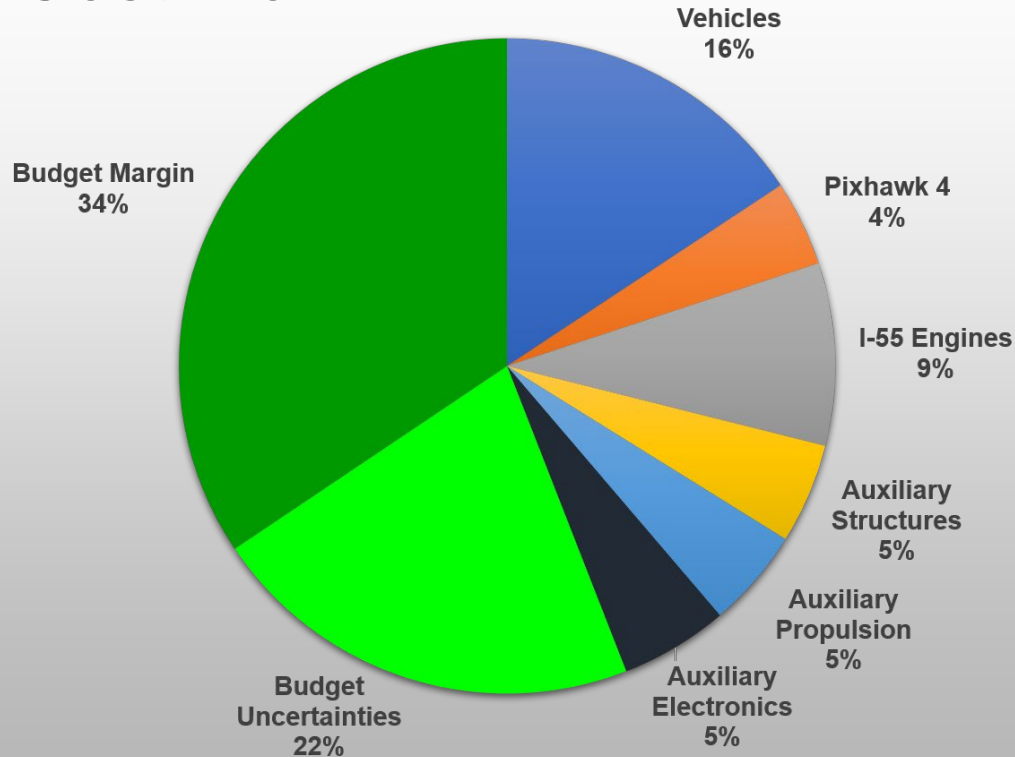
Planned

Hardware	Software	Electronics & Controls	Propulsion	Aerodynamics	Fall Deliverables	Spring Deliverables
Vehicle CAD Model	Geolocation Algorithm	Wiring Diagram	Launch Dates and Sites	CFD Modeling	PDD	MSR
Structural Analysis	ROI ID Algorithm	Approximate Gains	Motor Selection	Stability Derivatives	CDD	TRR
Vehicle Assembly	Uncertainty Propagation	Controller Simulation	Propulsive Simulation	Stability Verification	PDR	SFR
Structural Testing	Preliminary Test Validation	Finalize Gains	Motor Acquisition	Control Derivatives	CDR	
Finalize Vehicle	Optimization	Validate Controls	Thermal Testing	Wind Tunnel Testing	FFR	
Integration and Test	Integration and Test	Integration and Test	Integration and Test	Integration and Test		

# Gantt Chart



# Cost Plan



Expenditure	Cost
Vehicles	\$785
Pixhawk 4	\$211
I-55 Engines	\$450
Auxiliary Structures	\$247
Auxiliary Propulsion	\$245
Auxiliary Electronics	\$266
<b>Expected Cost</b>	<b>\$2204</b>
Budget Uncertainties	\$1075
<b>Maximum Cost</b>	<b>\$3279</b>
<b>Budget Margin</b>	<b>\$1721</b>

# Acknowledgements

- Ben Mihevc
- Theresa Brown
- Tim Moon
- Eileen Liu
- Dr. Akos
- Professor Gerren
- Professor Holzinger
- Professor Rhode
- Professor Lopez
- Christine Reilly & Ian Cooke
- Professor Nabity
- Professor Ahmed
- Professor Lawrence
- Arielle Blum
- CU Boulder Quadcopter Club
- IRIS
- James Mack
- Dan Hesselius
- Joe Hinton

# Questions?

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[http://szeliski.org/Book/drafts/SzeliskiBook\\_20100903\\_draft.pdf](http://szeliski.org/Book/drafts/SzeliskiBook_20100903_draft.pdf)
- <https://www.rocketarium.com/Build/Ejection-Baffles>
- <http://www.aerospaceweb.org/question/propulsion/q0220.shtml>
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- <https://cdn.automationdirect.com/static/manuals/d4user/ch8.pdf>
- <https://www.eucass.eu/doi/EUCASS2017-411.pdf>
- <https://core.ac.uk/download/pdf/52106533.pdf>
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- Design of Robust Controller of Fixed-Wing UAV for Transition Flight by Satoshi Kohno and Kenji Uchiyama
- Attitude Estimation for UAV Using Extended Kalman Filter by ofei Jing<sup>1</sup>, Jiarui Cui<sup>1</sup>, Hongtai He<sup>2</sup>, Bo Zhang<sup>3</sup>, Dawei Ding<sup>1</sup>, Yue Yang<sup>1</sup>
- Experimental validation of Unmanned Aerial Vehicles to tune PID controllers in open source autopilots by Pedro L. Jimenez\*, Jorge A. Silva\*\* and Juan S. Hernandez\*\*\*
- Modeling of Closed Loop PID Controller for an Auto-Pilot Aircraft Roll Control by E.Gouthami and M. Asha Rani
- Quadrotor Tuning for Attitude Control based on PID Controller using Fictitious Reference Iterative Tuning (FRIT) by Arthit Julkananusart\*, Itthisek Nilkhamhang\*, Rangsarit Vanijjirattikhan† and Atsushi Takahashi‡
- PIXHAWK: A System for Autonomous Flight using Onboard Computer Vision by Lorenz Meier, Petri Tanskanen, Friedrich Fraundorfer and Marc Pollefeys
- Dynamics of Flight Stability and Control by Bernard Etkin and Lloyd Duff Reid
- Feedback Control of Dynamic Systems by Gene Franklin

# Backup Slides

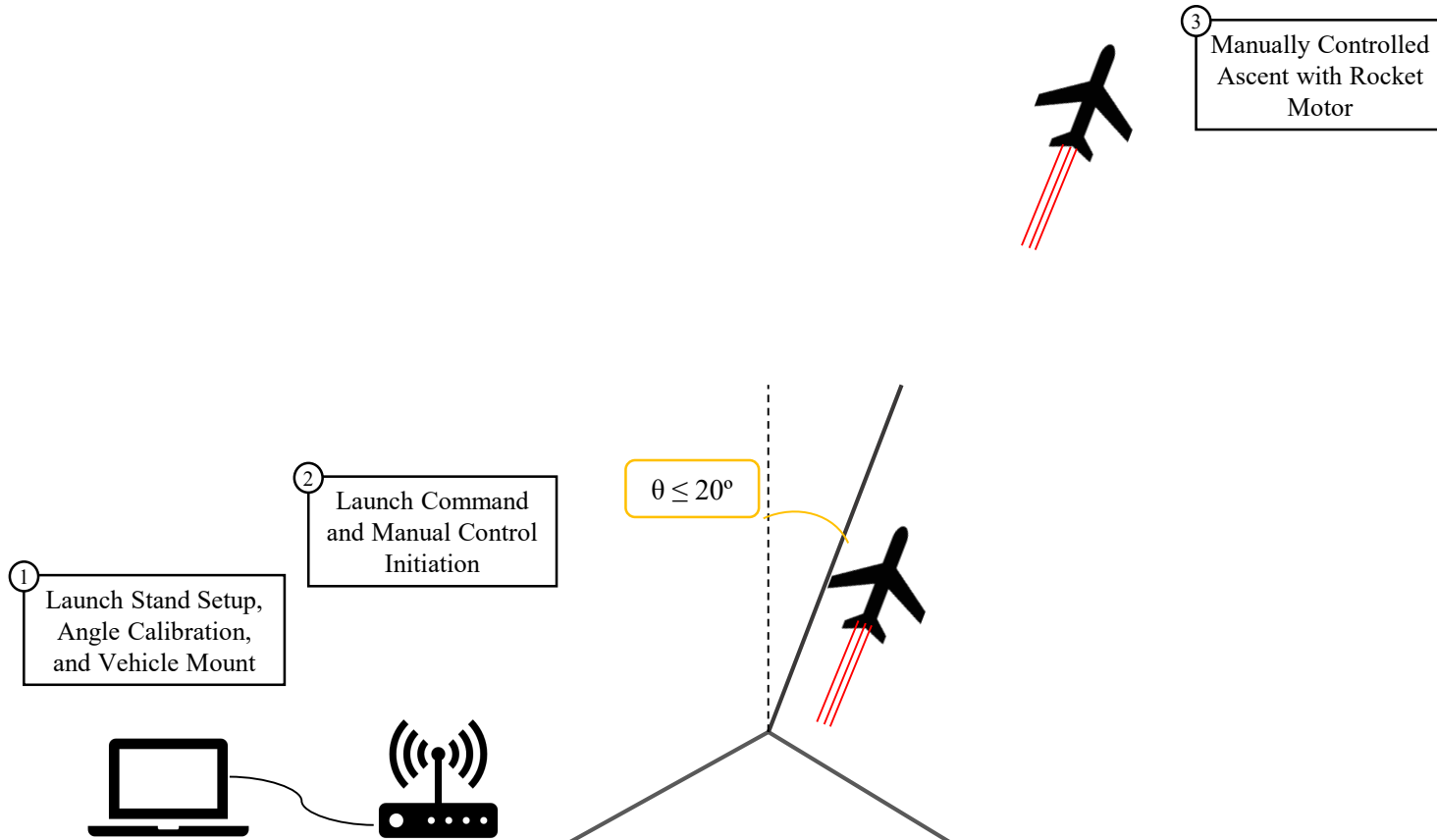
Index
<a href="#">Objectives</a>
<a href="#">Design Solution</a>
<a href="#">CPEs</a>
<a href="#">Requirements</a>
<a href="#">Risks</a>
<a href="#">Validation</a>
<a href="#">Planning</a>
<a href="#">Backups</a>



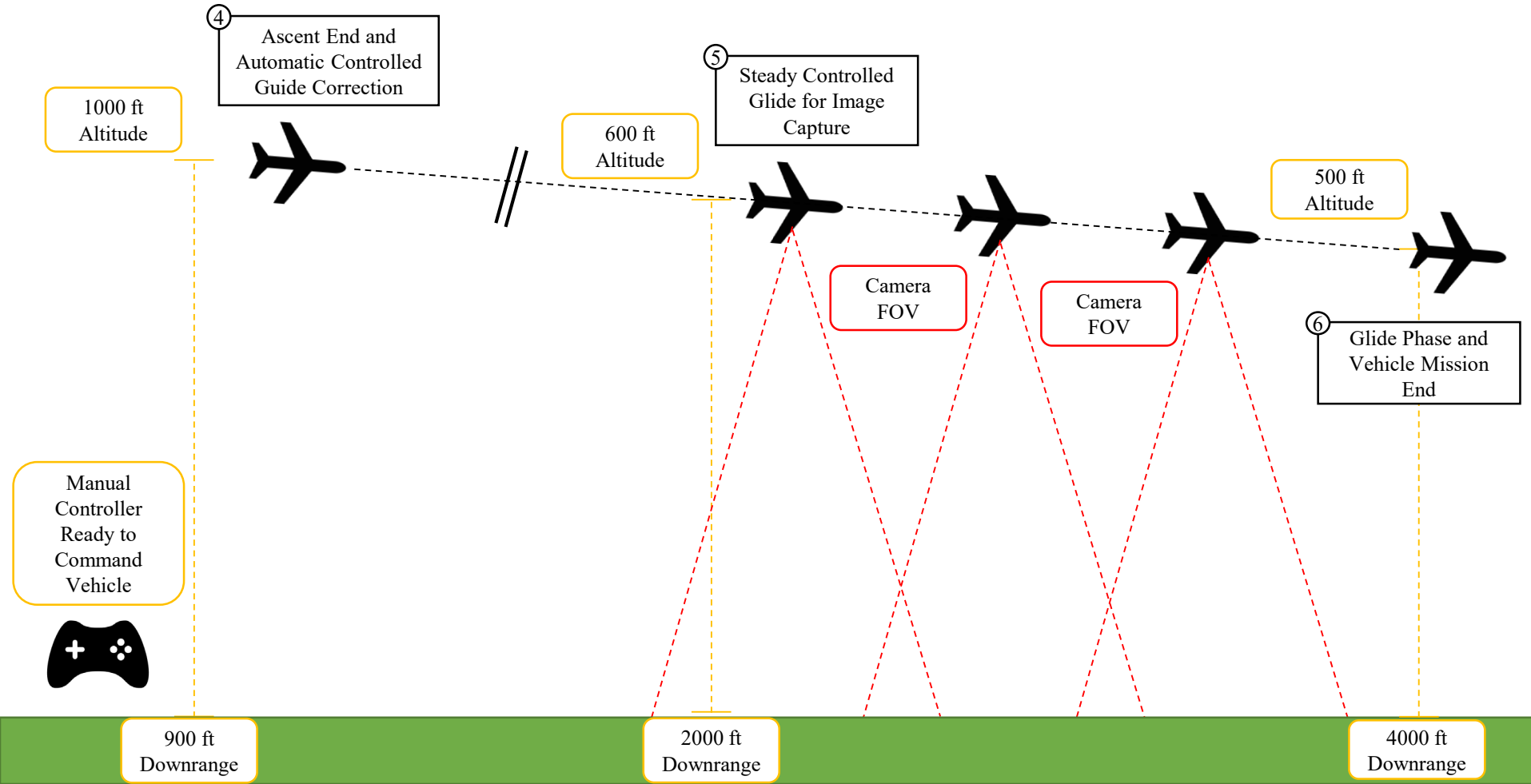
# Backup Slides

Backup Slides Index
<a href="#"><u>Project Planning</u></a>
<a href="#"><u>Aerodynamics</u></a>
<a href="#"><u>Electronics</u></a>
<a href="#"><u>Controls</u></a>
<a href="#"><u>Propulsion</u></a>
<a href="#"><u>Software</u></a>
<a href="#"><u>Structures</u></a>
<a href="#"><u>Testing</u></a>

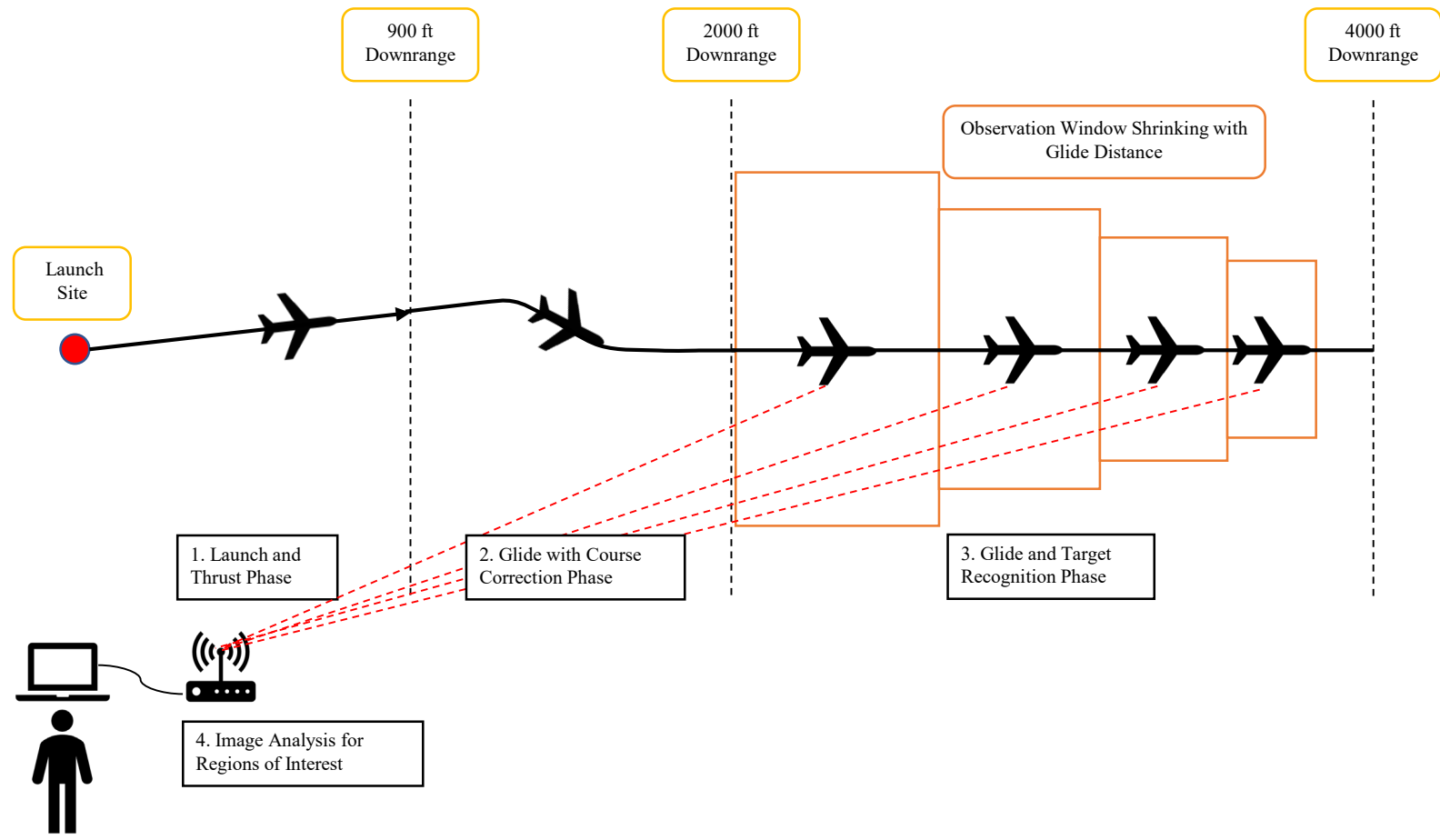
# RAPTR CONOPs – Launch Phase



# RAPTR CONOPs – Glide Phase



# RAPTR CONOPS — Mission Profile Top View



# Detailed Cost Breakdown - Subteams

Subteam	Minimum Budget	Budget Uncertainty	Maximum Budget
Electronics and Controls	\$477	\$405	\$882
Structures	\$1032	\$340	\$1372
Propulsion	\$695	\$330	\$1025
Totals	\$2204	\$1075	\$3279

# Detailed Cost Breakdown - Electronics

Item	Cost
Pixhawk 4 and GPS Module	\$211
Digital Airspeed Sensor	\$64.59
FrSky X8R Receiver	\$34.99
Radio Telemetry Set	\$45.00
Sevos (x2)	\$71.98
950mAh Battery	\$12.24
Voltage Regulator (x6)	\$3.24
Diode (x6)	\$9.42
Printed Circuit Board (x10)	\$15.00

# Detailed Cost Breakdown - Structures

Item	Cost
AndREaS Glider (x4)	\$560.32
Oracover Monokote (x4)	\$77.92
Carbon Rod (x4)	\$21.92
Bearing Carriage	\$6.26
Guide Rails	\$15.00
Manufacturing Supplies	\$36.86
Pre-CDR Purchases	\$314.05

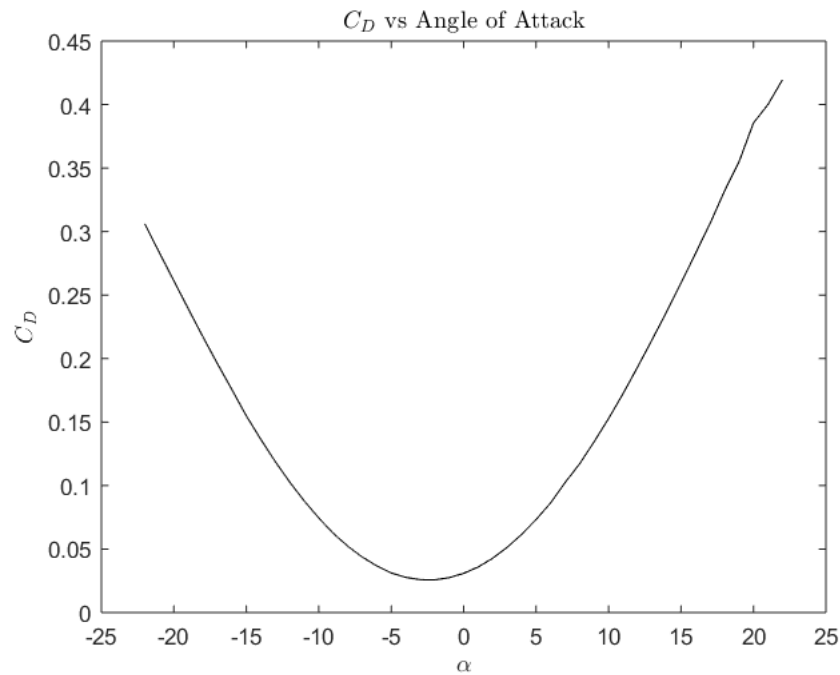
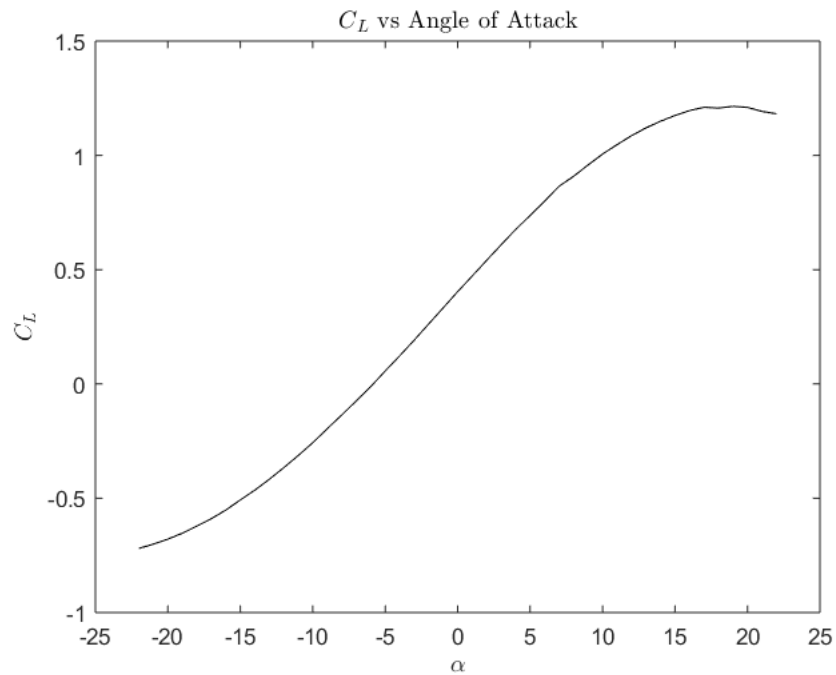
# Detailed Breakdown - Propulsion

Item	Cost
Nose Cone (x3)	\$24.94
Parachute (x3)	\$3.63
I-55 Engine (x10)	\$450.00
Grain Casing (x3)	\$39.75
Launch Controller	\$39.99

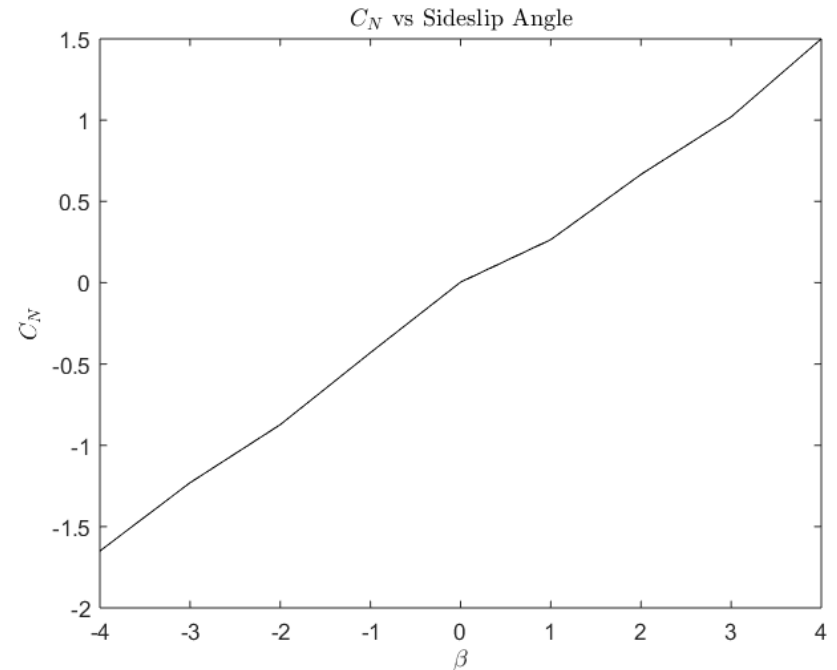
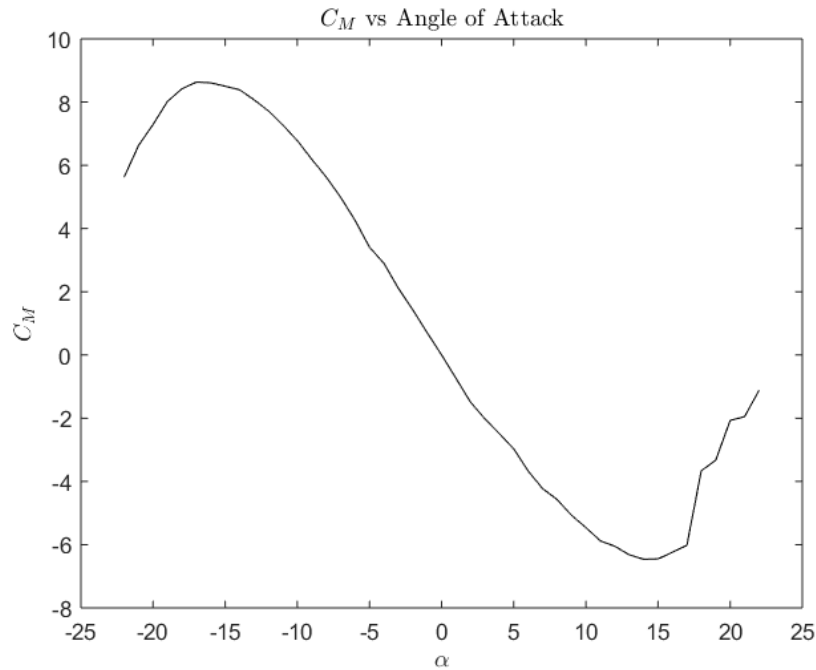


# Aero Backup Slides

# Lift and Drag - CFD



# Pitching and yawing moment - CFD



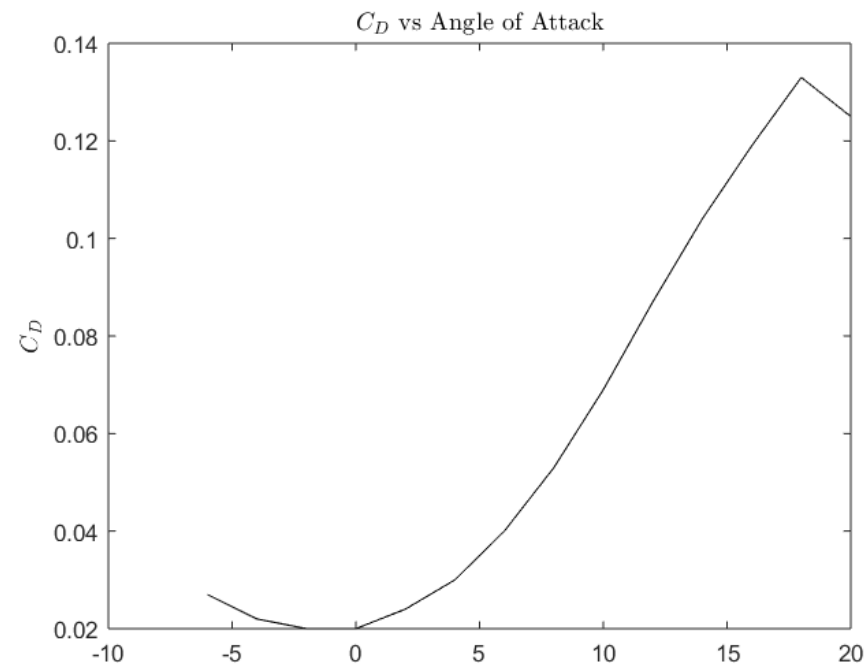
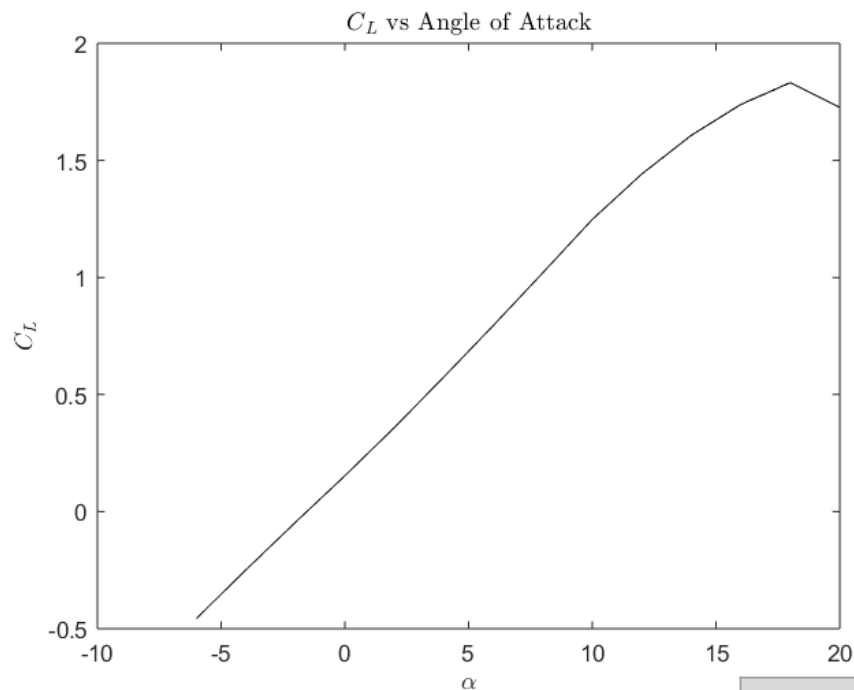
# Digital Datcom Input

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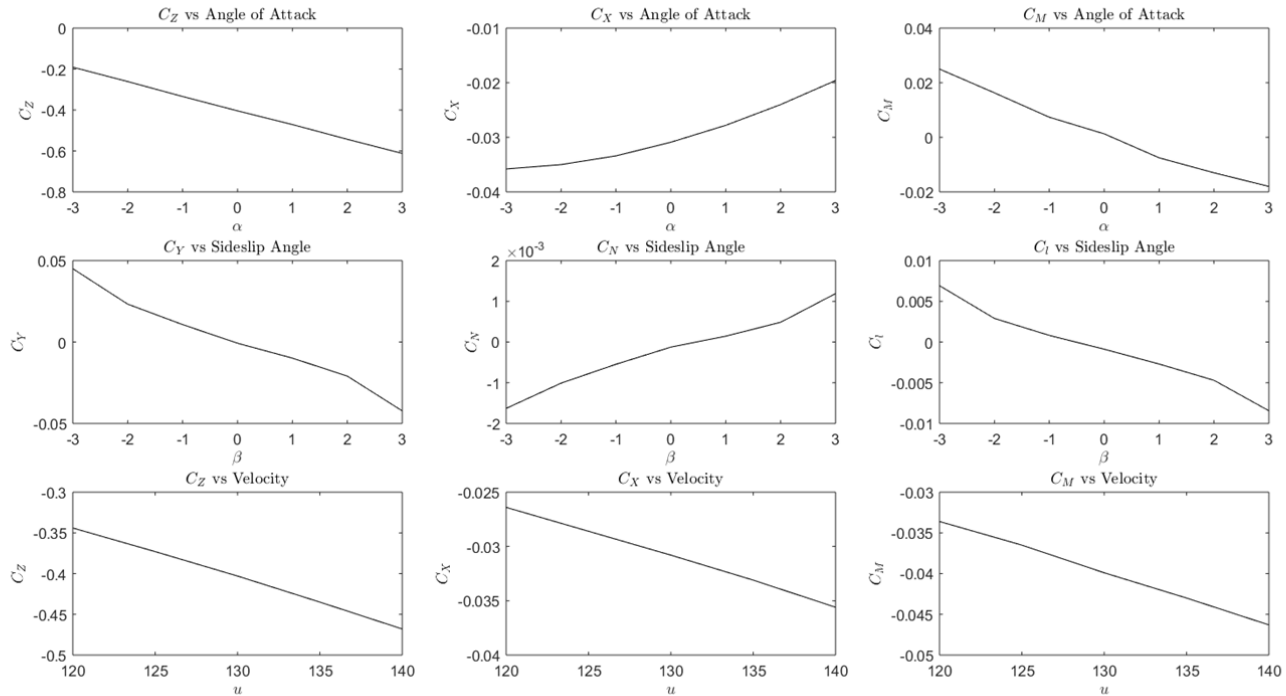
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NEXT CASE

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# Lift and Drag - Datcom



# Stability Plots



# Control Derivatives

## Results from CFD analysis

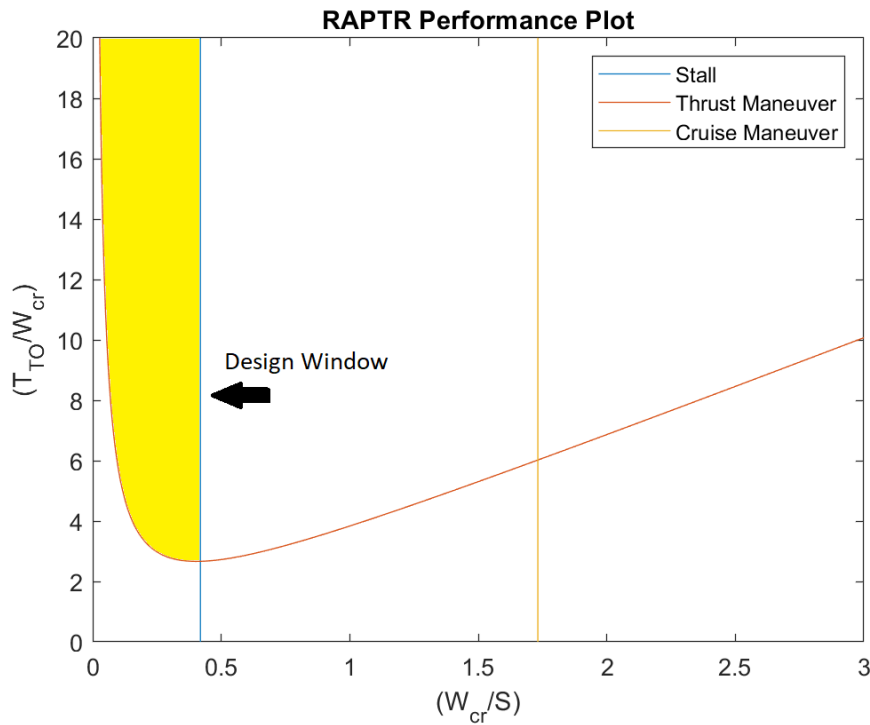
	$C_x$	$C_z$	$C_m$
u	$-4.58 \cdot 10^{-4}$	-0.0062	$-6.38 \cdot 10^{-4}$
$\alpha$	0.1559	-4.0189	-0.4143
$\dot{\alpha}$	0	-1.4944	-5.1164
q	0	-4.9263	-16.866

	$C_y$	$C_l$	$C_n$
$\beta$	-0.7589	-0.1326	0.0248
p	-0.0124	-	0.0045
r	1.9344	0.0045	-0.0178

## Results from Datcom analysis

	$C_x$	$C_z$	$C_m$
u	$-4.58 \cdot 10^{-4}$	-0.0062	$-6.38 \cdot 10^{-4}$
$\alpha$	0.1559	-5.8041	-1.6604
$\dot{\alpha}$	0	-2.3715	-8.0042
q	0	-8.6001	-24.3335

	$C_y$	$C_l$	$C_n$
$\beta$	-0.1112	-0.0019	0.0347
p	-0.0139	-0.5091	-0.018
r	1.9344	0.0386	-0.0296



Stall:

$$\frac{W_{cr}}{S} = \frac{1}{2} \rho V_s^2 C_{L_{max}}$$

Thrust Man.:

$$\frac{T}{W_{cr}} = \frac{q C_{D_o}}{\frac{W_{cr}}{S}} + \frac{n^2}{q \pi A R e} \frac{W_{cr}}{S}$$

Cruise Man.:

$$\frac{W_{cr}}{S} = V \left( \frac{2n}{\rho C_L} \right)^{-\frac{1}{2}}$$

$$n_{cruise} = \sqrt{\left( \frac{V^2 \cos^2 \gamma}{R_{turn} g} \right)^2 + \cos^2 \gamma}$$

$$n_{thrust} = \frac{V_{max}^2}{h_{end}}$$



# Electronics Backup Slides

## Electronics Slides Appendix

1. Electronics Hardware
2. Servo Design Envelope

# Sensor Attitude Determination *(Electronics Assembly Procedure)*

## PCB

- Solder surface mount components to solder pads
- Solder battery leads to input power solder pads
- Solder 5V and 6V output power leads to applicable solder pads

## Pixhawk and Sensors

- Connect GPS and compass module via GPS pins (pre-installed plug)
- Connect telemetry radio via TELEM 1 pins (pre-installed plug)
- Connect buzzer and safety switch via SWITCH and BUZZER pins (pre-installed plugs)
- Connect airspeed sensor via I2C pins (pre-installed plug)
- Connect XR8 sensor to XR8 SBUS pins and Pixhawk RC pins on servo rail (pre-installed plug)
- Connect servo rail power wires (solder or JST SM 2 pin connector)

## Servos

- Plug into appropriate servo rail pins (3-pin PWM JST SM connectors)
  - Rudder connects to pin 4
  - Elevator connects to pin 2

# Sensor Attitude Determination *(Power Consumption and Physical Specifications)*

## Battery (Turnigy Graphene Panther 950mAh)

- 950mAh, 7.4V 2 cell lithium polymer battery
- Capable of continuous discharge of up to 71.25 Amps (1.9 hour life with 750mA current draw)
- Weight of 50g

## Servos (Futaba S3152, 2 used)

- 87 oz-in of torque at 6V and .18 seconds per 60 degrees of rotation
- Idle current of approximately 10mA, operating current of 100-250mA, stall current of approximately 1 amp (all at 6V)
- Weight of 41g each

## Pixhawk

- Operating current draw of approximately 300mA at 5V when battery powered (includes safety switch and LED power consumption)
- Weight of 15.8 grams

## Airspeed/Temperature Sensor

- Measures from 0 to 100 m/s (0 to 223 mph) with temperature correction
- Operating current draw of approximately 25mA at 5V
- Weight of 12g

## GPS/Compass Module

- Operating current draw of approximately 60mA at 5V
- Weight of 32g with case

## FrSky X8R

- Operating current draw of approximately 100mA at 5V
- Weight of 16.6g

## HK Pilot Transceiver

- Operating current draw of 25mA and 100mA at 5V (receiving and transmitting)
- Weight of approximately 20g with antenna

## Totals

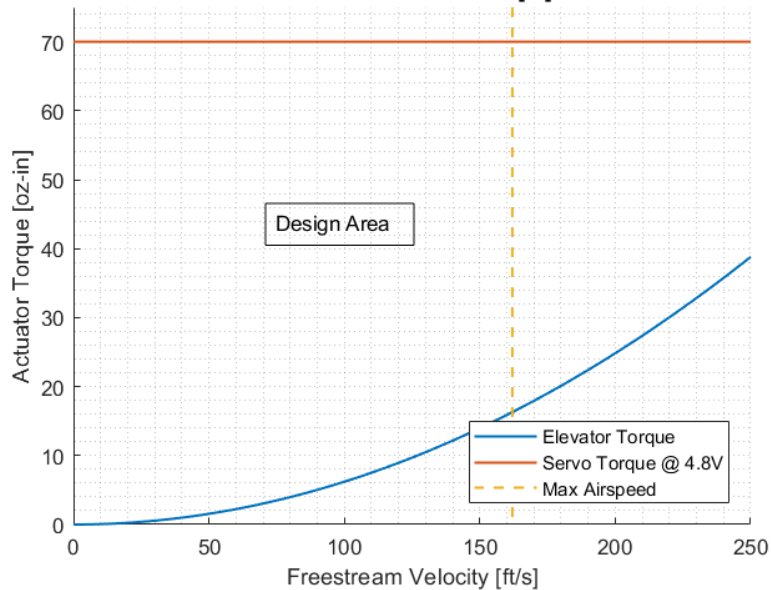
- Max current draw of approximately 2,585mA with typical operating current draw of approximately 725mA, idle current draw of approximately 560mA
- Approximate operating (flying) battery life of approximately 1.3 hours, idle battery life of approximately 1.7 hours
- Weight of 219.9g without transceiver antenna, approximately 230g with antenna

Sensor Attitude Determination  
(DR 4.2.1)

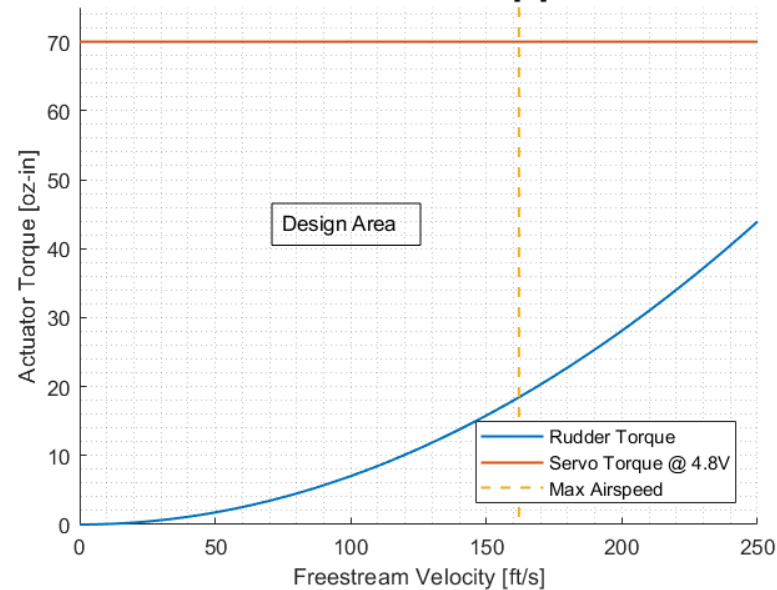
Capable Vehicle Control  
(DR 1.1.2)

# Servo Design Envelope

**Elevator Design Area**  
Elevator Size: 16.5x1.5 [in]



**Rudder Design Area**  
Rudder Size: 9.5x1.6 [in]

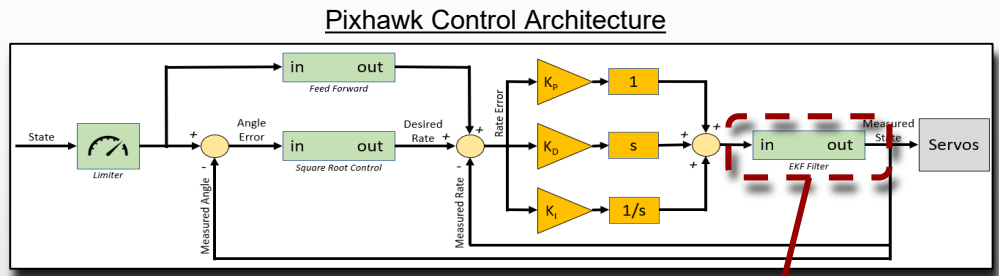


# Controls Backup Slides

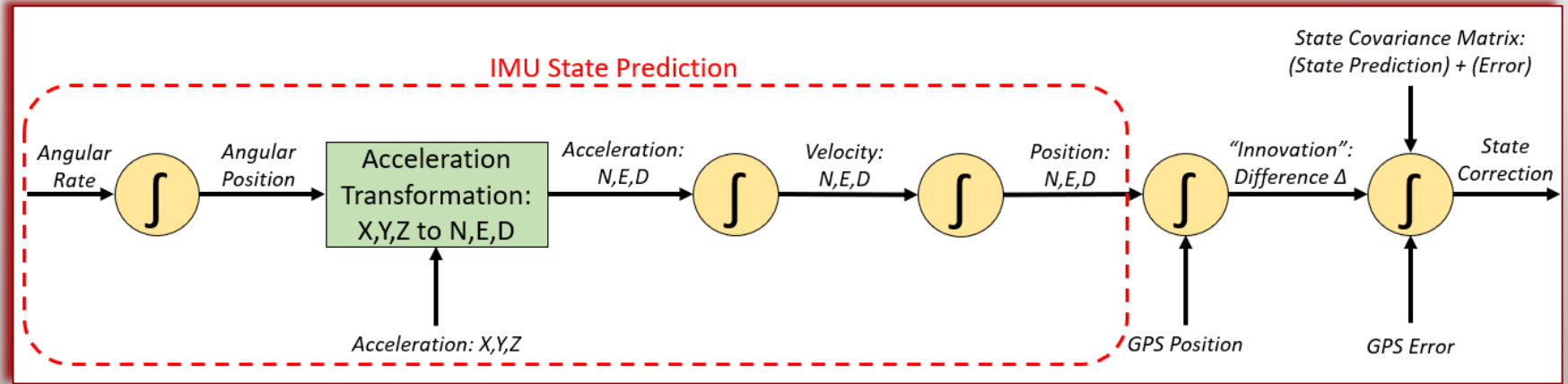
## Controls Slides Appendix

- EKF FBD
- Longitudinal and Lateral dynamics
- Gains

# Vehicle Control



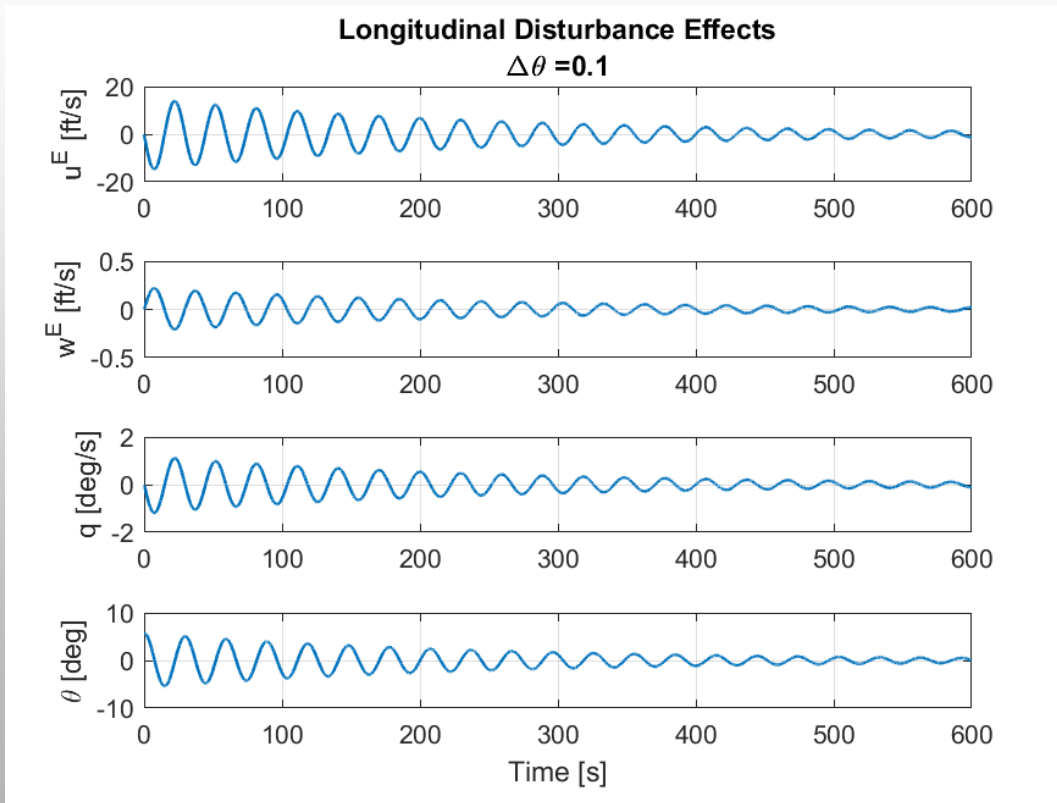
## Extended Kalman Filter Architecture



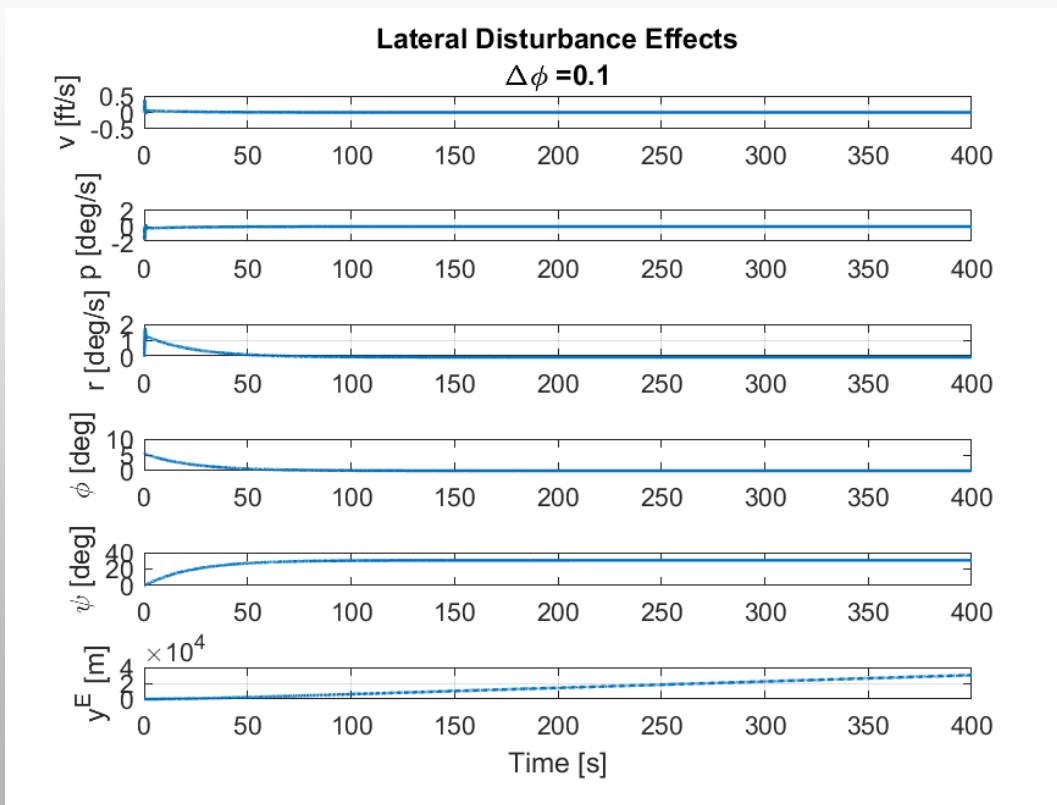
Sensor Attitude Determination (DR 4.2.1)

Capable Vehicle Control (DR 1.1.2)

# Longitudinal Open-Loop Dynamics

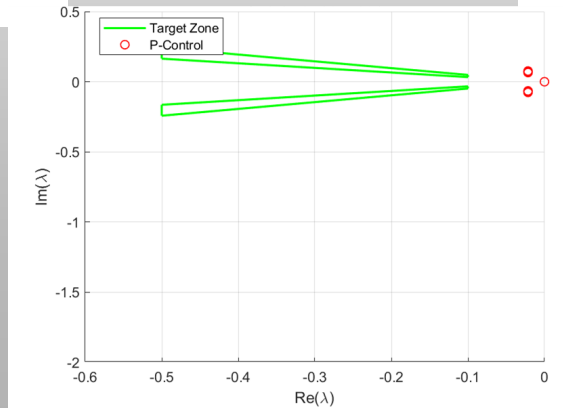
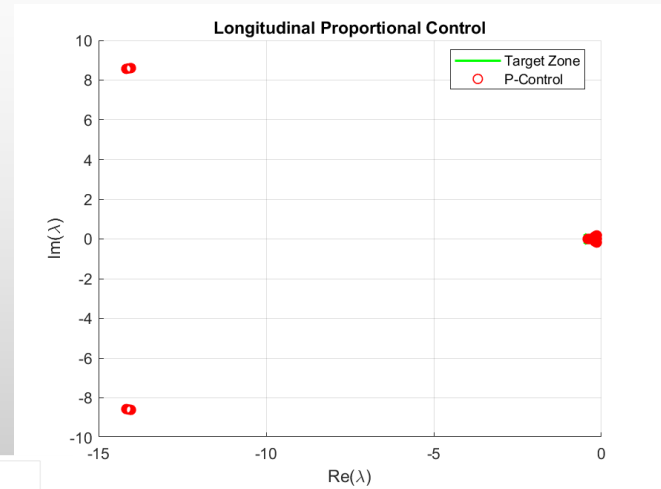
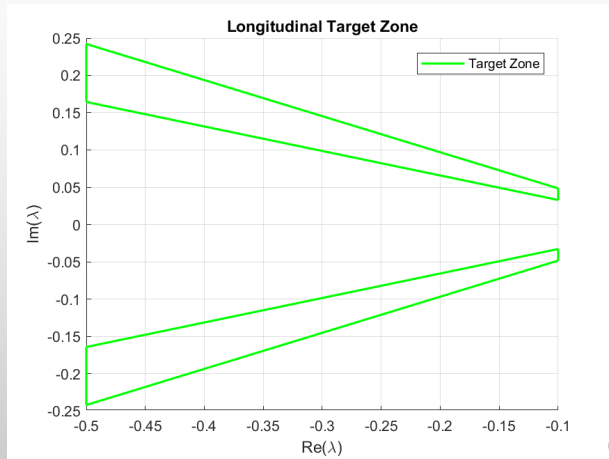


# Lateral Open-Loop Dynamics

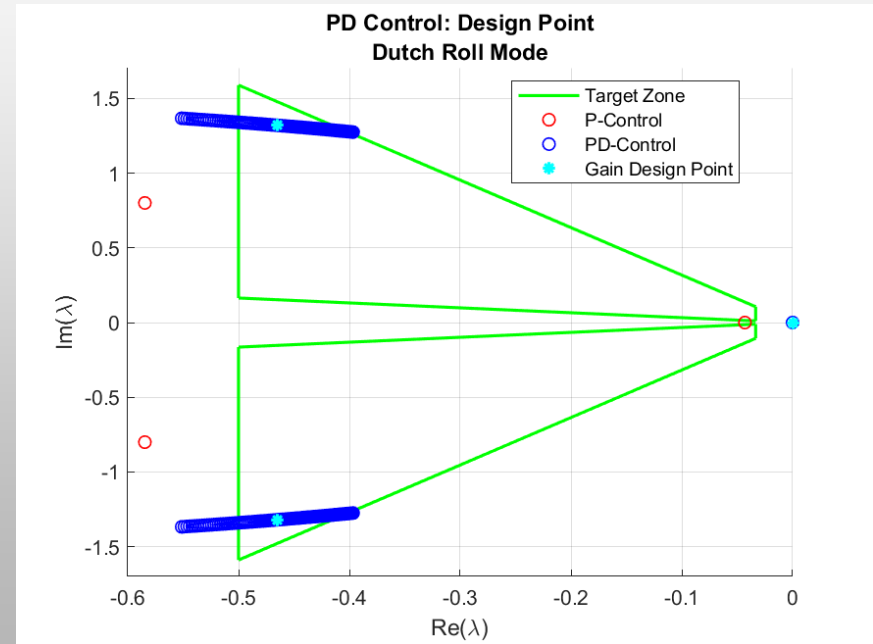
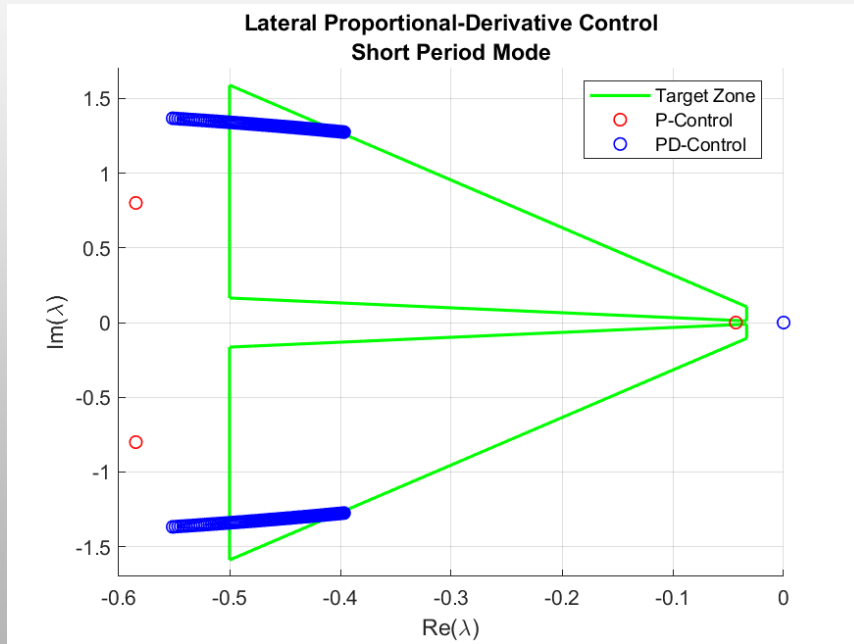




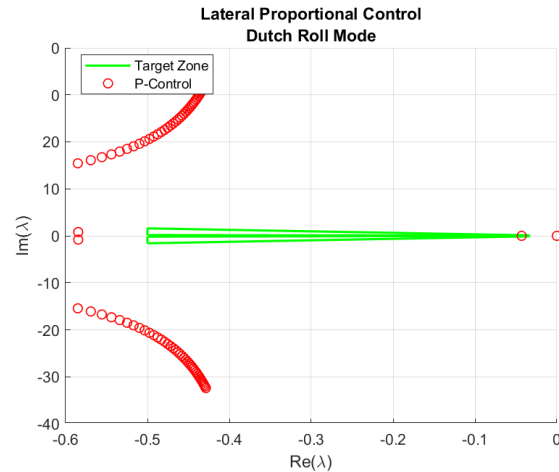
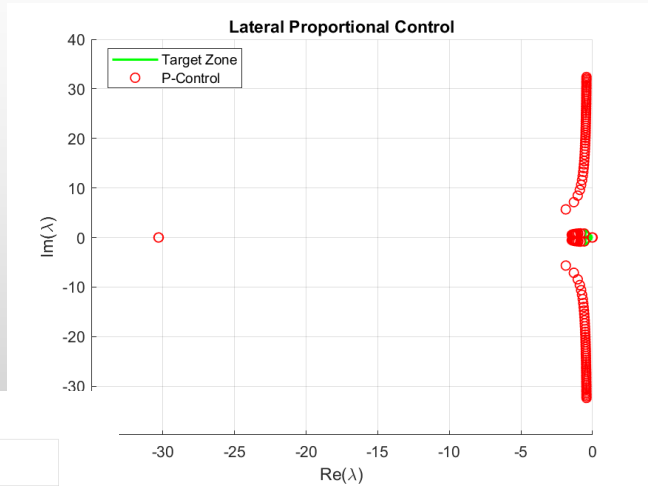
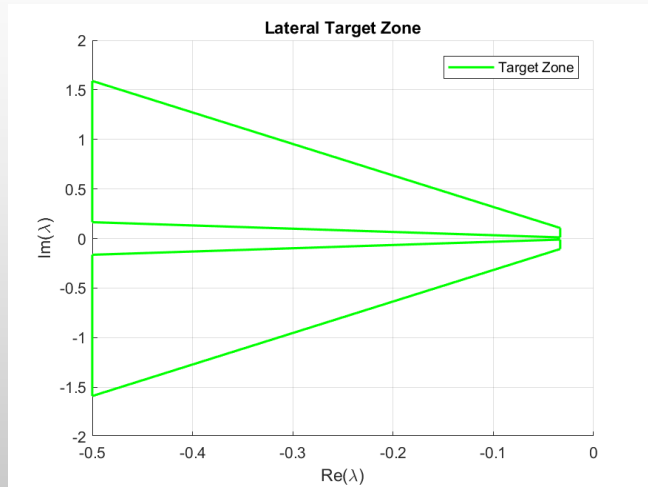
# Longitudinal Gains



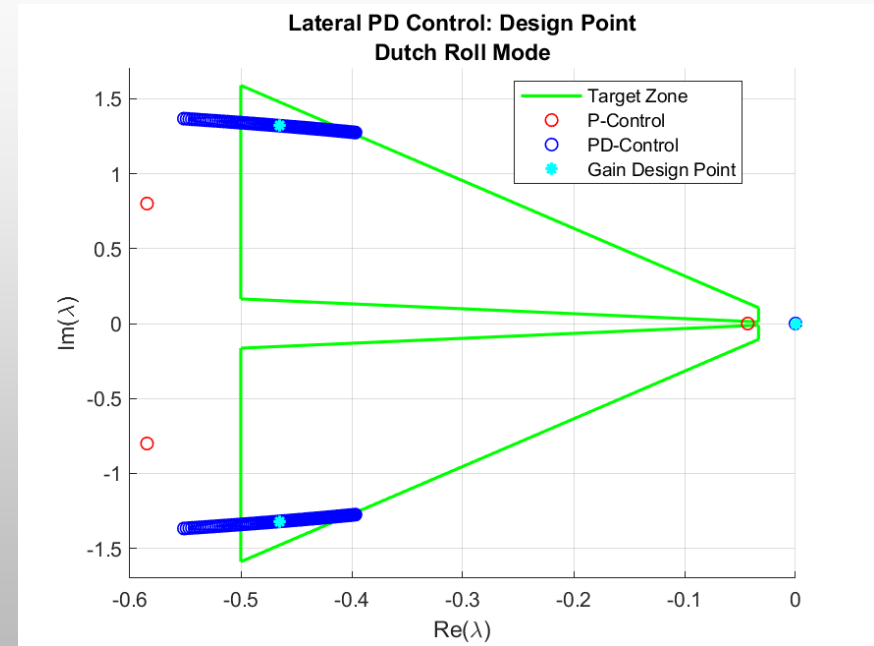
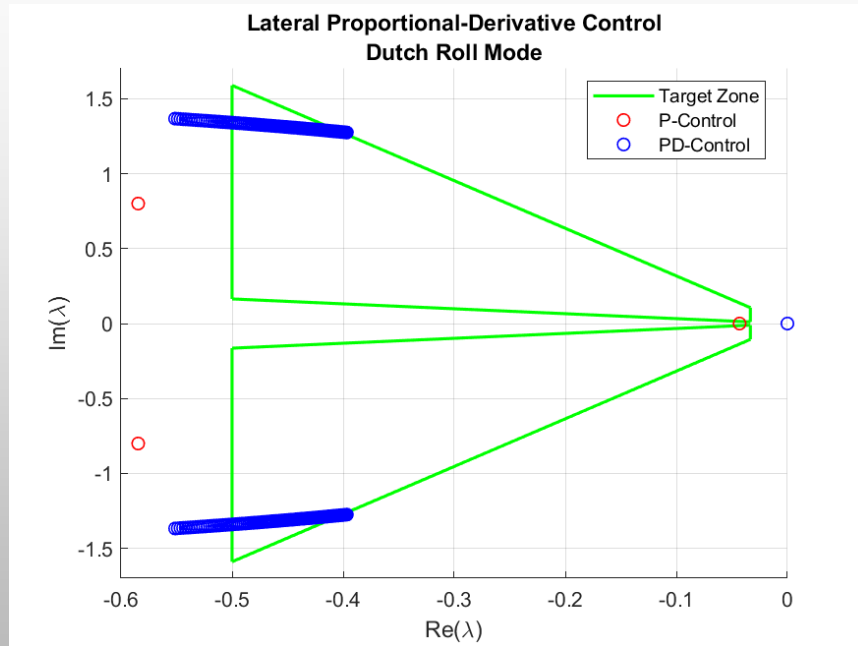
# Longitudinal Gains



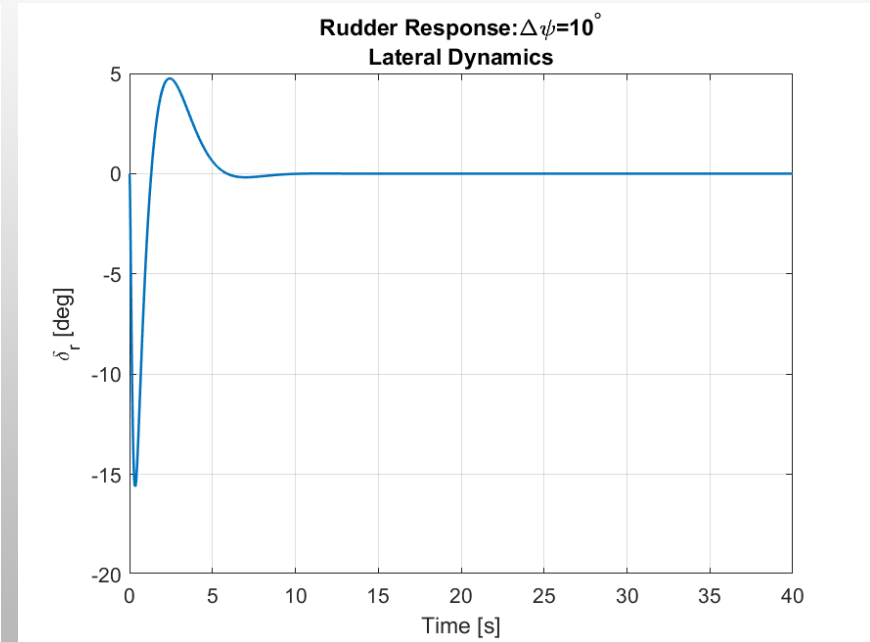
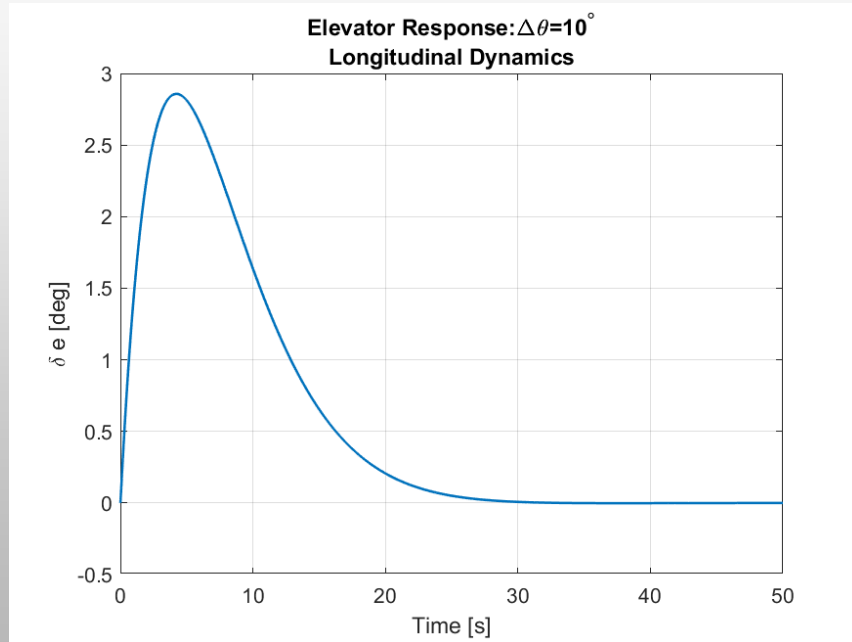
# Lateral Gains



# Lateral Gains



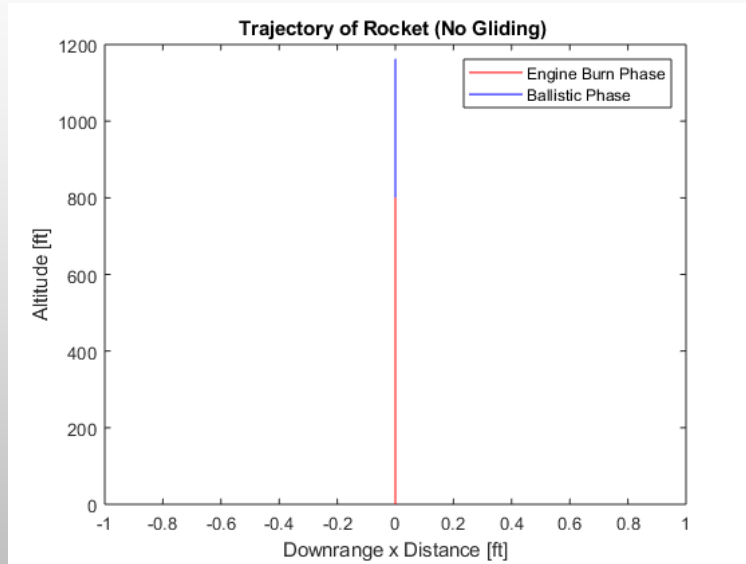
# Control Surface Deflection



# Propulsion Backup Slides

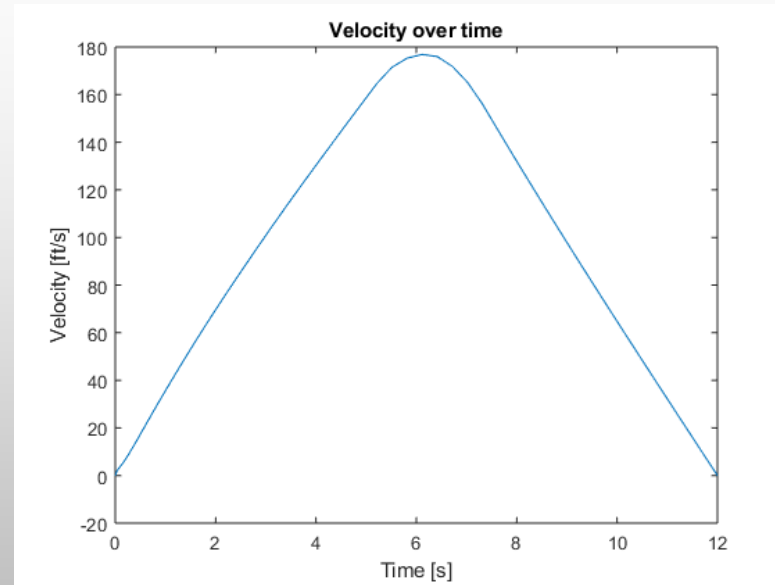
1. MATLAB model - Trajectory/Velocity
2. MATLAB model - Thrust uncertainty
3. MATLAB model - Thrust uncertainty
4. OpenRocket Governing Equations
5. Parachute Choice
6. Motor Recovery
7. Launch Controller
8. Igniter
9. Plume Characteristics
10. Plume Characteristics
11. Engine Assembly
12. Thermal Risk Mitigation
13. Baffle
14. Launch Pad
15. Reducing Velocity

# MATLAB Model - Trajectory/Velocity



Max Altitude: 1163 ft

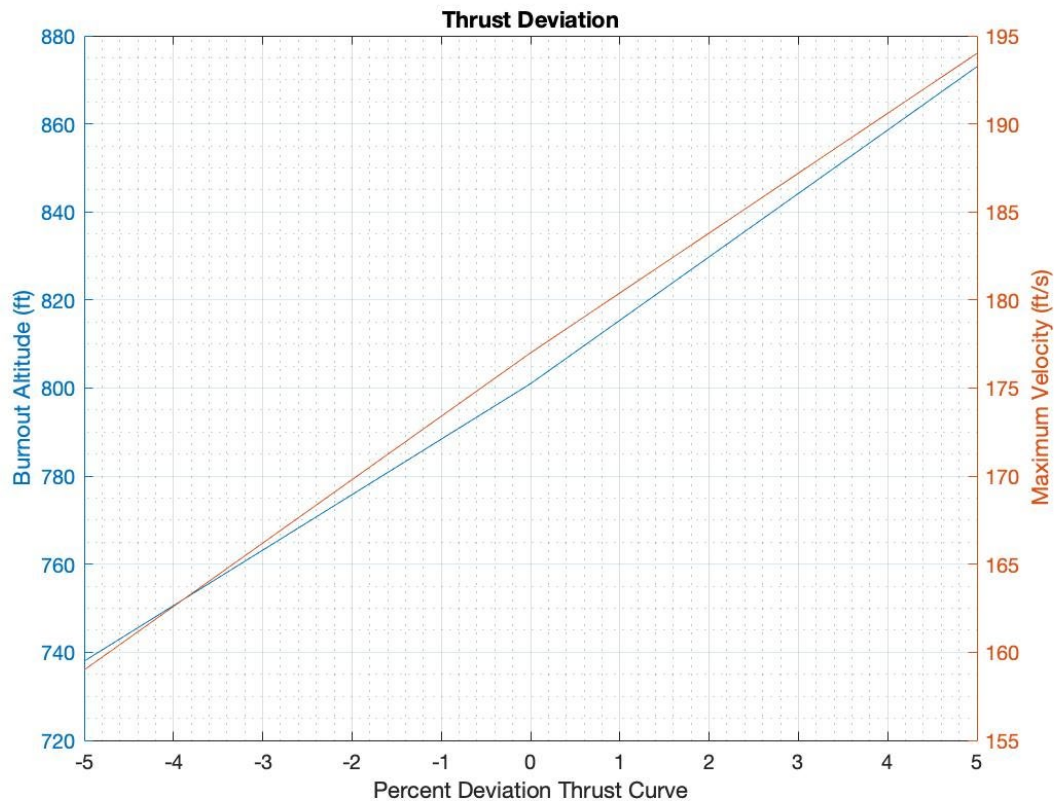
Burnout Altitude: 801 ft



Max Speed: 177 ft/s

Time to Apogee : 11.9s

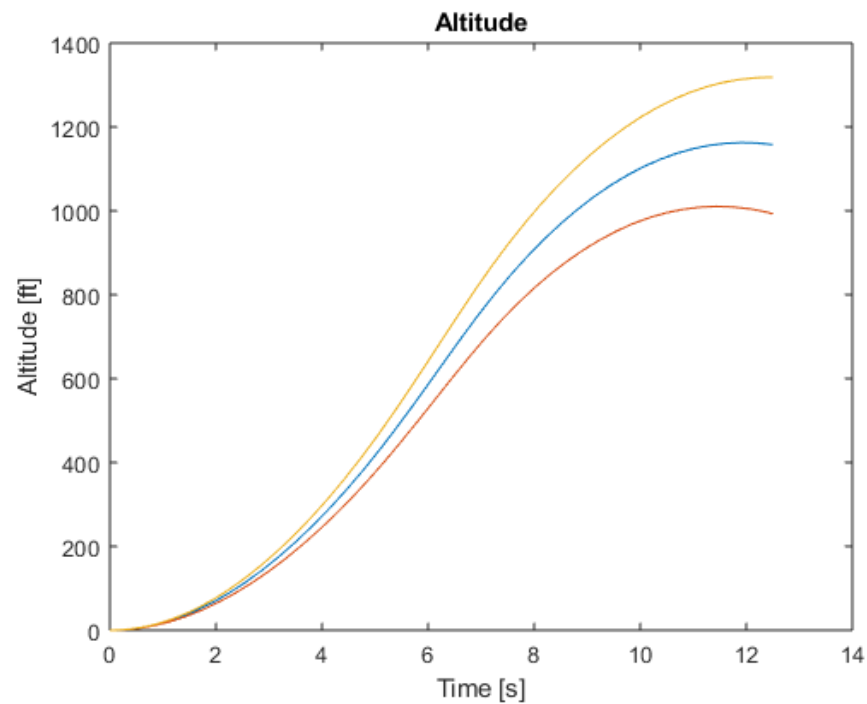
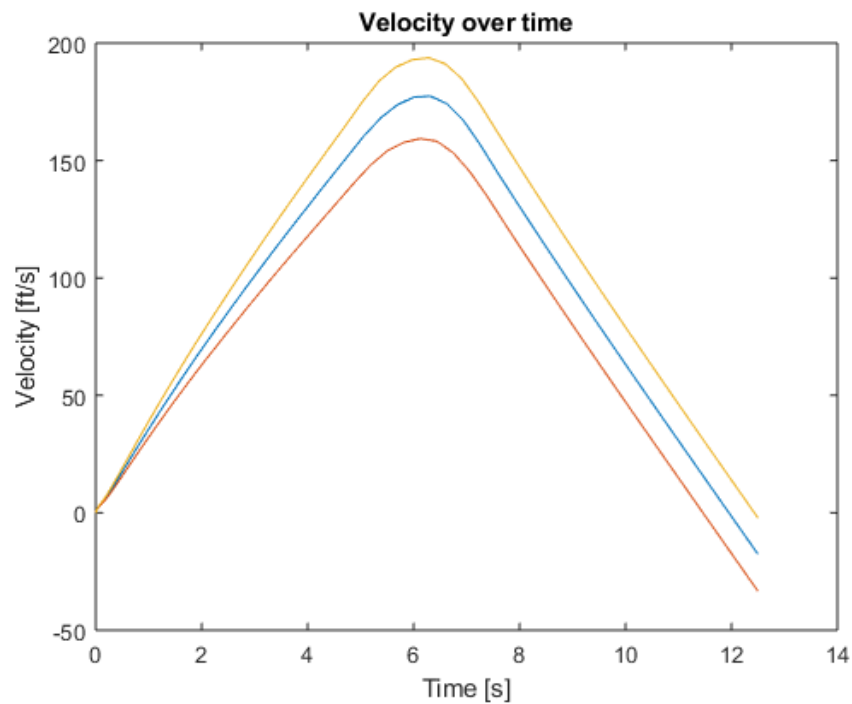
# MATLAB Model - Thrust Uncertainty



Deviation	Burnout Altitude [ft]	Max Speed [ft/s]
0%	801	177
-5%	738	159
+5%	873	194



# MATLAB Model - Thrust Uncertainty



# OpenRocket Equations - Aerodynamics

$$C_D = \frac{D}{\frac{1}{2}\rho v_0^2 A_{\text{ref}}}$$

$$C_l = \frac{l}{\frac{1}{2}\rho v_0^2 A_{\text{ref}} d}$$

$$C_m = \frac{m}{\frac{1}{2}\rho v_0^2 A_{\text{ref}} d}$$

$$C_f = \frac{D_{\text{friction}}}{\frac{1}{2}\rho v_0^2 A_{\text{wet}}}$$

$$C_N = \frac{N}{\frac{1}{2}\rho v_0^2 A_{\text{ref}}}$$

$$X = \frac{C_m}{C_N} d$$

$$C_{f_c} = \frac{C_f}{(1 + 0.15 M^2)^{0.58}}$$

Wind Turbulence Equation:

$$\bar{c} = \frac{1}{A_{\text{fin}}} \int_0^s c^2(y) dy$$

$$y_{\text{MAC}} = \frac{1}{A_{\text{fin}}} \int_0^s y c(y) dy$$

$$x_{\text{MAC,LE}} = \frac{1}{A_{\text{fin}}} \int_0^s x_{\text{LE}}(y) c(y) dy$$

$$\text{Kaimal: } \frac{S_u(f)}{\sigma_u^2} = \frac{4L_{1u}/U}{(1 + 6fL_{1u}/U)^{5/3}}$$

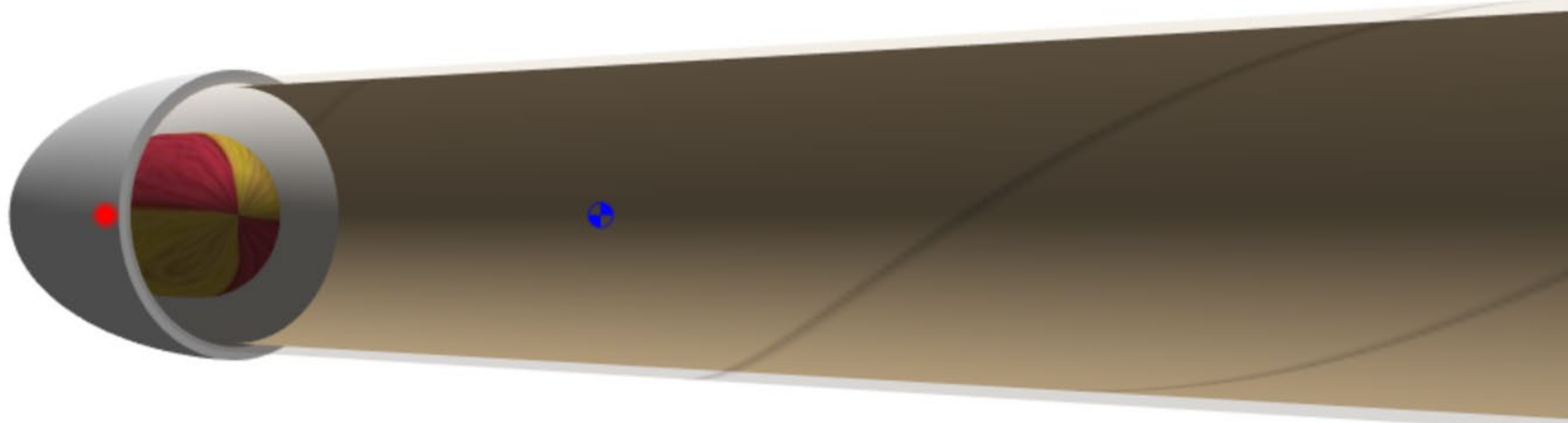
$$\text{von Kármán: } \frac{S_u(f)}{\sigma_u^2} = \frac{4L_{2u}/U}{(1 + 70.8(fL_{2u}/U)^2)^{5/6}}$$

# Parachute Choice

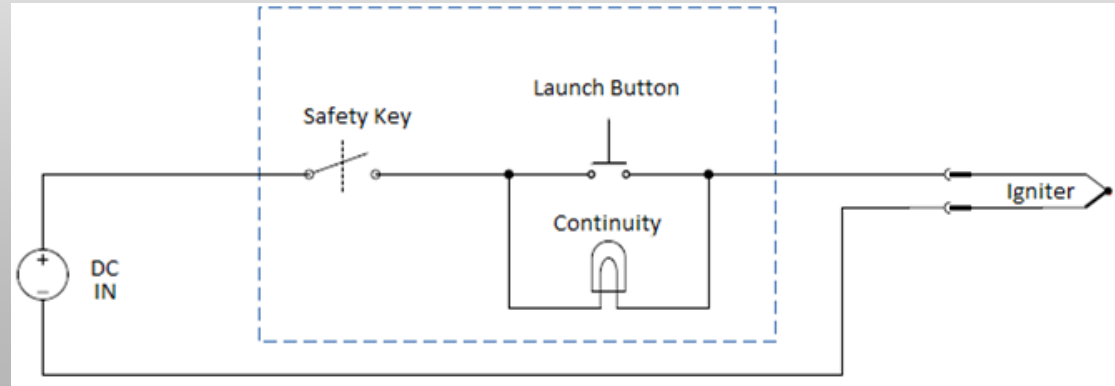
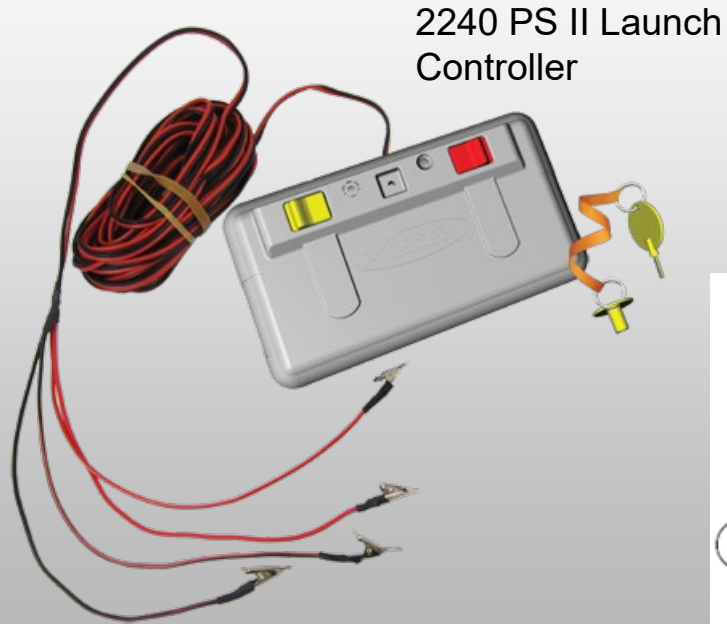


$$D = \sqrt{\frac{8mg}{\pi\rho C_D V_g^2}} = \sqrt{\frac{8 \cdot 0.2521[kg] \cdot 9.81[m/s^2]}{\pi \cdot 0.975[kg/m^3] \cdot 1.5 \cdot (5[m/s])^2}} = 0.415[m] = 41.5[cm] = 16.34[in]$$

# Motor Recovery

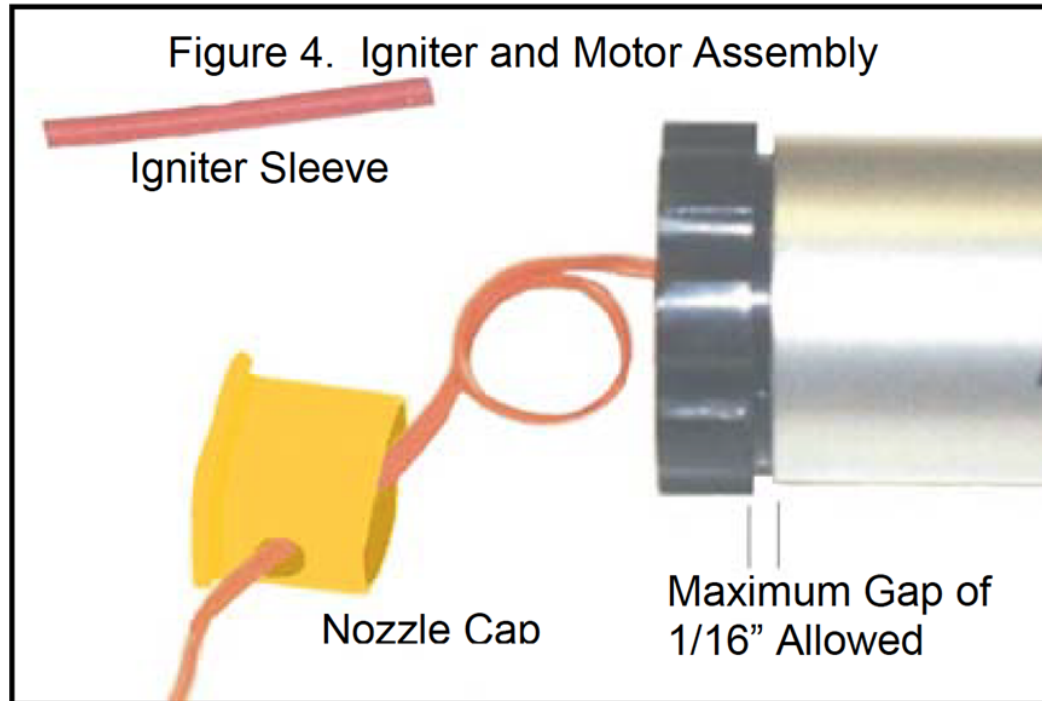


# Launch Controllers



# Igniter

Figure 4. Igniter and Motor Assembly



## Igniter specifications\*:

Bridgewire resistance:  
1.2 – 1.8 $\Omega$

Rated all-fire current:  
1.2 Amps for 10 milliseconds

Typical response:  
2.3ms @ 1.2 Amps

(\*) These are manufacturer's specs.  
CTI assumes no responsibility for  
their use or misinterpretation

# Exhaust Plume Regions

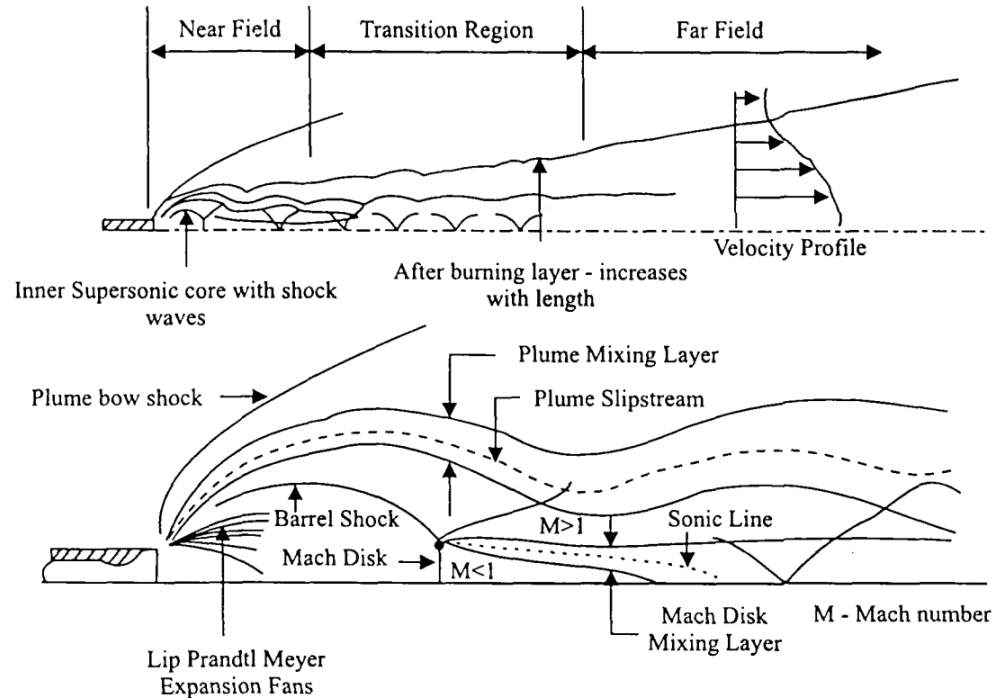


Fig. 3.1.2 Description of a Typical Supersonic Plume

# Rocket Engine Integration

## Grain Integration



## Motor Integration

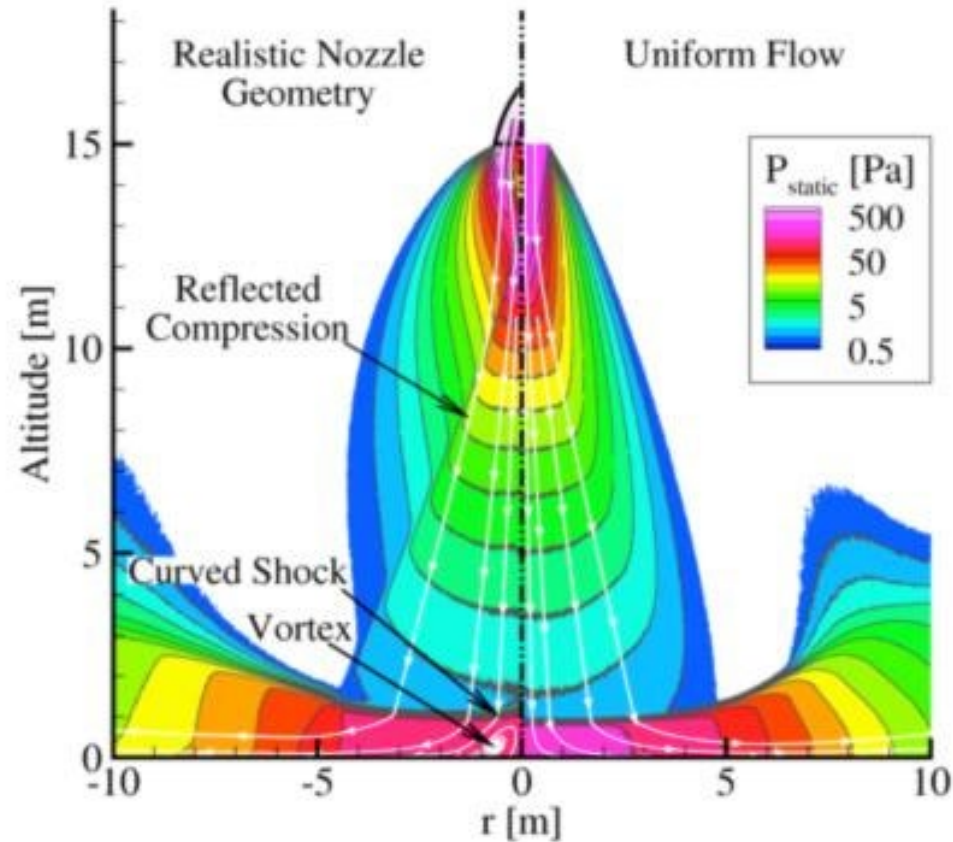


## Fully Integrated Motor and Casing



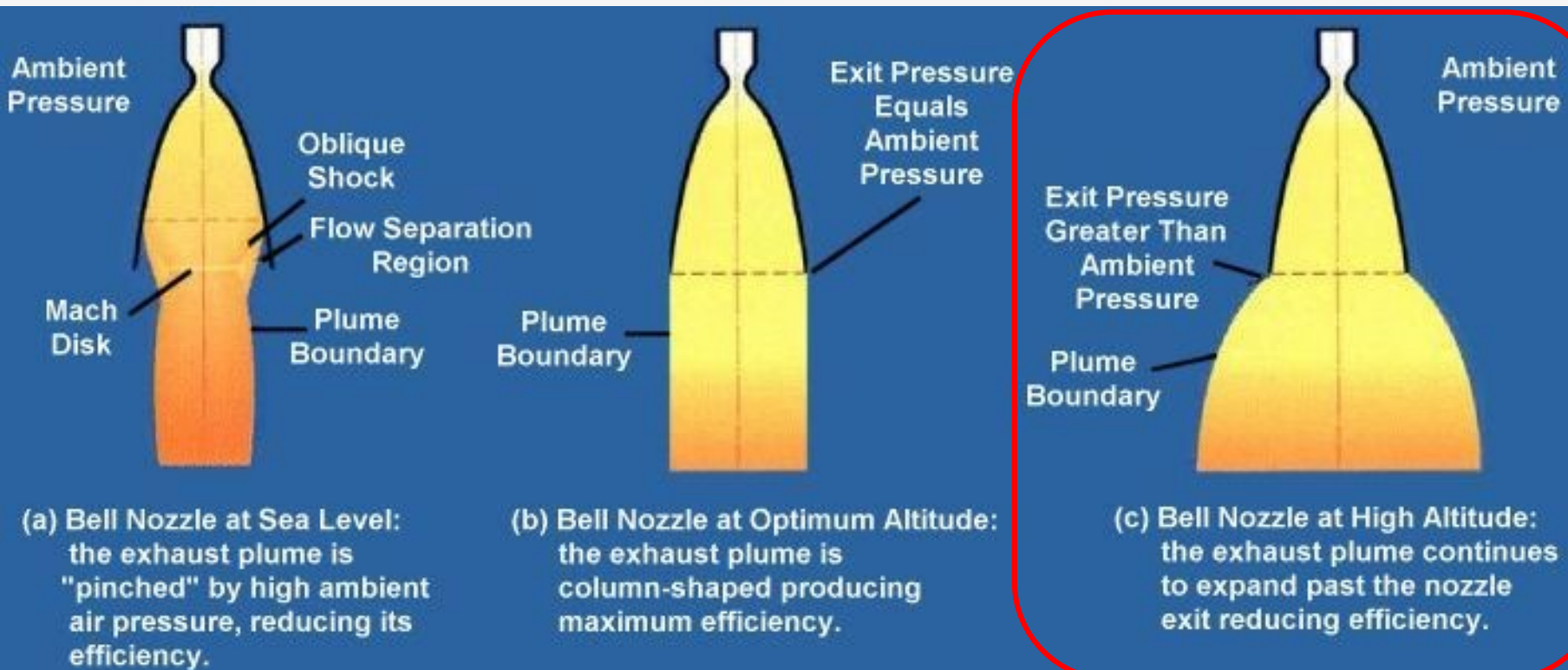


# Nozzle Flow - Ideal vs. Realistic

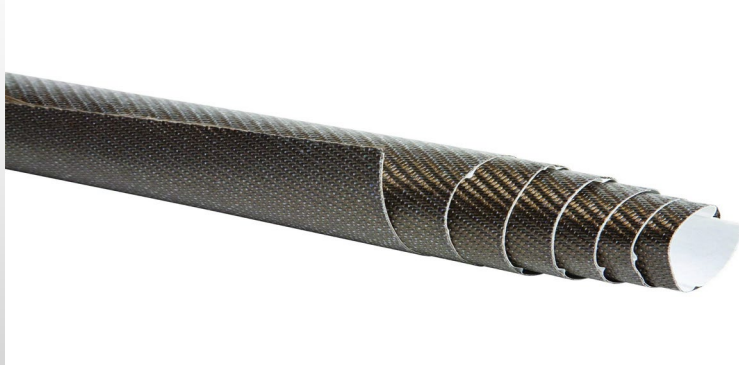


# Exhaust Plume Expansion

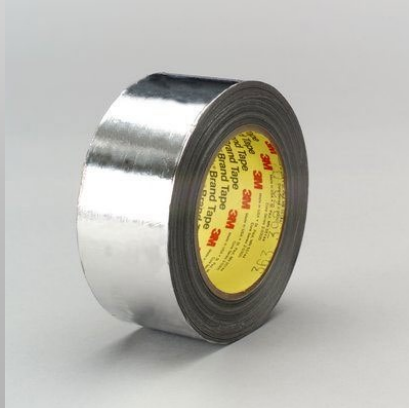
- Underexpanded nozzle at altitude leads to expanded exhaust plume



# Thermal Risk Mitigation



- **Worst Case: Lava Heat Shield**
  - Made from crushed volcanic rock
  - Shields 80% radiant heat
  - Direct temperatures up to ~1400K
  - ~\$130 for 36"x48" sheet



- **Best Case: Aluminum Tape**
  - Aluminum foil with glass cloth
  - Performs consistently up to ~600K
  - \$23.74 for 1/2"x 5 yd

# What is a Baffle?



The ejection baffle eliminates the requirement for recovery wadding. It is used to protect the parachute from the ejection charge.

# Launchpad and Launch Lug

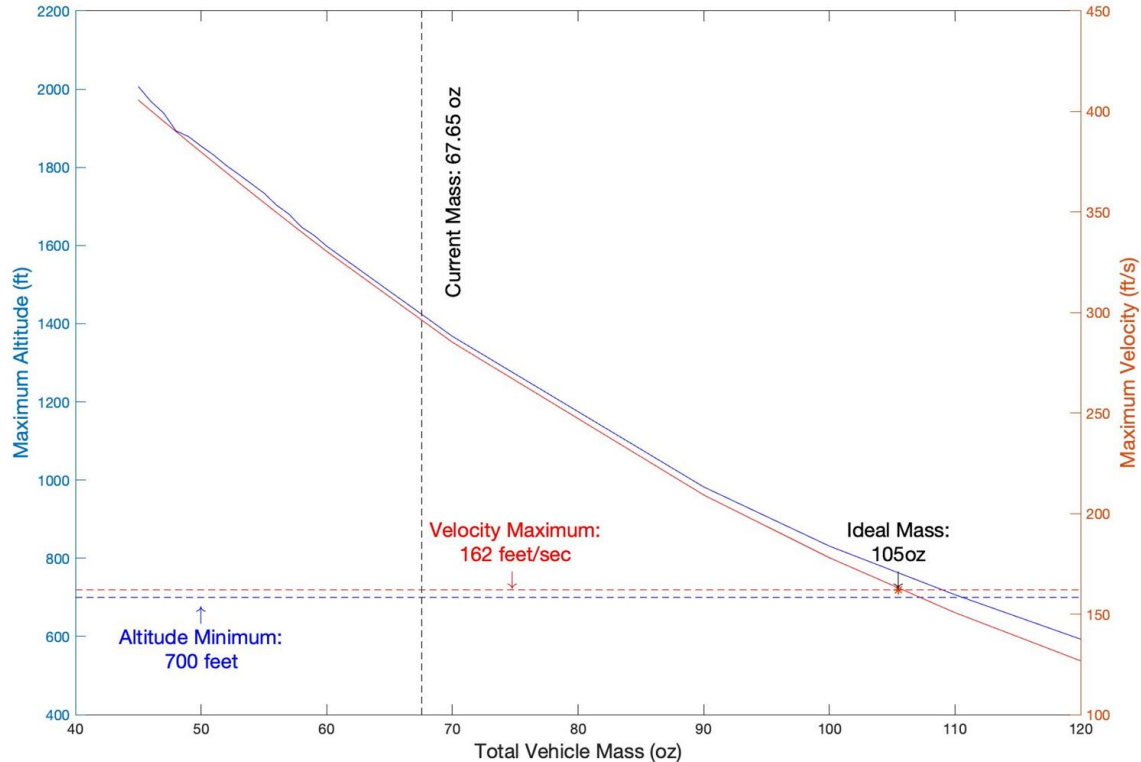
**Launchpad** - Knight Manufacturing, FLP-48

**Launch Rail** - Standard 1010 Aluminum

**Launch Lug** - Linear, compatible with 1010 rail



# Reducing Velocity



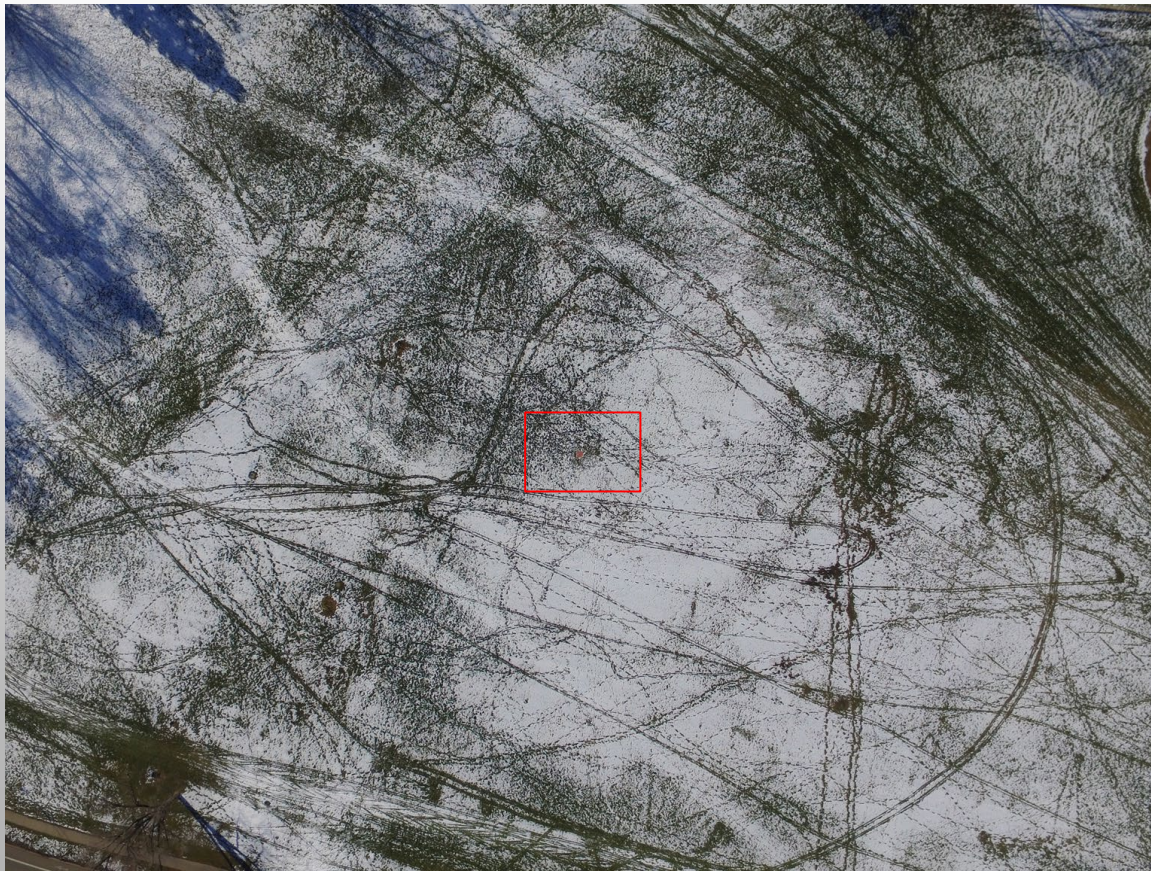
# Software Backup

# Preliminary Testing Targets





## Example Image from Drone:



**Same target pixel size compared to mission profile**

# Pixel to World Transformation

## Problem to solve:

$$\tilde{P}\tilde{p}_w = x_s$$

$$x_s = \begin{bmatrix} u \\ v \\ 1 \\ R(\text{range}) \end{bmatrix}$$

$$\tilde{p}_w = \begin{bmatrix} N(\text{north}) \\ E(\text{east}) \\ D(\text{down}) \\ 1 \end{bmatrix}$$

$$P = K(R|t) \quad \tilde{P} = \begin{pmatrix} \mathbf{K} & \mathbf{0} \\ \mathbf{0}^T & 1 \end{pmatrix} \begin{pmatrix} \mathbf{R} & \mathbf{t} \\ \mathbf{0}^T & 1 \end{pmatrix}$$

$K \equiv$  Camera Matrix

$R \equiv$  world to camera rotation

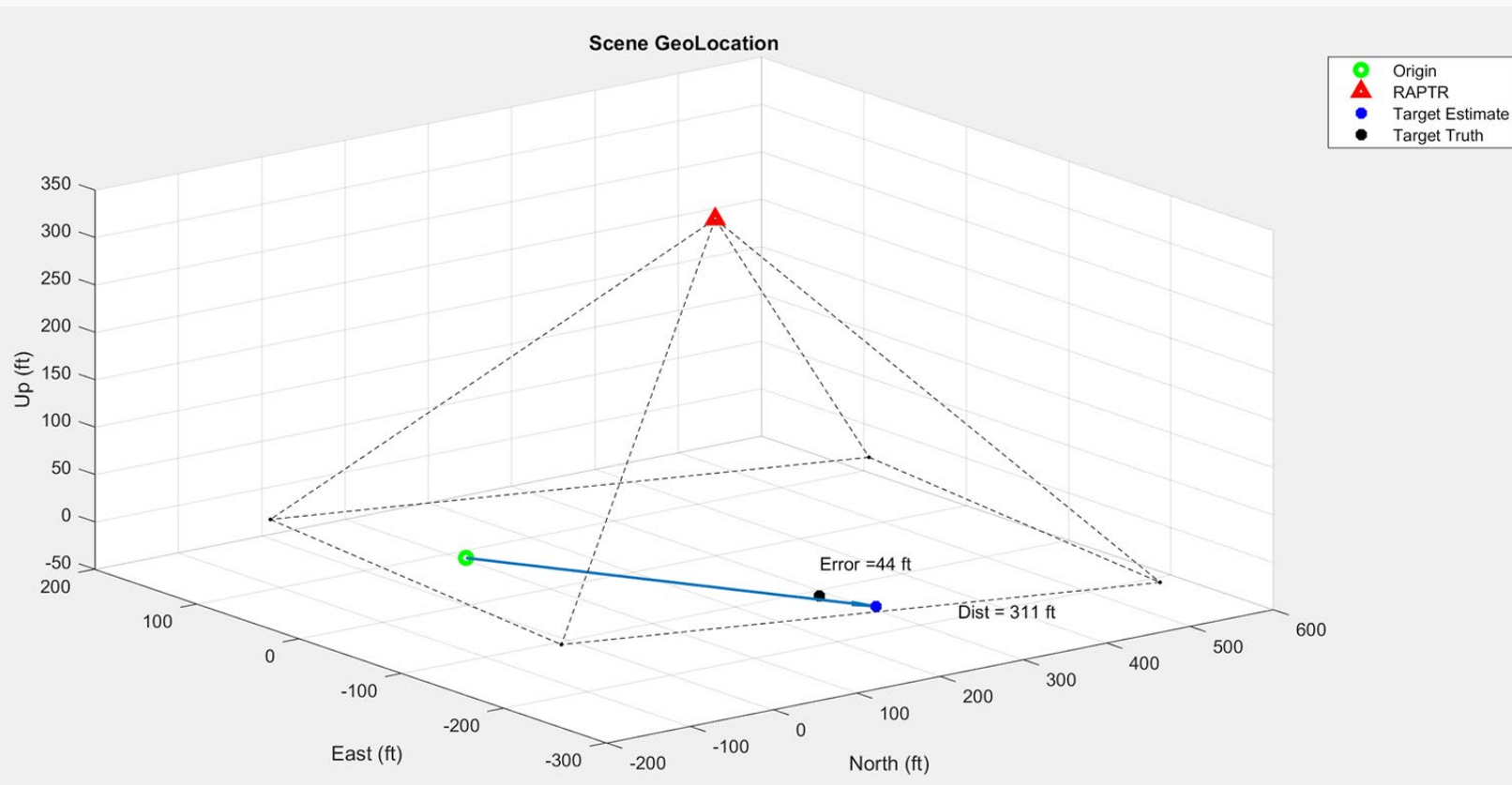
$t \equiv$  world to camera translation

$$K = \begin{bmatrix} f & s & C_x \\ 0 & af & C_y \\ 0 & 0 & 1 \end{bmatrix}$$

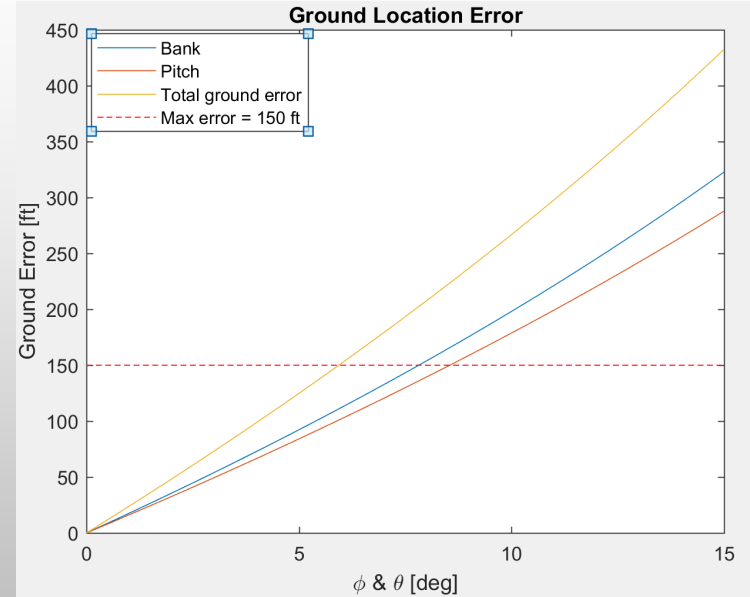
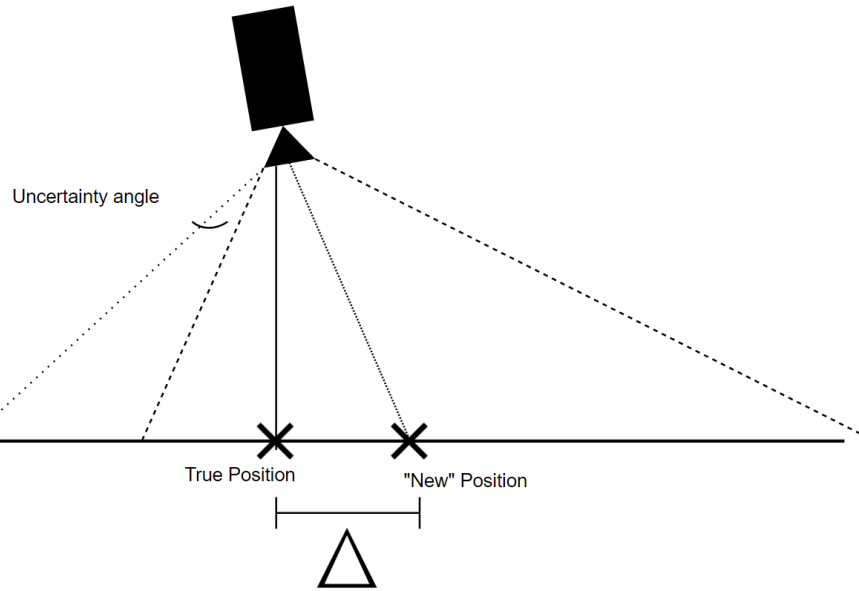
$$R = R_1(\phi)R_2(\theta)R_3(\psi)$$

**Vehicle Roll, pitch, yaw**

# Geolocation Compared to Truth:



# Attitude Uncertainty for Geo-Location:



$$\Delta = h[L\tan(\phi + \alpha + F/2) + (1 - L)\tan(\phi - \alpha - F/2) + (1 - 2L)\tan(F/2 + \alpha)]$$

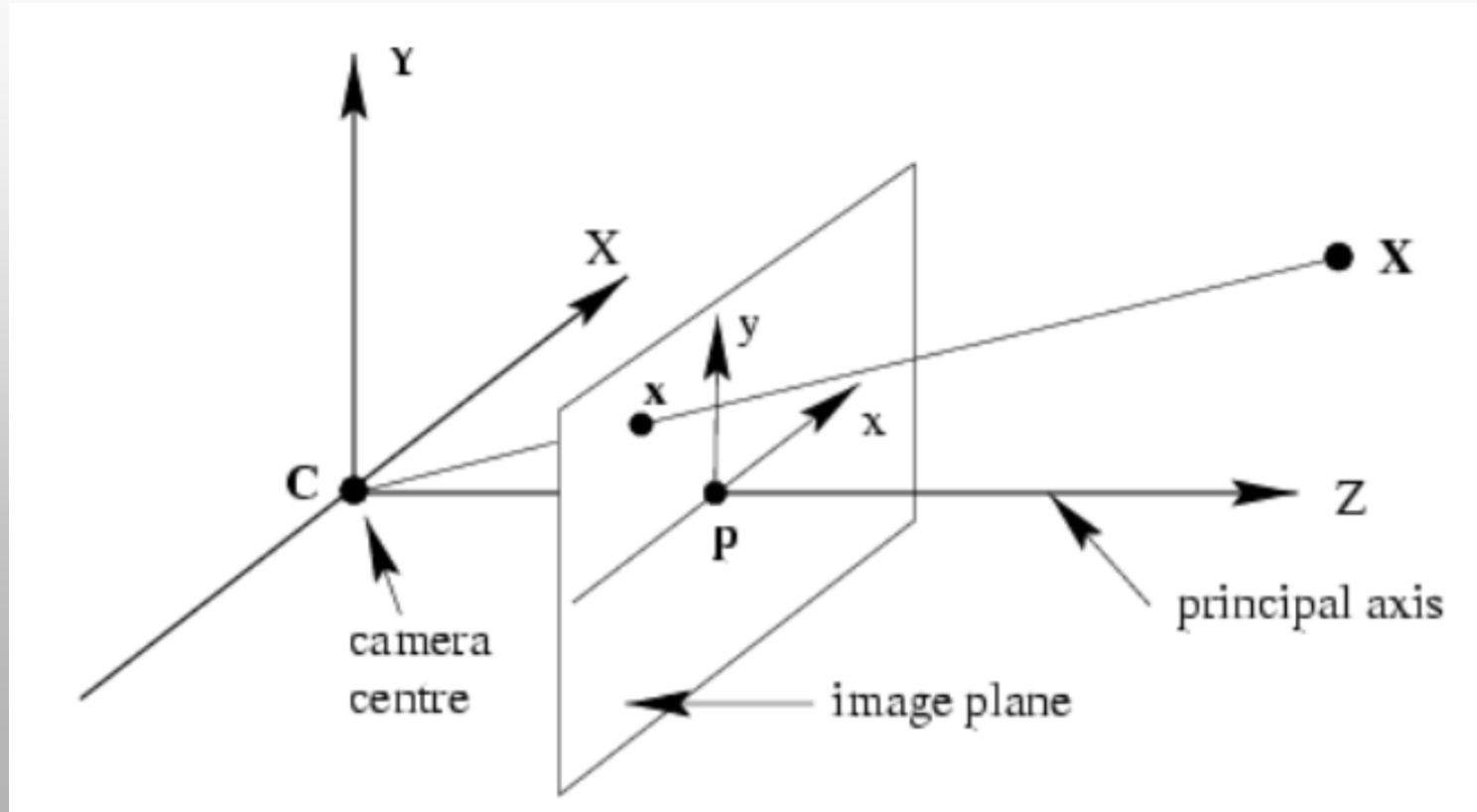
$$\Delta \equiv \text{Ground Distance [ft]}$$

$$\phi \equiv \text{Bank Uncertainty [deg]}$$

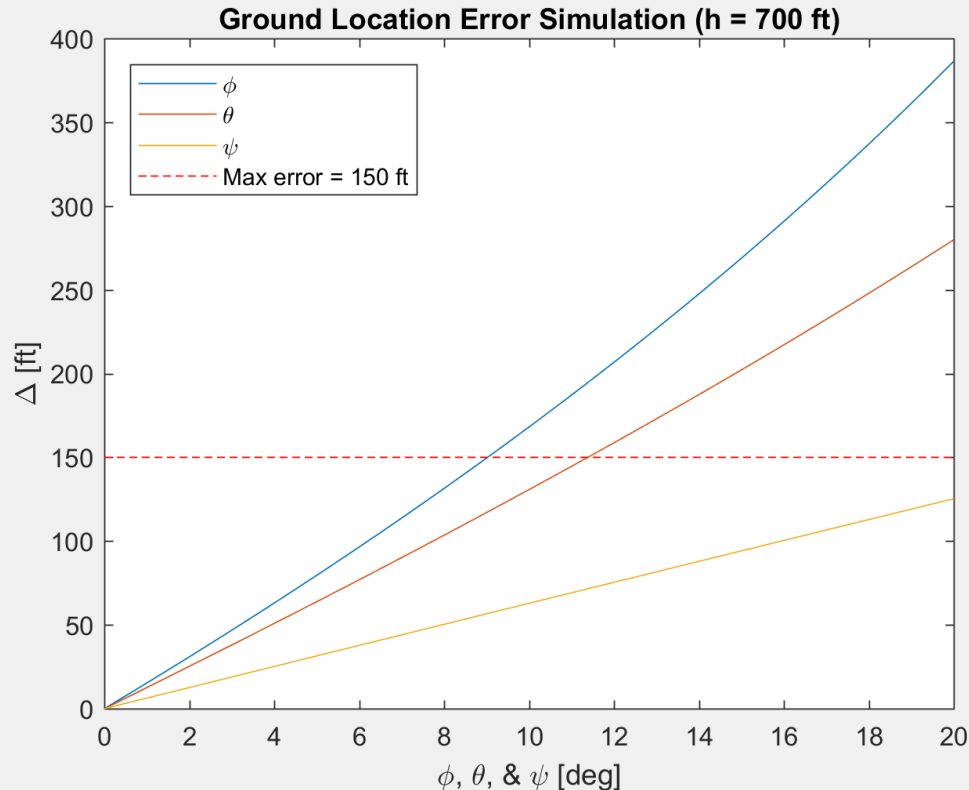
$$\alpha \equiv \text{True Bank Angle [deg]}$$

$$L \equiv \text{Target Location in image (left = 0, right = 1)}$$

# Pixel Mapping Diagram



# Attitude Error with Payload & Algorithm Simulation



- Max pitch, roll uncertainty of 8-10 degrees
- Attitude uncertainty much less than max allowable value
- EE Payload specs compatible with requirements

# Structures Backup

# Structural Requirements

Derived Requirements	Description
DR 1.4	The vehicle shall withstand the forces of the launch and glide phases.

A Matlab model of shear force and bending moment along the wing.

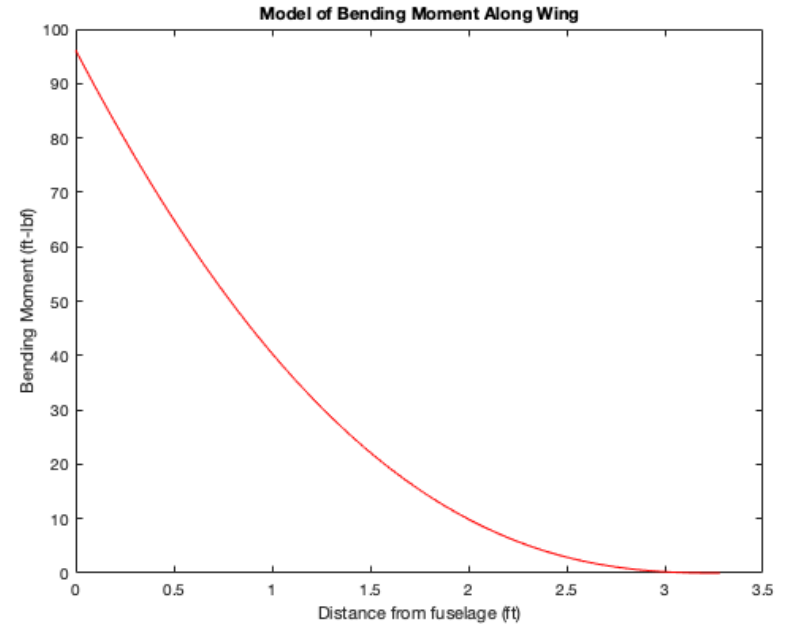
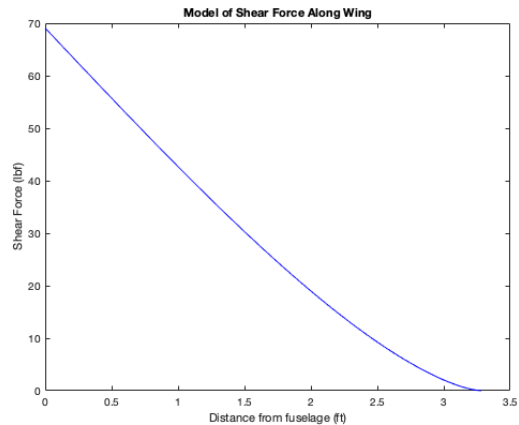
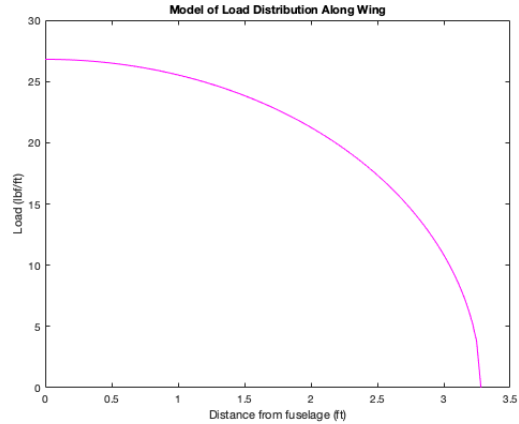
Flexure Formula for 0.25" diameter rod → slight climb  $\sigma_{\max} = 12,457$  psi → worst case  $\sigma_{\max} = 376,232$  psi

Material	$\sigma_y$ [psi]	FOS (slight climb)	FOS (worst case)
Balsa	2,828	0.276	0.007
Al-6061	40,000	3.916	0.106
Steel	53,700	5.257	0.142
Carbon Fiber	82,762	8.102	0.219



# Structural Requirements

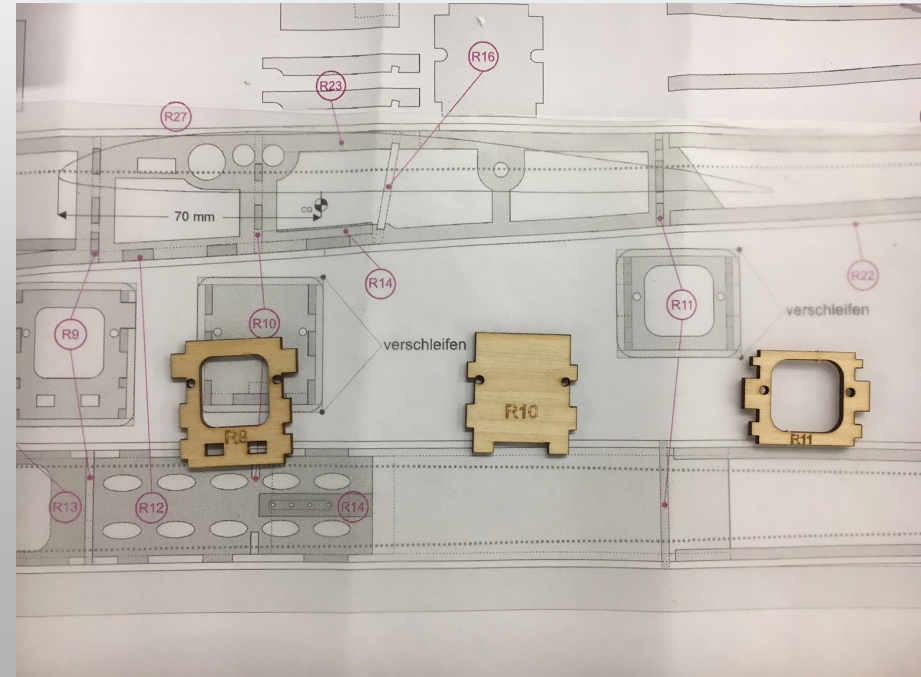
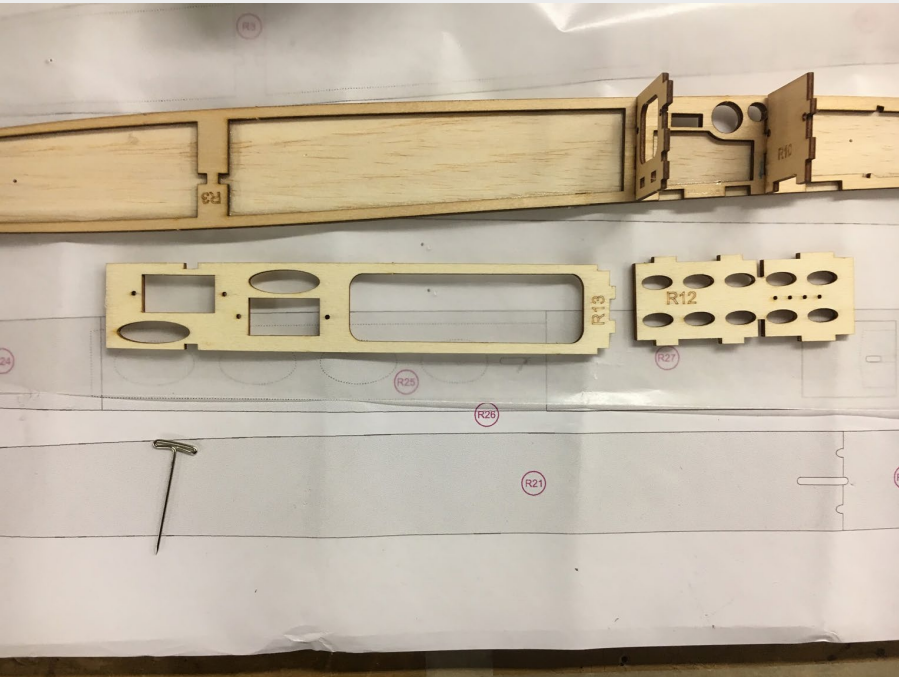
Worst Case



Structural Integrity  
(DR 1.4) ✓

# Fuselage Modification

- Need to widen fuselage from 1.5" to approximately 2.5".
- Bulkheads will be re-made or modified to accommodate the additional width



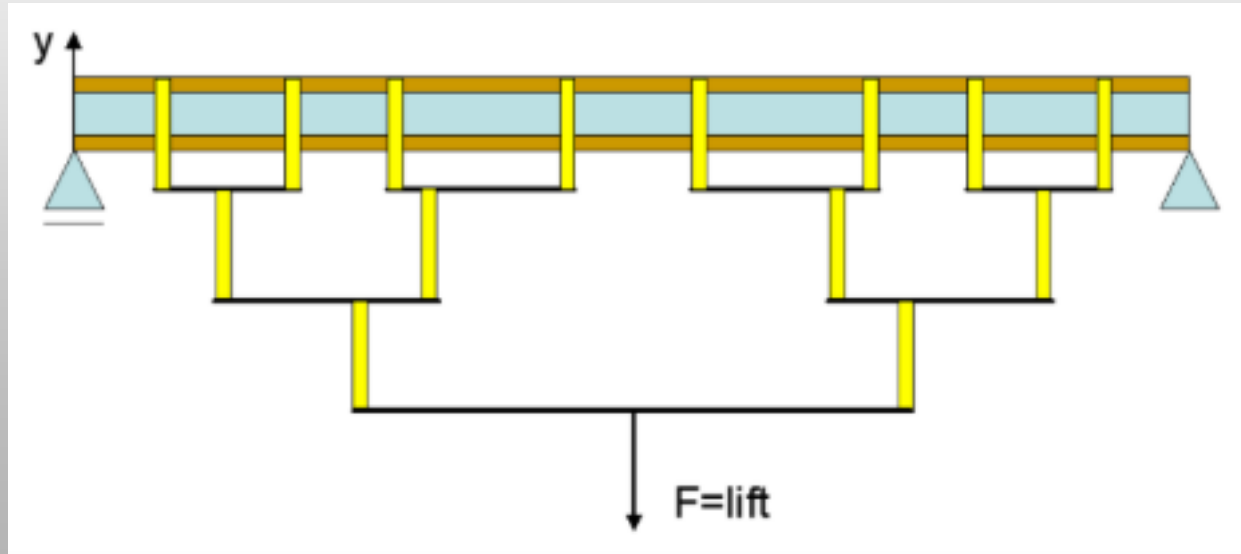
# Fuselage Modification

- Top covering will also be modified to fit the new fuselage



# Wing Loading Test

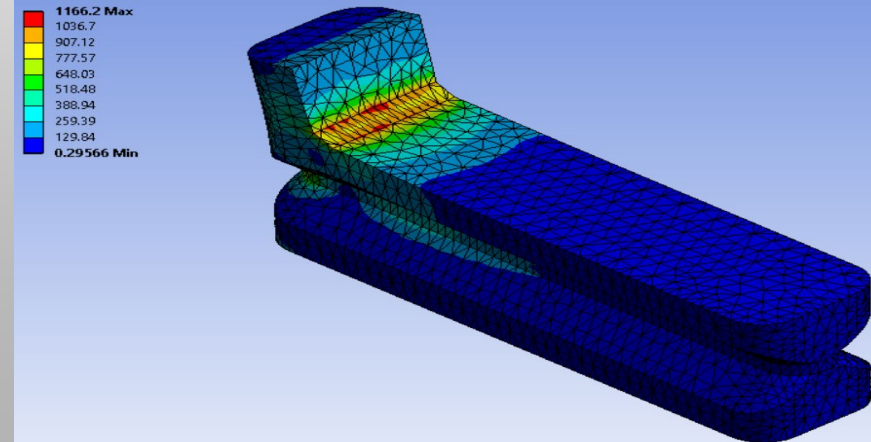
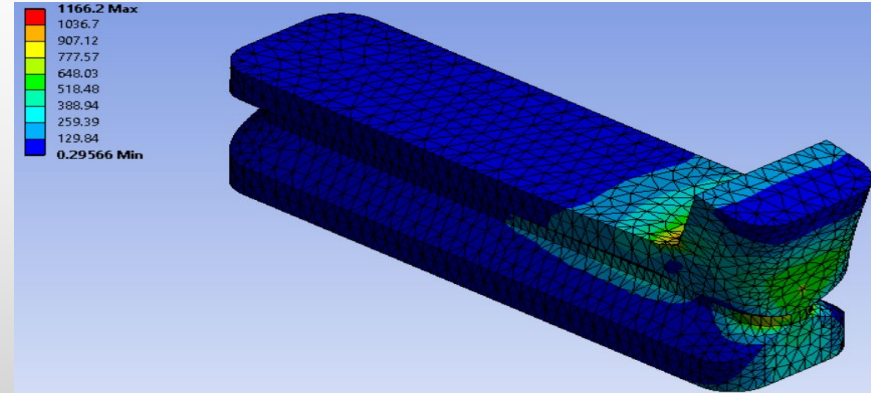
- Whiffletree loading test to verify Matlab model.
- Will hang 8.245 pounds to simulate straight and level flight with FOS of 2



# Motor Mount Ansys Analysis

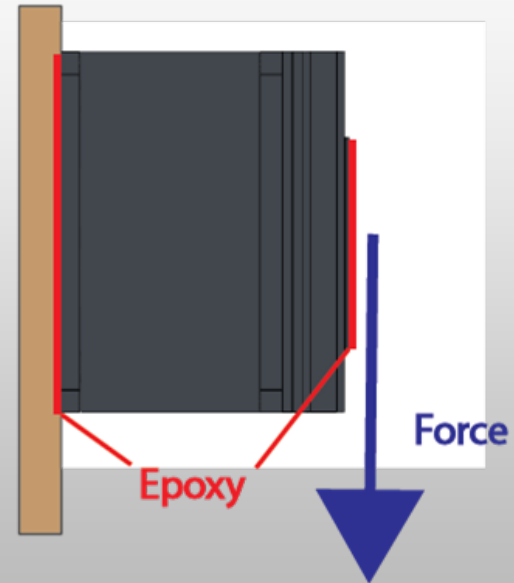
- Maximum stress: 1036.7 psi
- Epoxy rating: 3400 psi

Material	Tensile Strength [psi]
PLA	6066.23
ABS	5656.47
Onyx with Carbon Fiber	101526



# Structural Requirements

- 3D print engine mount and epoxy base to stationary balsa wood
- Epoxy hook to engine side of engine mount
- Hang weight from hook to emulate thrust
- Add weight until mount breaks
- Note how it broke (shear, bending, glue failure, etc.)



# Structural Requirements

Item(s)	Mass [g]	Mass [lb]
Airframe	518	1.1419
Motor and Mount	680.29	1.4998
Electronics	218.09	0.4808
Payload	498.95	1.1000
<b>Total</b>	<b>1,915.33</b>	<b>4.2225</b>

# Test Backup

1. Software Testing
2. Structures Testing
3. Aerodynamics Testing
4. Controls/PixHawk
5. Test Regulations
6. Test Regulations



# Software

- **Purpose:** Verify functionality of target detection and geolocation software (**FR 4**)
- **Location/Facilities:** North Boulder Park
- **Equipment:**
  - DGI Phantom Standard (Drone)
  - Cardboard
  - Bright Tape
- **Measurements:**
  - GPS and altitude data of drone
  - Images of target
  - Actual GPS location of target
- **Methods:** Capture images of scaled down target with drone from up to 350ft altitude.



# Structures

- **Purpose:** Verify structural integrity of wing/motor mount (FR 1)
- **Location:** Outside of ITLL
- **Equipment:**
  - AndREaS Glider
  - Eye Hook
  - 5 Gallon Bucket
  - Epoxy
  - 3D Printed Motor Mount
  - Vice Grips
- **Measurements:**
  - Failure of Wings/Motor Mount
- **Methods:**
  - Insert eye hook into nose of glider
  - Hold glider by wingtips
  - Hang weight from eye hook
  - Progressively increase weights
  - Repeat for motor mount

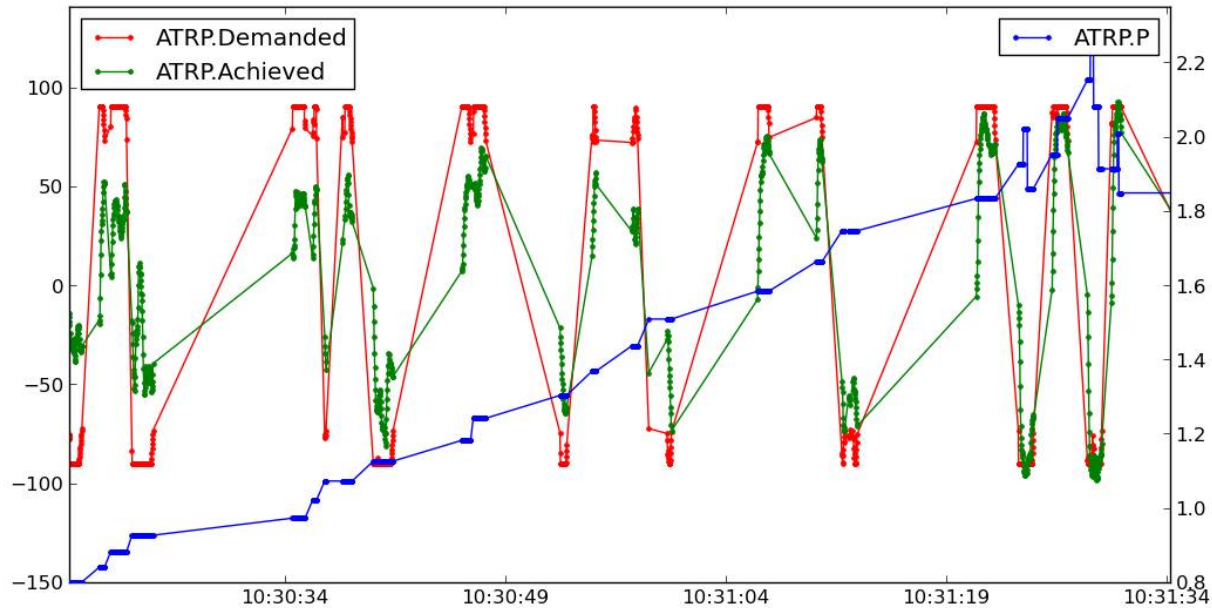
Picture coming soon

# Aerodynamics

- **Purpose:** Verify CFD analysis
- **Location/Facilities:** ITLL
- **Equipment:**
  - 3D Printer
  - ASEN Dept. Wind Tunnel
- **Measurements:**
  - Axial force
  - Normal force
  - Pitching moment
- **Methods:**
  - 3D print a scale model of glider
  - Mount model in wind tunnel
  - Vary angle of attack
  - Compute  $C_L$ ,  $C_d$ , and  $C_m$



# Controls/PixHawk



# Test Regulations

Requirement	Derived From
1 A member at launch shall have a level 1 certification for high powered rockets	NFPA Code 1127
2. Rocket shall be launched no greater than 20 degrees from vertical	NFPA Code 1127
3. Shall be launched through a local rocketry club at an appropriate launch site	NFPA Code 1127
7. Unmanned and does not create a hazard to any persons, property, or other aircraft	14 CFR Part 101.23
5. Operating requirements in Part 101.25	14 CFR Part 101.25
6. Proper notification is given to FAA as defined in Part 101.27	14 CFR Part 101.27
7. Aircraft shall be capable of manual controls override	AMA Doc #560
8. Vehicle shall weigh less than 55 lbs (Fig. 101.41)	14 CFR Part 101.41

# Test Regulations

## § 101.25 Operating limitations for Class 2-High Power Rockets and Class 3-Advanced High Power Rockets.

When operating *Class 2-High Power Rockets* or *Class 3-Advanced High Power Rockets*, you must comply with the General Operating Limitations of § 101.23. In addition, you must not operate *Class 2-High Power Rockets* or *Class 3-Advanced High Power Rockets* -

- (a) At any altitude where clouds or obscuring phenomena of more than five-tenths coverage prevails;
- (b) At any altitude where the horizontal visibility is less than five miles;
- (c) Into any cloud;
- (d) Between sunset and sunrise without prior authorization from the FAA;
- (e) Within 9.26 kilometers (5 nautical miles) of any airport boundary without prior authorization from the FAA;
- (f) In controlled airspace without prior authorization from the FAA;
- (g) Unless you observe the greater of the following separation distances from any person or property that is not associated with the operations:
  - (1) Not less than one-quarter the maximum expected altitude;
  - (2) 457 meters (1,500 ft.);
- (h) Unless a person at least eighteen years old is present, is charged with ensuring the safety of the operation, and has final approval authority for initiating high-power rocket flight; and
- (i) Unless reasonable precautions are provided to report and control a fire caused by rocket activities.