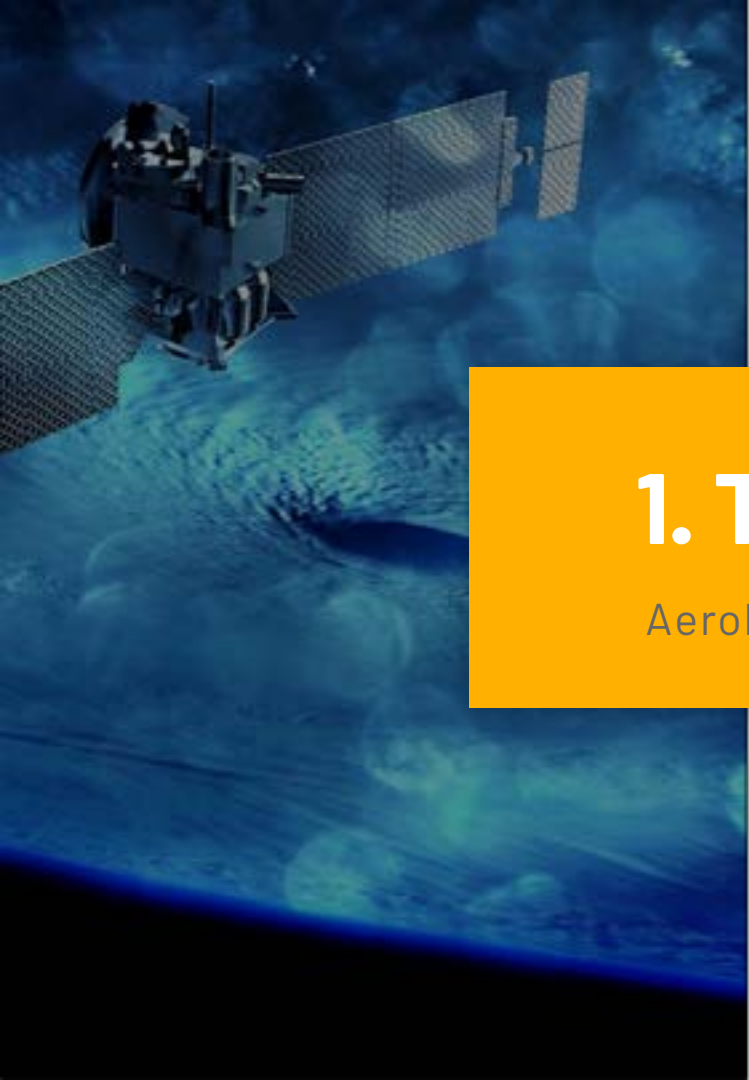


The background of the slide features a grayscale image of a spacecraft's heat shield and parachutes as it descends through the atmosphere of Mars. The surface of Mars, with its characteristic craters, is visible at the bottom of the frame.

# **AEROBRAKING AT MARS: A Machine Learning Implementation**

Giusy Falcone  
Zachary R. Putnam

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University of Illinois at Urbana-Champaign



# 1. THE CONCEPT

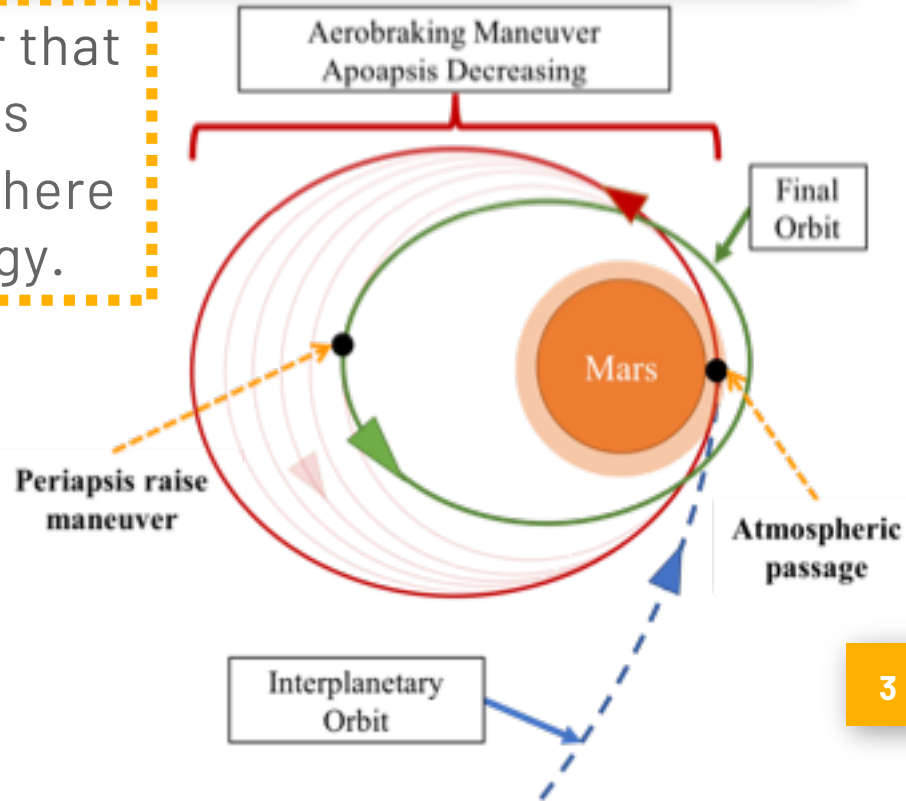
Aerobraking, Autonomy, Goal & Challenges

# AEROBRAKING



Aerobraking is a maneuver that uses successive passes through the upper atmosphere to dissipate orbital energy.

Creation of drag is a function of velocity and flight-path angle  
Propulsive maneuvers at apoapsis control velocity and flight-path angle



# IMPORTANCE OF AEROBRAKING & AUTONOMY



## Benefits and Costs

Massive propellant saving WRT single propulsive maneuver at the expense of risk caused by variability in atmospheric density (**heat rate & dynamic pressure**)

Successfully performed for three Mars missions:

- Mars Global Surveyor (1996)
- Mars Odyssey (2001)
- Mars Reconnaissance Orbiter (2005)

## Importance of Autonomy

Ground cost, a team of engineers always-online, less aggressive conditions (more when orbital period decreases)

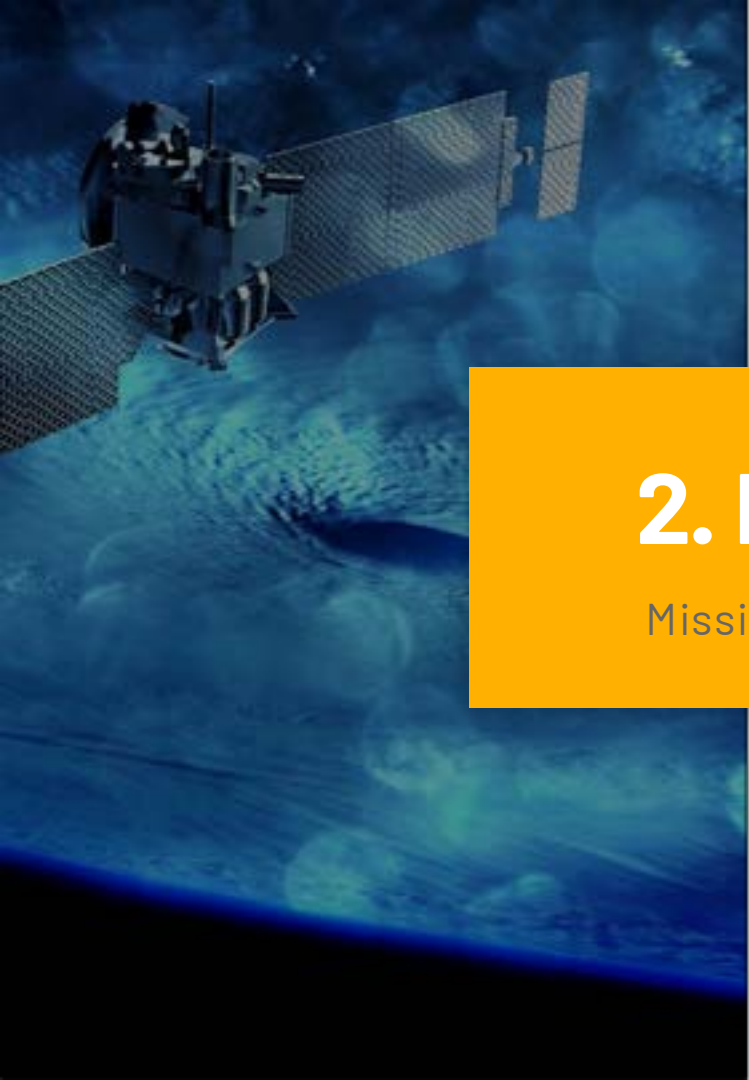
Previous efforts to address these issues with autonomy:  
Aerobraking Autonomous Control (1999-2012)

# GOAL AND CHALLENGES



Perform a complete and successful autonomous aerobraking campaign at Mars with a learning and adaptive behavior approach while:

1. Satisfying constraints on dynamic pressure and heat rate
2. Managing mission risk
3. Minimizing control effort and time of flight (**cost**)



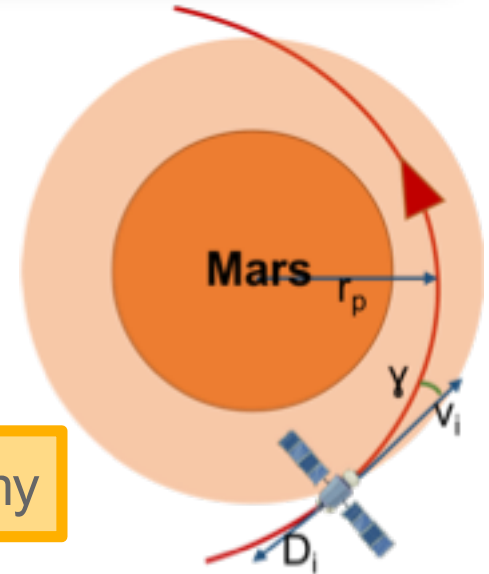
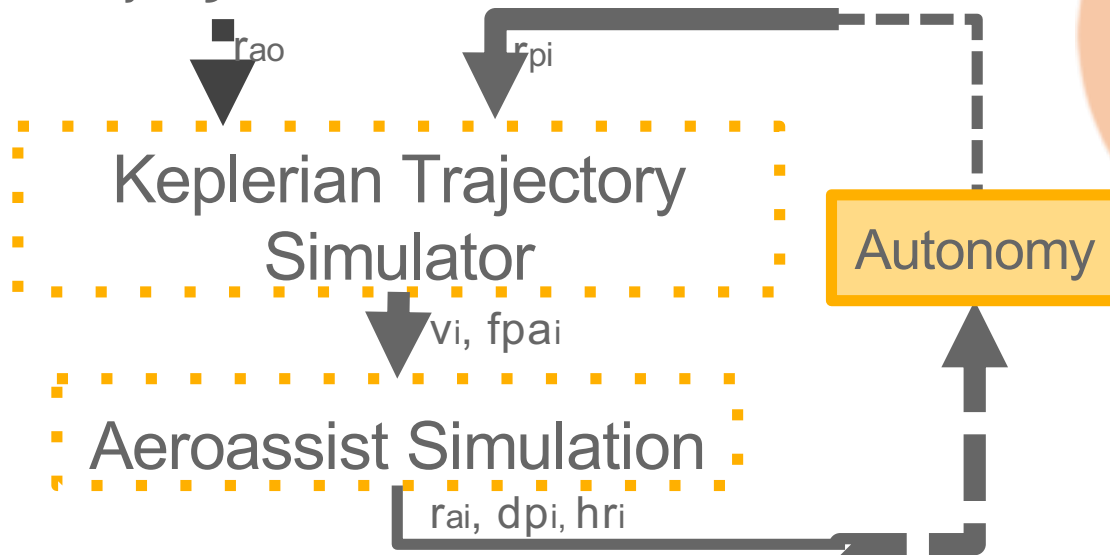
## 2. PROBLEM FORMULATION

Mission Modeling, Reinforcement Learning and Interface

# AEROBRAKING MISSION MODELING



Aerobraking mission: vary periapsis altitude to lower apoapsis altitude while satisfying constraints



# REINFORCEMENT LEARNING



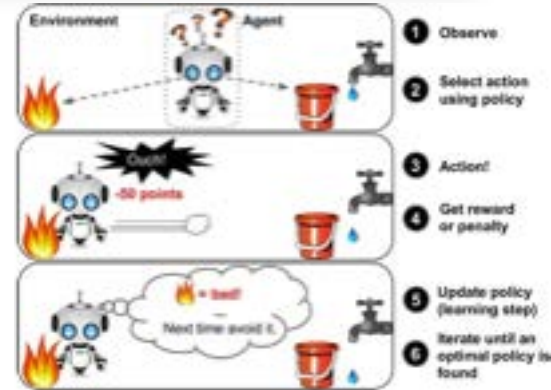
Tabular Q-Learning Algorithm with  $\epsilon$ -greedy policy search

$$\langle S, A, P^{a_{ss'}}, R^{a_{ss'}}, \gamma \rangle$$

S = apoapsis radius

A = periapsis altitude

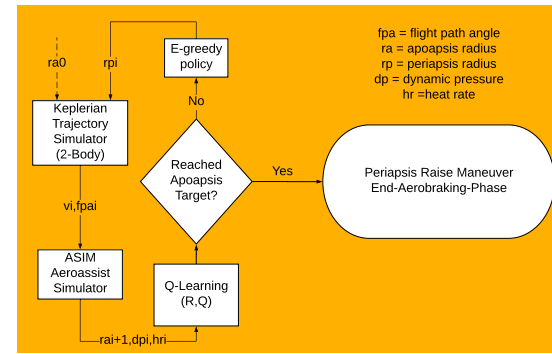
$R^{a_{ss'}}$  = reward built to minimize the aerobraking whole time.



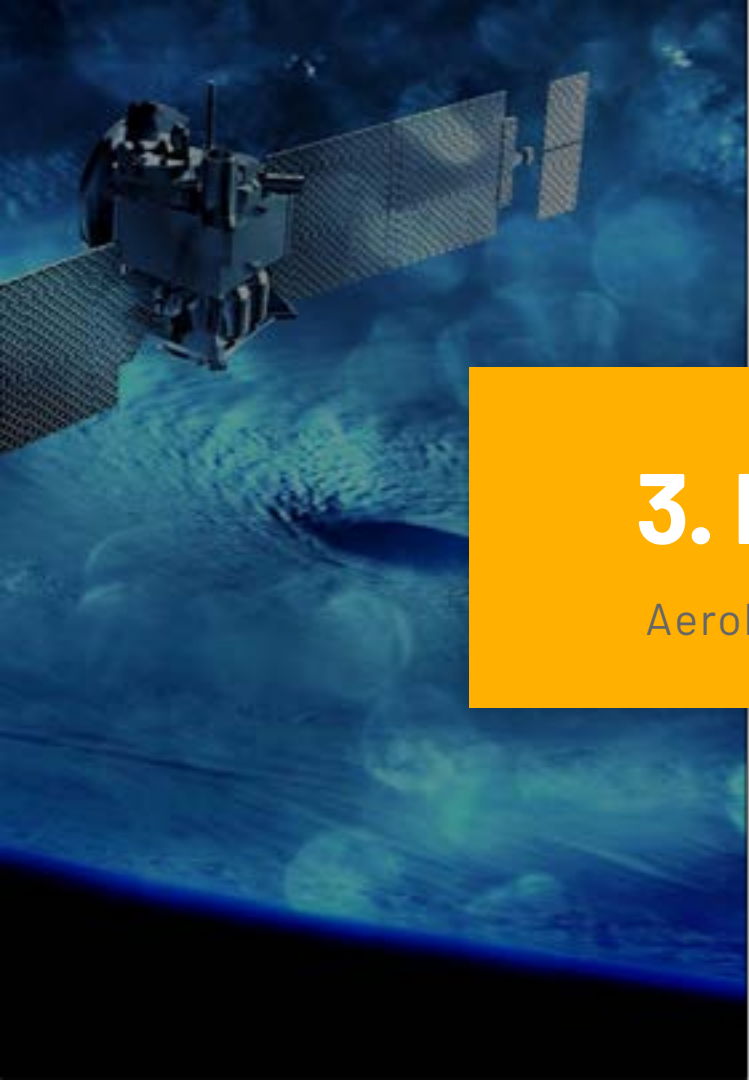
“ Reinforcement learning is learning what to do...so as to maximize a numerical reward signal. (Sutton)



# INTERFACE BETWEEN MISSION AND RL



A trained policy chooses when perform a trim maneuver to minimize the aerobraking time and to avoid the violating constraints.



# 3. RESULTS

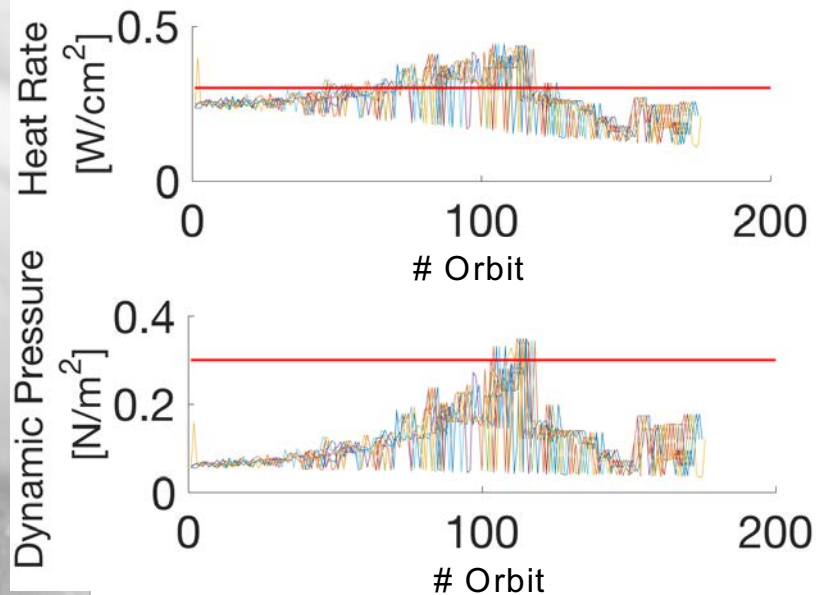
Aerobraking Simulation, Constraints & Corridor, Learning

## AEROBRAKING SIMULATION

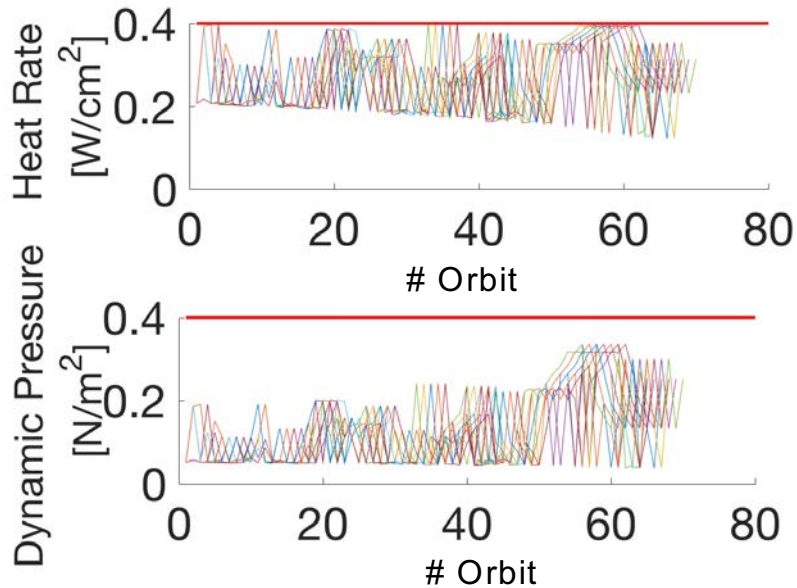
Apoapsis radius  
from 200,000 km  
to 5,000 km



# CONSTRAINTS AND CORRIDOR

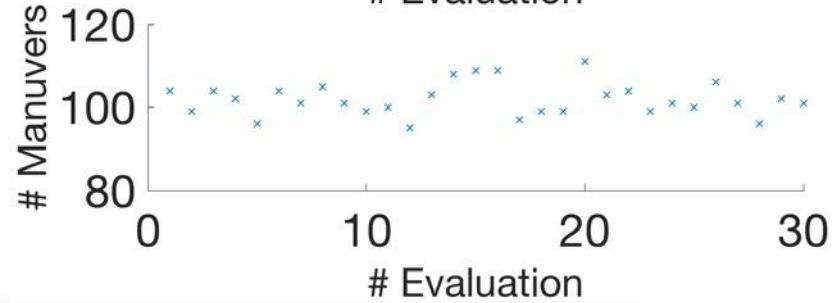
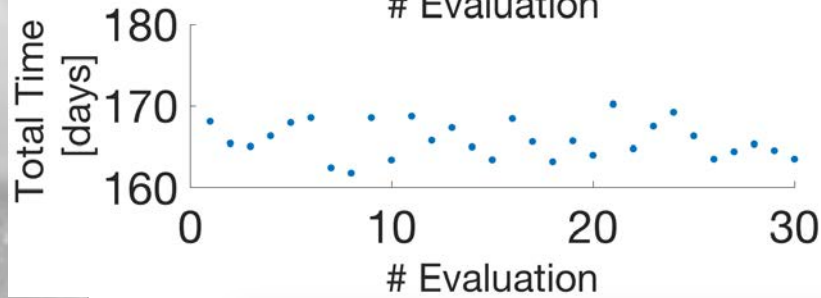
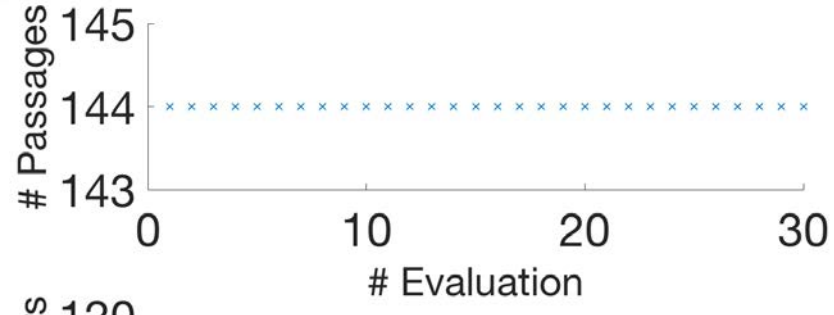
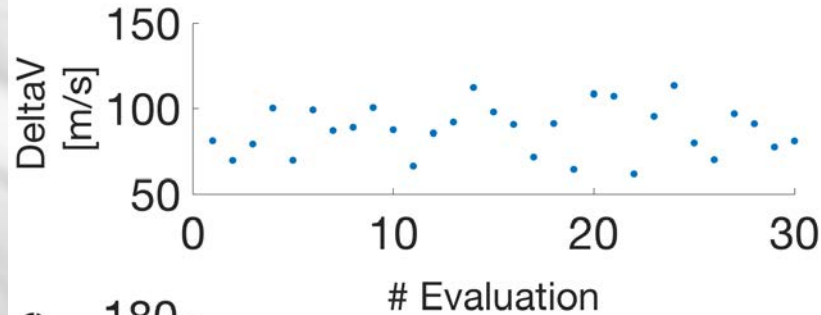


**NOT TRAINED MACHINE**

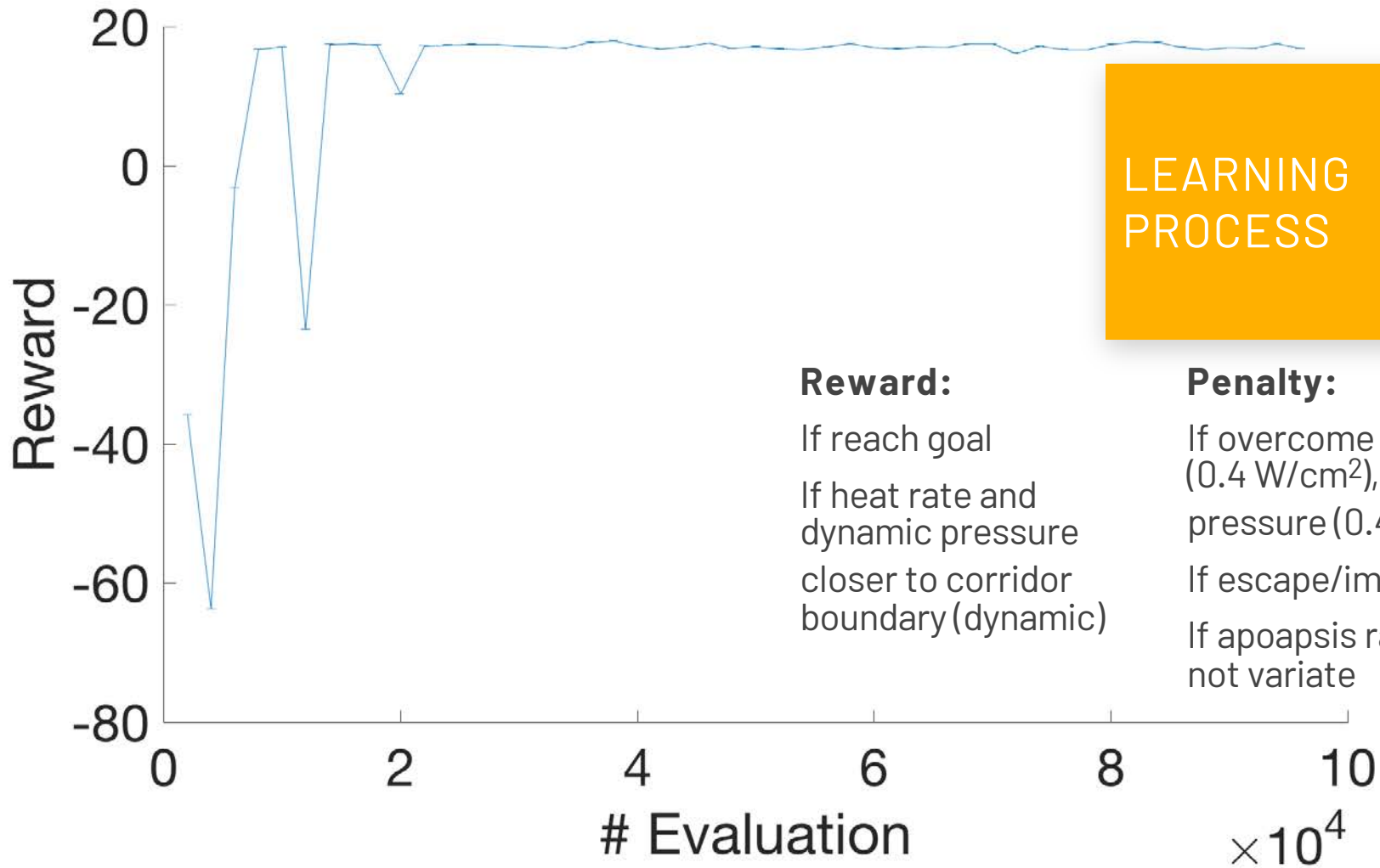


**TRAINED MACHINE**

# RESULTS DELTA-V AND TOTAL TIME



**REWARD FUNCTION DECREASES ONLY TOTAL TIME**



LEARNING  
PROCESS

**Reward:**

- If reach goal
- If heat rate and dynamic pressure closer to corridor boundary (dynamic)

**Penalty:**

- If overcome heat rate ( $0.4 \text{ W/cm}^2$ ), dynamic pressure ( $0.4 \text{ N/m}^2$ )
- If escape/impact
- If apoapsis radius does not variate



# THANKS!

**Any questions?**

You can find me at:

`gfalcon2@illinois.edu`

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# MISSION DESIGN CHARACTERISTICS



## Small Satellite

Mass: 110 kg

Drag Area: 10 m<sup>2</sup>

C<sub>D</sub>: 1.2

## Keplerian Trajectory Simulator (2-bodies)

$$\ddot{r} - r\dot{\vartheta}^2 = -\frac{\mu}{r}$$

## Aeroassist Simulator

3 DOF equations of motion. Numeric simulation integrated using a fourth order Runge-Kutta scheme.

Density model: Mars-Gram 2010

# REINFORCEMENT LEARNING



Markov Decision Process (stochastic):

$$\langle S, A, P^{a_{ss'}}, R^{a_{ss'}}, \gamma \rangle$$

S = state space (apoapsis radius)

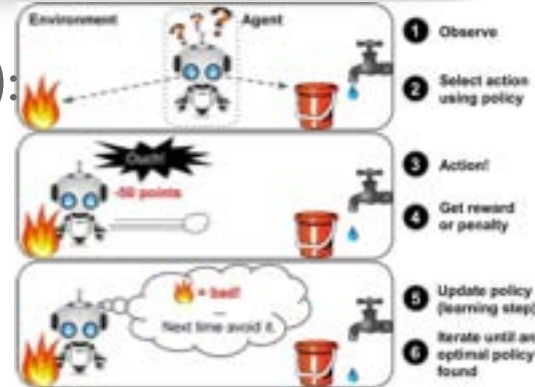
A = action space (periapsis altitude)

$P^{a_{ss'}}$  = probability of getting into  $s'$  after  $a$  from  $s$

$R^{a_{ss'}}$  = expected reward from  $s$  to  $s'$  after  $a$

Find policy  $\pi^*$  through iteration Bellman eq.

$$Q^*(s, a) = \sum_{s' \in S} P_{ss'}^{\pi(s)} [R_{ss'}^a + \gamma \max_{a'} Q^*(s', a')]$$



# MDP



## STATE SPACE

Apoapsis radius

From 4000 to  
400000 km.

981 states.

## ACTION SPACE

Periapsis altitude

From 105 to 127 km.

147 states.

## REWARD FUNCTION

### **Reward:**

Reach goal.

If closer to corridor  
boundary (dynamic).

### **Penalty:**

Overcome heat rate (0.4  
W/cm<sup>2</sup>), dynamic  
pressure (0.4 N/m<sup>2</sup>).

Escape/Impact.

If apoapsis radius does  
not variate.

# Q-LEARNING ALGORITHM



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## Algorithm 5: Q-Learning

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Complexity

**Input:**  $\text{MDP} \setminus \{\mathcal{P}, \mathcal{R}\}, \alpha, \epsilon$

**Output:**  $\pi$

1  $\theta \leftarrow$  Initialize arbitrarily

2  $\langle s, a \rangle \leftarrow \langle s_0, \pi^\epsilon(s_0) \rangle$

3 **while** time left **do**

4     Take action  $a$  and receive reward  $r$  and next state  $s'$

5      $Q^+(s, a) \leftarrow r + \gamma \max_{a'} Q(s', a')$

$\mathcal{O}(n|\mathcal{A}|)$

6      $\delta \leftarrow Q^+(s, a) - Q(s, a)$

7      $\theta \leftarrow \theta + \alpha \delta \phi(s, a)$

$\mathcal{O}(n)$

8      $\langle s, a \rangle \leftarrow \langle s', \pi^\epsilon(s') \rangle$

$\mathcal{O}(n|\mathcal{A}|)$

9 return  $\pi$  greedy w.r.t.  $Q$

---

Off-policy and model free algorithm

# $\epsilon$ -GREEDY POLICY SEARCH



$\epsilon$ -greedy policy spans between exploration and exploitation:

- With probability  $1 - \epsilon$ , uses the greedy action:

$$a_i = \underset{a}{\operatorname{argmax}} \hat{Q}(s_i, a)$$

- With probability  $\epsilon$ , play random action.