

HIGH-EFFICIENCY MICROWAVE POWER AMPLIFIERS THROUGH  
PASSIVE AND ACTIVE HARMONIC CONTROL

by

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M.S., University of Colorado at Boulder, 2016

B.S., University of Colorado at Boulder, 2013

A thesis submitted to the  
Faculty of the Graduate School of the  
University of Colorado in partial fulfillment  
of the requirements for the degree of  
Doctor of Philosophy  
Department of Electrical, Computer, and Energy Engineering  
May 2019

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High-efficiency Microwave Power Amplifiers Through Passive and Active Harmonic Control

Thesis directed by Professor Zoya Popović

The design of the next generation of microwave transmitters must advance in stride with state-of-the-art radar, communication, and remote-sensing systems. As the performance of high-frequency transmitters improves, so too do the systems and the science which rely on them. Among the forefront of challenges facing the design of active microwave components is that of enabling highly-efficient operation. Doing so demands the application of a breadth of circuit and electromagnetic theory to overcome pragmatic limitations imposed by factors such as lossy circuit elements, non-linear reactances, and parasitic impedances. The praxis of active and passive microwave design to high-frequency power amplifiers (PAs) serves to further the state-of-the-art and empower the industry to which it is applied. Gainful applications of highly-efficient PAs lie in both communication and sensing. In satellite transmitters, e.g., power and volume is significantly limited, and the communication of data to terrestrial networks is directly affected by the efficiency of the transmitter PA.

Non-linear microwave power transistors inherently generate power at harmonic frequencies. In this work, harmonic power is controlled with both passive and active impedances in order to precisely engineer current and voltage waveforms at the current generator plane. Transistor packages present highly-reactive impedances that significantly limit harmonic control, but can also be used as a part of the matching network. In the L- and S-band PAs demonstrated in this thesis, bond-wires and package parasitics are analyzed with full-wave EM simulations and used to control amplitude and phase of up to 3 harmonics. This results in compact, highly-efficient in-package PAs with efficiencies ranging from 65% to 80% at around 10-W output power. Methodology is developed which can be applied to any package and transistor with known geometry and non-linear model. In addition to passively terminating harmonic frequencies, active terminations are investigated as a means to obtain efficiency and linearity, and a comparison between the two performed.

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# INTRODUCTION

In microwave transmitters used for both communications and radar, the final stage power amplifier efficiency is of critical importance [1]. For example, approximately 40% of the total power consumption in a satellite is attributed to the communications transmitter [2]. Although many current high-power transmitters are based on tubes (eg. TWTs) there has been a continuous focus on replacing tubes with solid-state devices. At lower microwave frequencies (up to approximately 2 GHz) LDMOS is used in the majority of terrestrial cellular systems while GaAs is predominantly used in space for lower power levels. Over the past decade, GaN devices which operate at a higher voltage resulting in larger power densities, are gaining attention.

In order to operate at higher frequencies, transistor gate dimensions must be reduced for lower capacitance. However, this results in an increased resistance, which limits the power handling due to heat generated in a small volume. Removing the heat is challenging and limits system performance. This is especially true for space-based systems, and for active arrays. Therefore, improving efficiency is an enabler for high-performance communication and sensing systems.

Methods for improving amplifier efficiency include improving the efficiency of a single transistor through voltage and current waveform shaping (Fig. 1.1a), to transmitter architectures which combine several amplifiers with the goal of efficiency enhancement. Shown in Fig. 1.1 are architectures

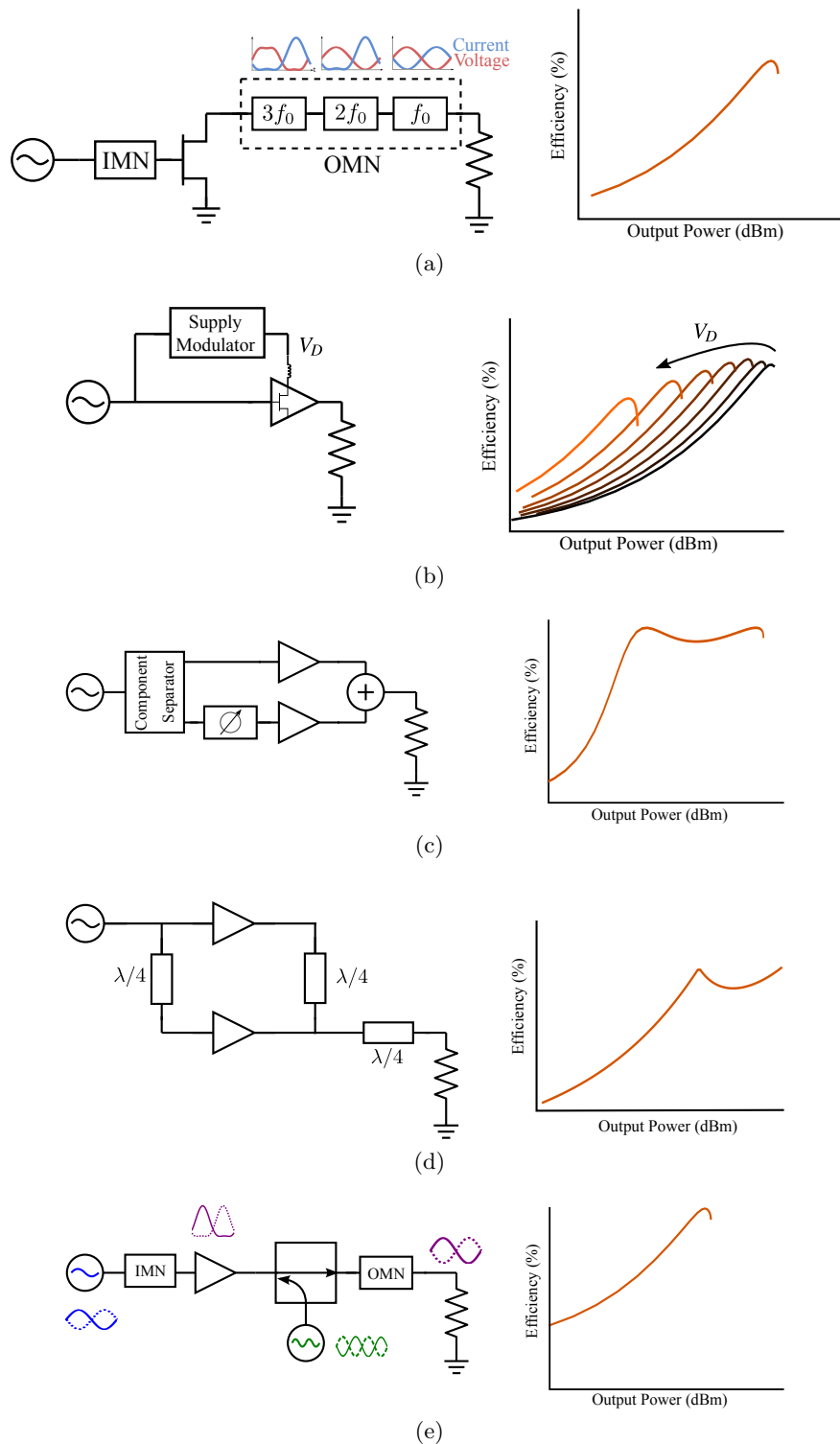


Figure 1.1: Power Amplifier architectures for enabling high-efficiency communication transmitters: (a) Single-ended harmonically-terminated PA, (b) Supply-modulated PA, (c) Outphasing PA, (d) Doherty PA 1.1.d, and (e) the Harmonic Injection PA.

that can be used to efficiently amplify modern communication signals which have phase and amplitude modulation and therefore a significant variation in output power. A single-ended PA can be designed to be efficient over a small range of input powers using passive harmonic terminations Fig. 1.1a. In supply modulation, a low-frequency amplifier is used to modulate the drain supply of a single-ended PA in proportion to the input signal power (envelope) level [3]. An outphasing PA (Fig. 1.1c) decomposes a complex modulated signal into two signals with constant envelope varying in relative phase [4] so that each transistor can be designed to be efficient at a single power level [5]. A Doherty PA (Fig. 1.1d) broadens the range of power levels at which high efficiency is achieved by using 2 asymmetric transistors which are individually efficient at different input powers [6]. In the harmonic injection architecture (Fig. 1.1e), the output of a transistor in linear operation is injected by the input signal doubled in frequency to effectively present an active 2nd harmonic termination without forcing strongly non-linear operation of the PA [7]. This thesis focuses on the single-ended PA (Fig. 1.1a) with special emphasis on redesigning transistor packages to further improve efficiency (Chapters 3-5), and then addresses improving the linearity and efficiency of a PA through the use of harmonic injection on modulated signals (Chapter 6), Fig. 1.1e. The device technologies used for demonstrating the concepts includes LDMOS and GaN for the 2-GHz range.

Table 1.1 summarizes the state-of-the-art efficiencies for LDMOS-based amplifiers in the lower GHz range. These are implemented in various classes of operation, which refer to different waveforms of the voltage and current. Standard reduced conduction angle classes (A, B, AB, C) are limited in the efficiency they can achieve, e.g. 78.5% for the class-B case, which is significantly reduced in realistic lossy amplifiers [8]. In all but class-A, the current waveform is not sinusoidal, and contains harmonic frequency components generated by the transistor non-linearities. In classes A-C, harmonics are not used as a part of the design. Classes F, F<sup>-1</sup>, J use the generated harmonic content to synthesise specific waveform shapes based on Fourier components [9]. Generally speaking, harmonics are used to square the voltage or current waveform which reduces the time-domain overlap of  $v(t)$  and  $i(t)$ , thus reducing dissipation [1]. In classes D and E, the transistor is used as a switch [10]. In class-E, the transistor should operate up to a frequency that is approximately five



times the operating frequency of the PA in order to enable efficient soft-switching. Similar results for GaN are reviewed in [11].

## 1.1 MOTIVATION

For single-ended high efficiency PAs (Fig. 1.1a), the overlap between current and voltage in the time-domain waveform is minimized by harmonic control for waveform shaping, within the transistor. Transistors can be in an integrated circuit, or diced in chip form and then packaged. At lower microwave frequencies for higher power levels, the devices are usually diced and mounted in standard packages that provide good thermal and electrical contacts.

Consider the commercially available PTFC260202FC Infineon packaged LDMOS 10-W device with internal pre-matching at 2.6 GHz. Series bond-wires serve as both an interconnect from the device to the drain tab and as an impedance transformation from the low output impedance of the LDMOS die ( $\sim 1 - j4\ \Omega$ ) to a higher impedance ( $\sim 20\ \Omega$ ). Fig. 1.2b defines the reference planes at which it is relevant to observe the impedance at the fundamental and harmonics. For the given package, the calculated normalized voltage and current waveforms starting from efficient class-F waveforms, assuming it is possible to correctly synthesize these at the virtual drain, are shown as they transform through the package. It is seen that the package parasitics eliminate all harmonic content after the package reference plane. Fig. 1.3 shows the limited range of harmonic impedances that can be presented at the transistor's virtual drain (current source). The grey uniformly spaced dots indicate impedances presented at the package plane in Fig. 1.3 using an ideal tuner. The tab and the pre-match significantly shrink the impedance range available at the die plane, at the 2<sup>nd</sup> and 3<sup>rd</sup> harmonics. The effect is even more pronounced at the virtual drain, where the 3<sup>rd</sup> harmonic range is reduced to a point. This illustrates how fundamental-only package design limits harmonic termination range and therefore high-efficiency operation.

The goal of this thesis is to enable high-performance amplifiers by moving the design plane into the package. This accomplishes not only smaller PAs, but also can be used to maximize efficiency

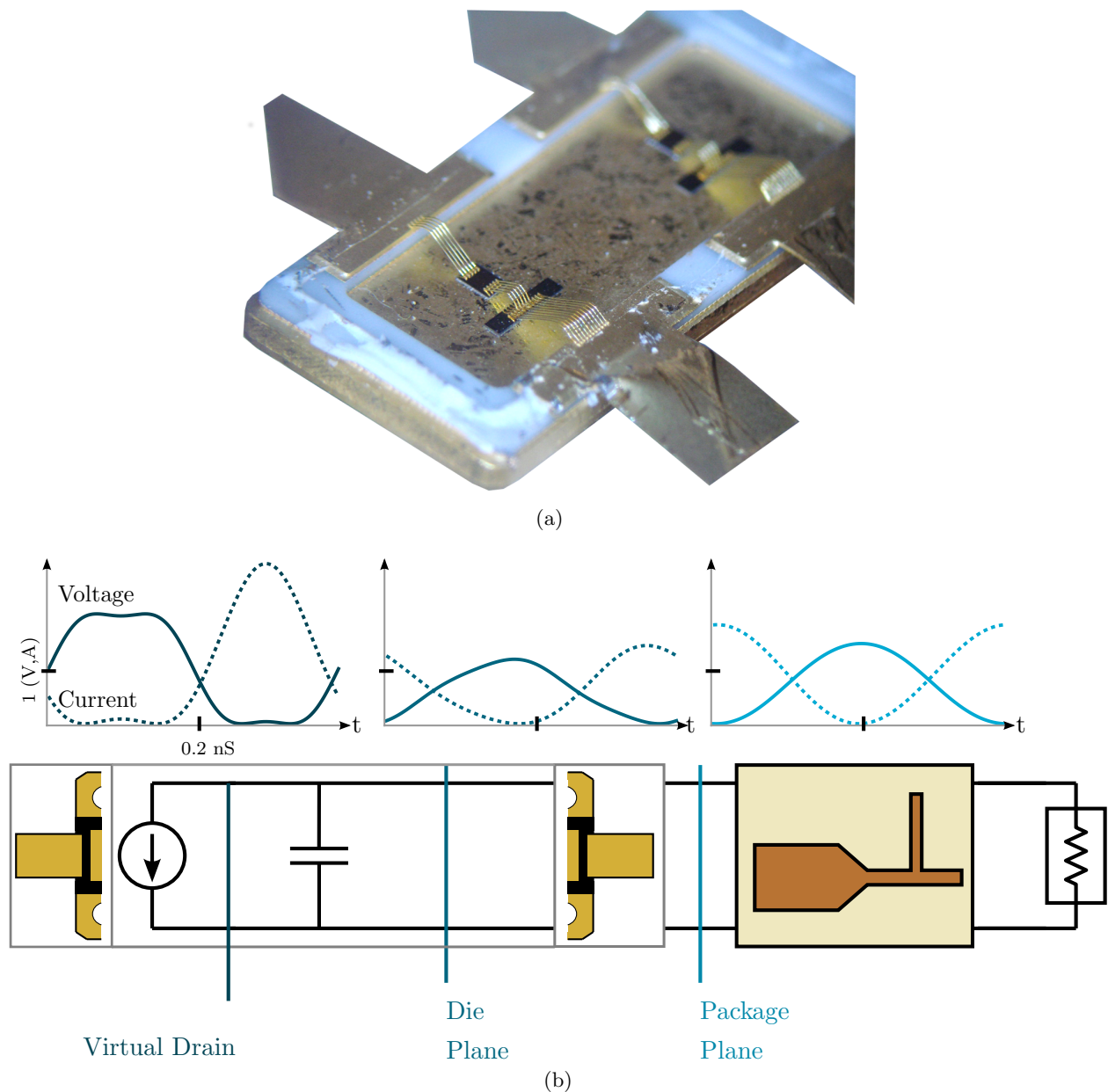


Figure 1.2: (a) Photo of a typical high-power packaged transistor for operation around 2 GHz. (b) Block diagram of the output side of a PA using a packaged transistor, with relevant reference planes labeled. The current and voltage waveforms are calculated from the package in Fig.1, starting from class-F waveforms approximated with a  $2^{nd}$  and  $3^{rd}$  at the virtual drain plane.

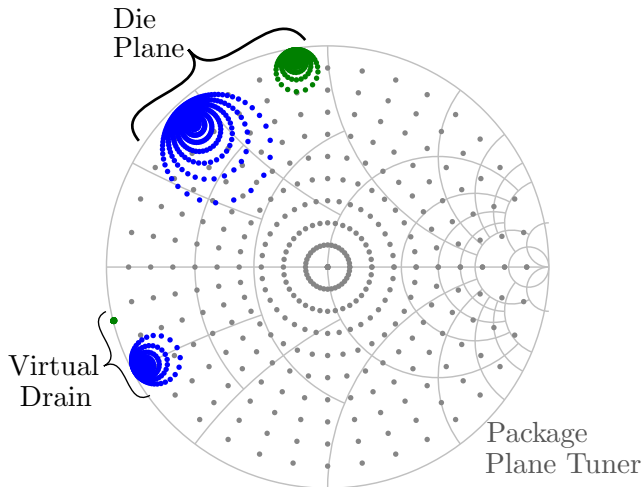


Figure 1.3: The transformed constellation presented at the Die Plane at  $2f_0$  (blue) and  $3f_0$  (green) and at the Virtual Drain plane for commercial package at 2.6 GHz. This illustrates the limited range of passive impedances that can be reached by matching outside of the package.

as will be detailed in Chapters (2-5).

## 1.2 DESIGN METHODS FOR HIGH-EFFICIENCY AMPLIFIERS

High-efficiency amplifiers can be designed using non-linear circuit simulations which rely on a accurate non-linear device models provided usually by the manufacturer. Such a model is incorporated into a harmonic-balance analysis implemented in standard microwave circuit simulators such as Keysight ADS and NI AWR Microwave Office, both of which are used in this thesis. Most non-linear models, however, are not designed to accurately model extremely high efficiency modes of operations and often are either validated or replaced by empirical models obtained from load-pull measurements [28]. However, load-pull systems are expensive and complicated to set up and calibrate. This is particularly true for systems which include control of harmonic impedances. The losses of traditional, passive load-pull systems can be overcome through the use of an active load-pull system. Using active load-pull at harmonic frequencies is limited by the power available from the harmonic sources.

In this thesis, all of the above design methods are used to optimize the efficiency of a given transistor in an amplifier. A specific active load-pull system developed by Mesuro (now Focus

Table 1.1: Comparison of LDMOS Performance between 1-4 GHz

Year	Freq (GHz)	PAE (%)	Class	Pout (W)	Gain (dB)	System
2004 [12]	1	73.8	F	12.4	12.9	—
2006 [13]	1	71.9	$F^{-1}$	13.2		—
2003 [14]	1	70	E	6.2	10	—
2006 [15]	1	60 ( $\eta$ )	$F^{-1}$	12.4		Load Modulation
2006 [16]	1	71 ( $\eta$ )	CMCD	20	15.1	—
2010 [17]	1	75	F	15		—
2009 [18]	1	80	AB	10		—
2006	1	69	$D^{-1}$			—
2005 [19]	1.8	60 ( $\eta$ )	$F^{-1}$	13	10	—
2008 [20]	2.1	77	F	5		—
2011 [21]	2.14	65	B/J*	2		ET, supply mod
2006 [22]	2.14	65	E	9.6	13.8	—
2003 [23]	2.14	62	Push-Pull	100	16.5	—
2013 [24]	2.5	61.7 ( $\eta$ )	—	30.2	13	Die, Modified process
2010 [25]	2.66	51 ( $\eta$ )	AB	1	20	—
2011 [26]	3.1	38 ( $\eta$ )	AB	130	8	—
2007 [27]	3.5	36.7	2-stage	29	26	—
2010 [25]	5.8	44	AB	0.93	11.8	—

Microwaves) was used to both evaluate the nonlinear model available from Infineon, as well a starting point for design of miniaturized package-level amplifier design, as is described in the next chapter.

### 1.3 THESIS ORGANIZATION

The work in this thesis will demonstrate using the signal harmonics to significantly improve PA performance inside a standard package, eliminating large and lossy printed circuit board (PCB) based implementations. Presented are novel solutions to the limitation on harmonic control for traditionally packaged RF/microwave devices - first through the design of passive elements and parasitics of a transistor package, then through an architecture which overcomes the loss of control

through the use of active harmonic impedances. The discussion begins in Chapter 2 where the various tools for the characterization of non-linear devices are discussed, as well as the impact of harmonic power on device efficiency. This chapter also shows characterization of a commercially packaged transistor in large-signal measurement to further illustrate efficiency limitations.

In Chapter 3, the passive package environment is simulated and modeled with full-wave finite-element tools, including mutual parasitic reactances. The modeling of the 3-dimensional electromagnetic environment of the transistor is used in conjunction with harmonic balance simulations to inform subsequent PA designs. In Chapter 4, the techniques and tools of the previous chapters are used to design in-package matching networks using only surface mount capacitors and bond-wires resulting in an extremely compact LDMOS PA. This chapter also discusses designing packages to allow greater external harmonic control through harmonically pre-matched packages, as well as techniques to fully terminate harmonics internally. This technique will be demonstrated on multiple package designs, each with 4 uniquely phased highly-reflective  $2^{nd}$  harmonic impedance. Also presented in Chapter 4 is a method for validating in-package networks up to all harmonics frequencies of interest.

Chapter 5 presents two package designs which present a matched, complex fundamental impedance to the device while also terminating the  $2^{nd}$  and  $3^{rd}$  harmonics to enable waveform shaping at the device virtual drain, without the need for package-external matching. In particular, the design of two packages is detailed, each fully matched at the fundamental frequency while also terminating the  $2^{nd}$  and  $3^{rd}$  harmonics in an open or short at the transistor virtual drain. The first of the presented packages houses an LDMOS transistor, while the second designed around a GaN HEMT. Although the circuits differ because LDMOS device prefers current peaking, while the GaN device prefers voltage peaking, both designs require a large degree of full-wave simulations, non-linear characterization, and design iterations.

Finally, in Chapter 6, a highly efficient and linear PA design using active harmonic terminations is presented. In this approach, the waveform shaping within the active device is not limited by harmonics generated by the device itself. In the experimental GaN PA, the 2nd harmonic is

injected through a duplexor circuit. In addition to obtaining high efficiency, this approach allows control of linearity by controlling the amplitude and phase of the injected harmonic. Two-tone signal measurements are for the first time performed on such a PA, quantifying linearity. Some conclusions and directions for future work are outlined in Chapter 7, along with a summary of the contributions of this thesis.

# NON-LINEAR PACKAGED DEVICE CHARACTERIZATION

## CONTENTS

1.1	MOTIVATION . . . . .	4
1.2	DESIGN METHODS FOR HIGH-EFFICIENCY AMPLIFIERS . . . . .	6
1.3	THESIS ORGANIZATION . . . . .	7

In highly-efficient microwave transmitters, the transistor operates in strongly non-linear regimes in order to generate the harmonic content necessary for waveform shaping. The behavior of non-linear devices is difficult to predict accurately considering that they depend on detailed device semiconductor process dependent structure, DC bias point, continuous versus pulsed operation, signal characteristics, temperature, level of saturation, etc. Therefore in order to achieve an efficiency-optimized design, it is necessary to accurately characterize the device in large-signal operation.

Compact non-linear models of microwave FETs are typically used in circuit simulators to inform design [29]. These are usually developed by device manufacturers or specialized companies (e.g. Modelithics [30]) for the most common operating points, such as Class-A or AB. However when

designing a very high-efficiency PA, the transistor is biased further in cut-off and models become less accurate [31]. For high-efficiency performance it is necessary to design with the active device characterized up to all harmonic frequencies of interest and at multiple bias points.

If an accurate non-linear device model is not available, a measurement-based approach is often adopted. This consists of doing pulsed-IV measurements followed by load-pull [28]. During load-pull, the impedances presented to the device terminals are methodically varied at a given frequency, along with bias point and input power. The resulting performance is measured and the designer can observe trends and relate them to the circuit's condition to inform design. Load-pull can also be used to validate non-linear models and simulations. The work presented in this thesis will use both non-linear characterization techniques in order to achieve novel high-efficiency PAs. The following section illustrates the procedure of load-pull by discussing the non-linear characterization of a packaged LDMOS FET.

## 2.1 LOAD-PULL SIMULATION AND MEASUREMENT

Consider the Infineon PTFC260202FC packaged LDMOS FET, with typical CW RF characteristics at 2.62 GHz, 28 V:  $P_{1dB} = 25$  W,  $\eta = 57\%$ , Linear Gain = 19.4 dB as obtained from the datasheet. The package integrates 2 independent 10-watt LDMOS FETs, with internal fundamental pre-matching for cellular applications in 2495-2690 MHz. The characterization presented in this chapter involves only one of the two FETs.

A non-linear model (which includes package effects) provided by Infineon was used to perform simulated load-pull (LP) and source-pull (SP) in AWR Microwave Office at a Class-AB bias ( $V_d = 28$  V,  $I_{dq} = 170$  mA). The fundamental LP/SP PAE contours for a fixed input power (20 dBm) and the LP simulation setup, along with chosen impedance points presented to the device, are shown in Fig. 2.1. For each of the points on the Smith chart presented to the gate and drain, the PAE is measured and plotted as the contours shown in Fig. 2.1c, 2.1d. In the simulation, the LP tuners are ideal and the reference plane is at the package plane (see Fig.1.2b).



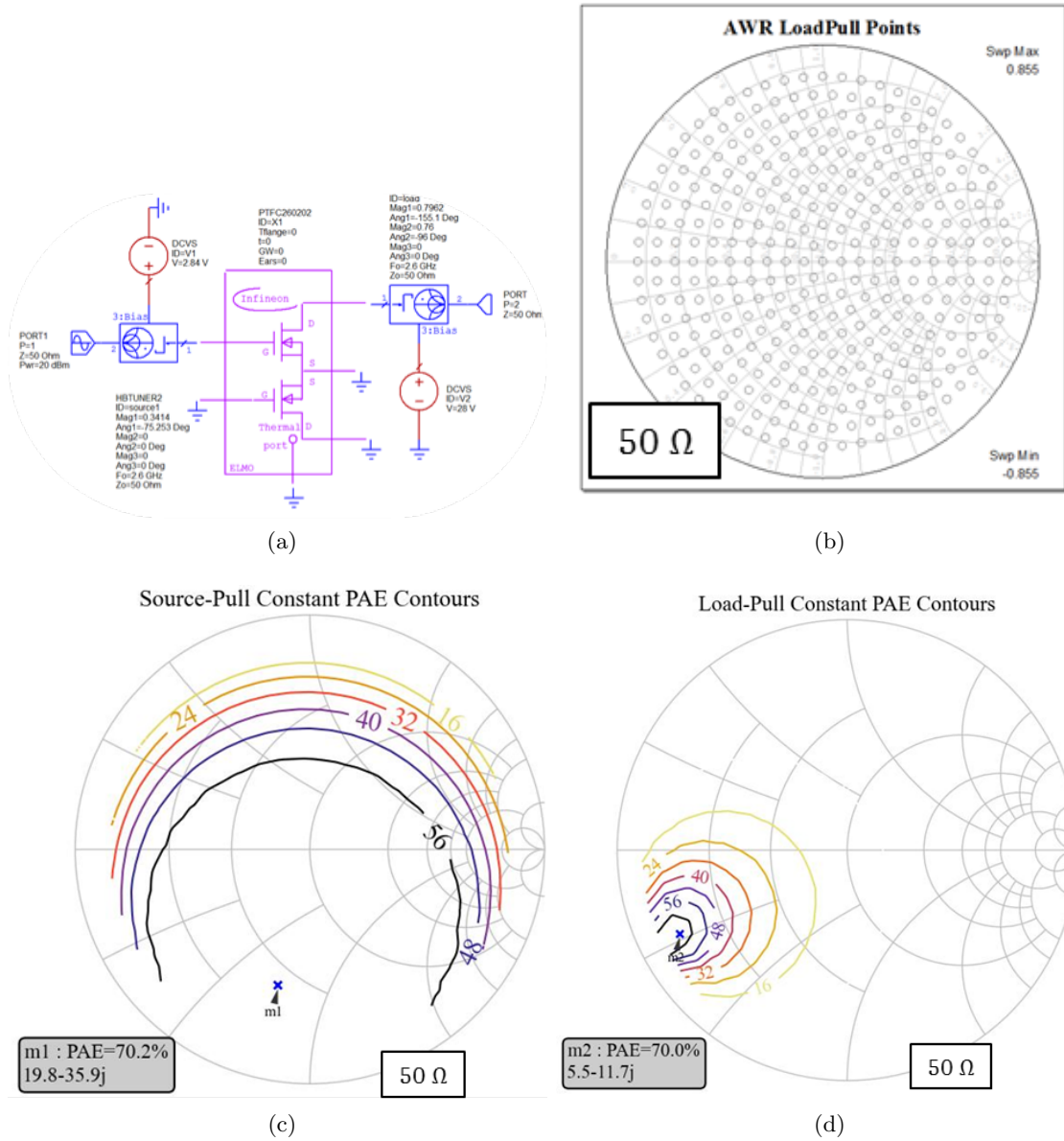


Figure 2.1: Fundamental LP simulation setup and non-linear model of packaged device PTFC260202FC at 2.6 GHz (a), constellation of impedance points presented during LP (b), Fundamental SP (c) and LP (d) PAE contours at a fixed input power (20 dBm).

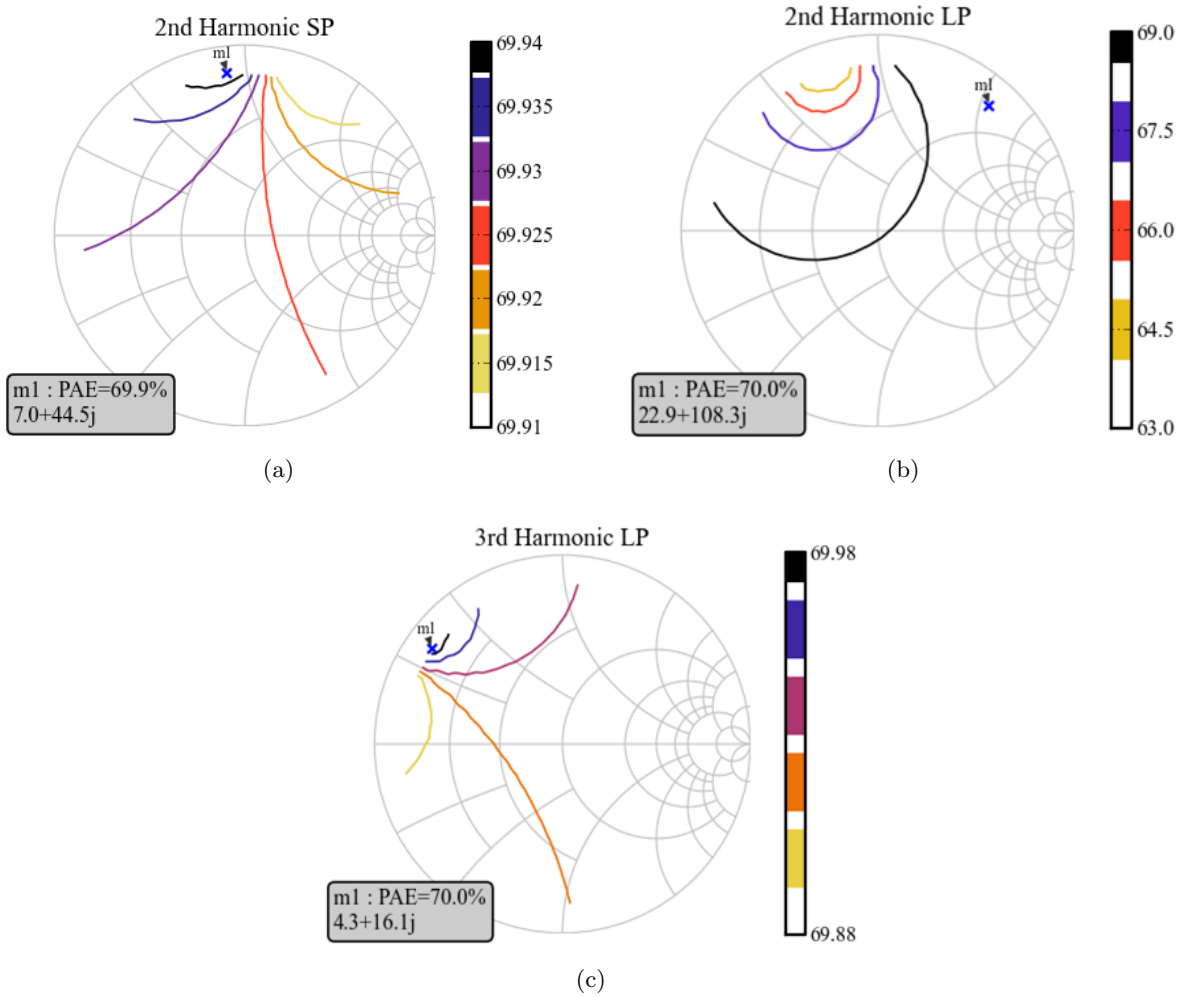


Figure 2.2: Simulated PAE contours for 2<sup>nd</sup> harmonic SP (a) and LP (b), and 3<sup>rd</sup> harmonic LP (c) on 50-Ω Smith charts. Impedance for max PAE is indicated by the marker.

The LP/SP was also performed at the 2<sup>nd</sup> and 3<sup>rd</sup> harmonic, with PAE contours shown in Fig.2.2. It was seen that the harmonics on the input are negligible, but are of consequence at the output. Choosing the proper 2<sup>nd</sup> harmonic impedance is shown to improve PAE by up to 7 points, while the 3<sup>rd</sup> harmonic showed no significant improvement. Therefore simulation concludes that with this device, at 2.6 GHz, only the load 2<sup>nd</sup> harmonic impedance has a practical impact on PAE. This is due to large package parasitic capacitances at the output, to be shown and discussed further in later sections.

Load- and source-pull were performed in measurement to validate simulation at the same bias

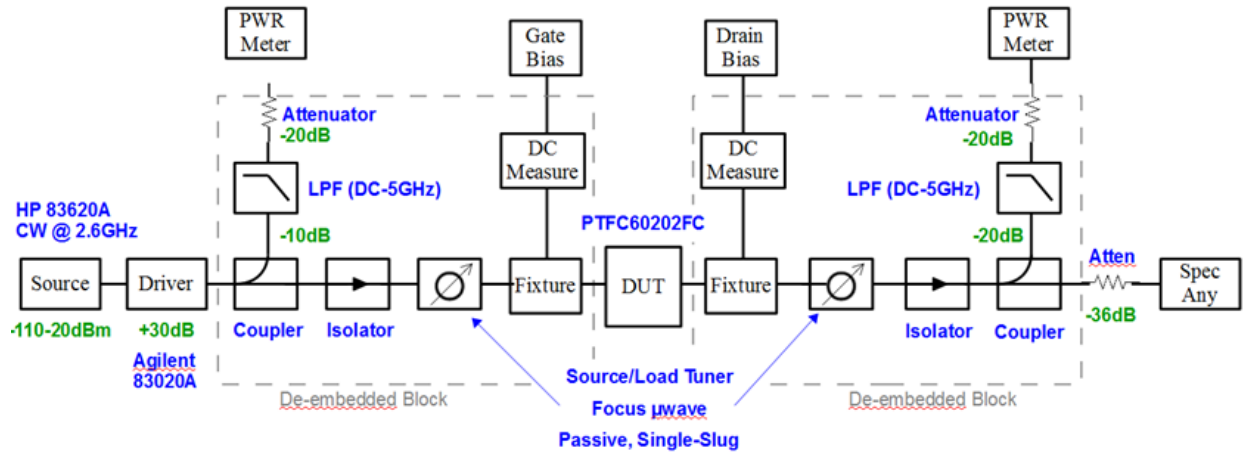
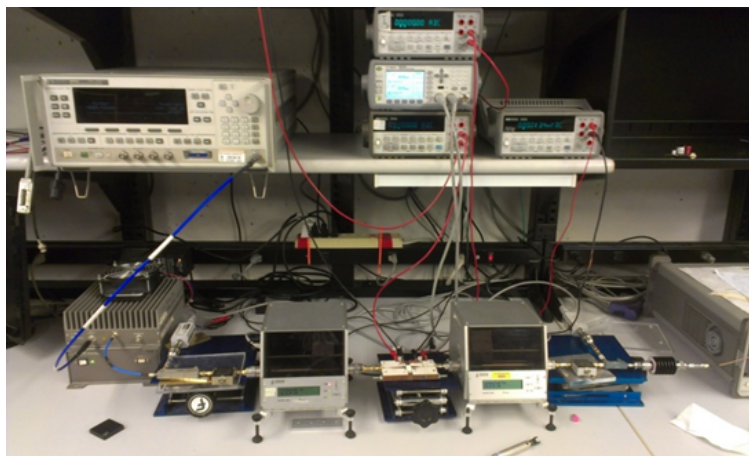
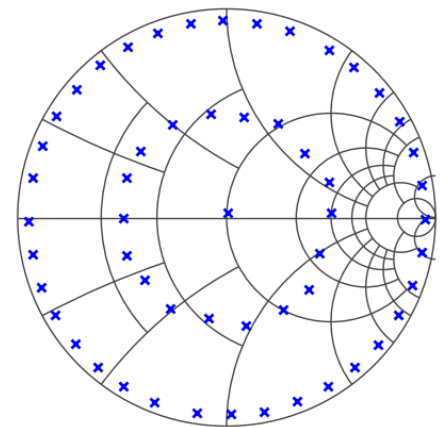


Figure 2.3: LP and SP measurement setup using fundamental-only passive single-slug Focus tuners, with capabilities for power, bias, and frequency sweeps. LP fixtures include a bias tee and transform 50-Ω line to a trace of width of package lead, and include a bias tee and a 2<sup>nd</sup> harmonic termination open-circuit stub on the load. Power meters measure fundamental power. The grey dashed line encapsulates the portion of the setup that is de-embedded, allowing measurement at the DUT reference plane.



(a)



(b)

Figure 2.4: Picture of the LP setup described in Fig. 2.3 (a). The LP constellation (55 points) is shown in (b).

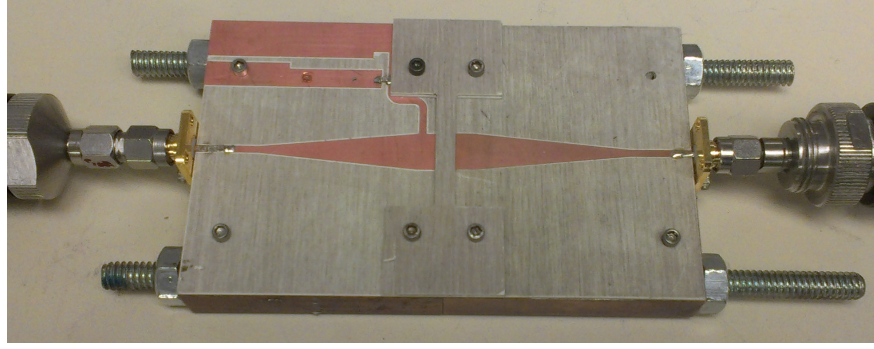


Figure 2.5: Fixtures used in load-pull to mount the device under test. The gap in the middle defines the reference plane of the package terminals. In the photo, the left side of this break-apart fixture includes the gate bias line. A similar circuit is made for the drain. The tapers without the bias lines serve as calibration standards to de-embed measurements to the package plane.

point using fundamental-only passive Focus Microwave single-slug tuners. The setup is shown in detail in Fig. 2.3. Shown in grey dashed line are the portions of the measurement setup that were de-embedded in order to obtain impedances at the package reference plane.

The device was placed in a fixture that tapered from  $50\ \Omega$  microstrip on Rogers 4350 30-mil substrate to the tab of the package. The fixture includes a broadband bias tee, with a gate resistor on the DC path for stability, Fig. 2.5. The setup allowed for a drive power sweep -25-30 dBm (or until 4-dB compression). The load-pull impedance constellation is shown in Fig. 2.4b, at the package lead reference plane, and on a 50-ohm Smith chart. The fixtures were de-embedded using TRL calibration.

The load fixture on the drain side includes an open-circuit microstrip stub to terminate the 2<sup>nd</sup> harmonic at an impedance indicated by simulation to correspond to the largest PAE. The source impedance was determined by setting the load to  $50\ \Omega$  and performing a LP for maximum gain, followed by a LP for maximum PAE, then another iteration of SP for maximum gain. The subsequent load-pull measurements were performed with the source impedance determined from this process ( $2.8 - 14j\ \Omega$ ).

With the load 2<sup>nd</sup> harmonic impedance fixed by a  $2f_0$  termination using an open-circuit microstrip stub, LP was performed for *PAE*. The corresponding  $P_{out}$ , gain, and *PAE* contours, at a fixed input power of 20 dBm, is shown in Fig. 2.6, with the performance versus swept input

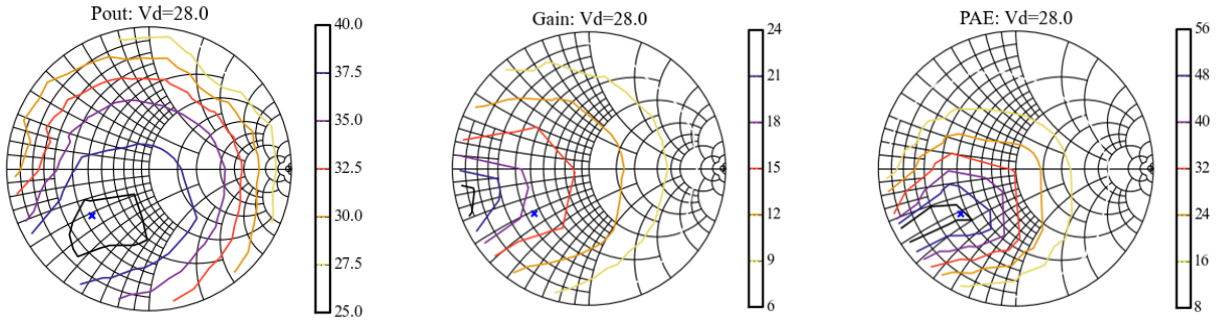


Figure 2.6: Measured LP contours for  $P_{out}$ , Gain, and  $PAE$  on  $50\text{-}\Omega$  Smith charts.

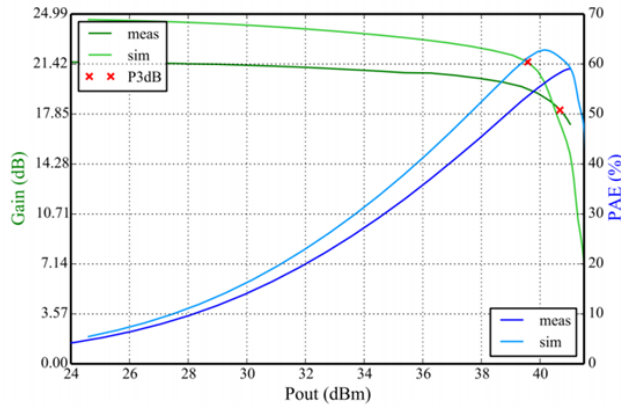


Figure 2.7: Measured drive-up curve with load impedance set to corresponding to the maximum  $PAE$  found from LP (Fig. 2.6).

power shown in measurement and simulation at the max  $PAE$  condition ( $PAE = 63.7\%$ ,  $P_{out} = 38\text{ dBm}$ ,  $Gain = 17\text{ dB}$ , at 4 dB compression with a load impedance of  $1.5 - 13.3j\ \Omega$ ) shown in Fig. 2.7. Up to 16% disagreement in the gain was seen between measurement and simulation with this non-linear model.

## 2.2 HARMONIC WAVEFORM SHAPING

The source of inefficiency in a power amplifier is the result of voltage and current overlapping in time across the transistor, where the dissipated power in one period is  $P = \int_0^T i(t)v(t)dt$ . An effective way to reduce the overlap of these time-harmonic waveforms, while also maintaining high output power, is to strategically add harmonic content to reshape the waveforms within the transistor.

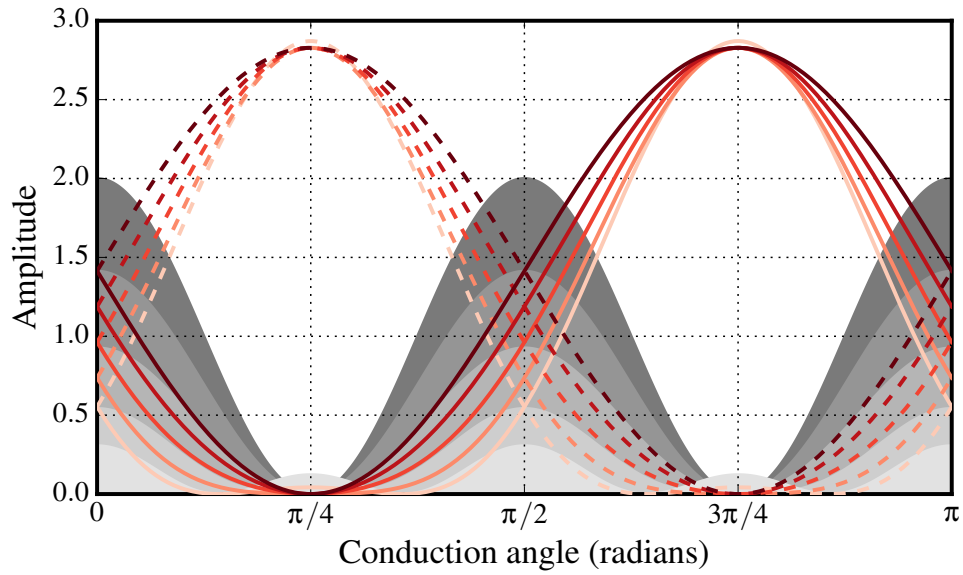


Figure 2.8: Two sinusoidal signals of same fundamental frequency with an amplitude of  $\sqrt{2}$  and offset by  $90^\circ$ . The waveforms in the darkest red do not contain any  $2^{nd}$  harmonic component. The shaded grey regions are the product of the two waveforms, showing the magnitude of overlap between them. As an increasing amplitude of  $2^{nd}$  harmonic is added to the waveforms, the overlapping grey region reduces. With the grey region representing power dissipated within a transistor and the waveforms relating to voltage and current normalized to class-A waveforms, this illustrates the reduced dissipated power by shaping waveforms with  $2^{nd}$  harmonic power.

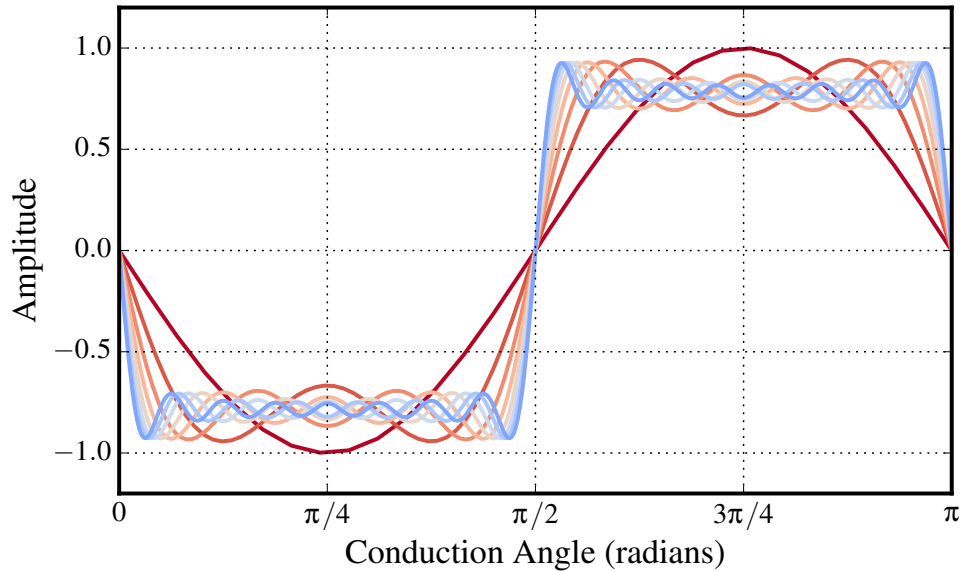


Figure 2.9: A purely sinusoidal signal (shown in red) with in-phase addition of an increasing number of odd harmonics to show the squaring of a waveform that can be used in waveform shaping classes of operation.

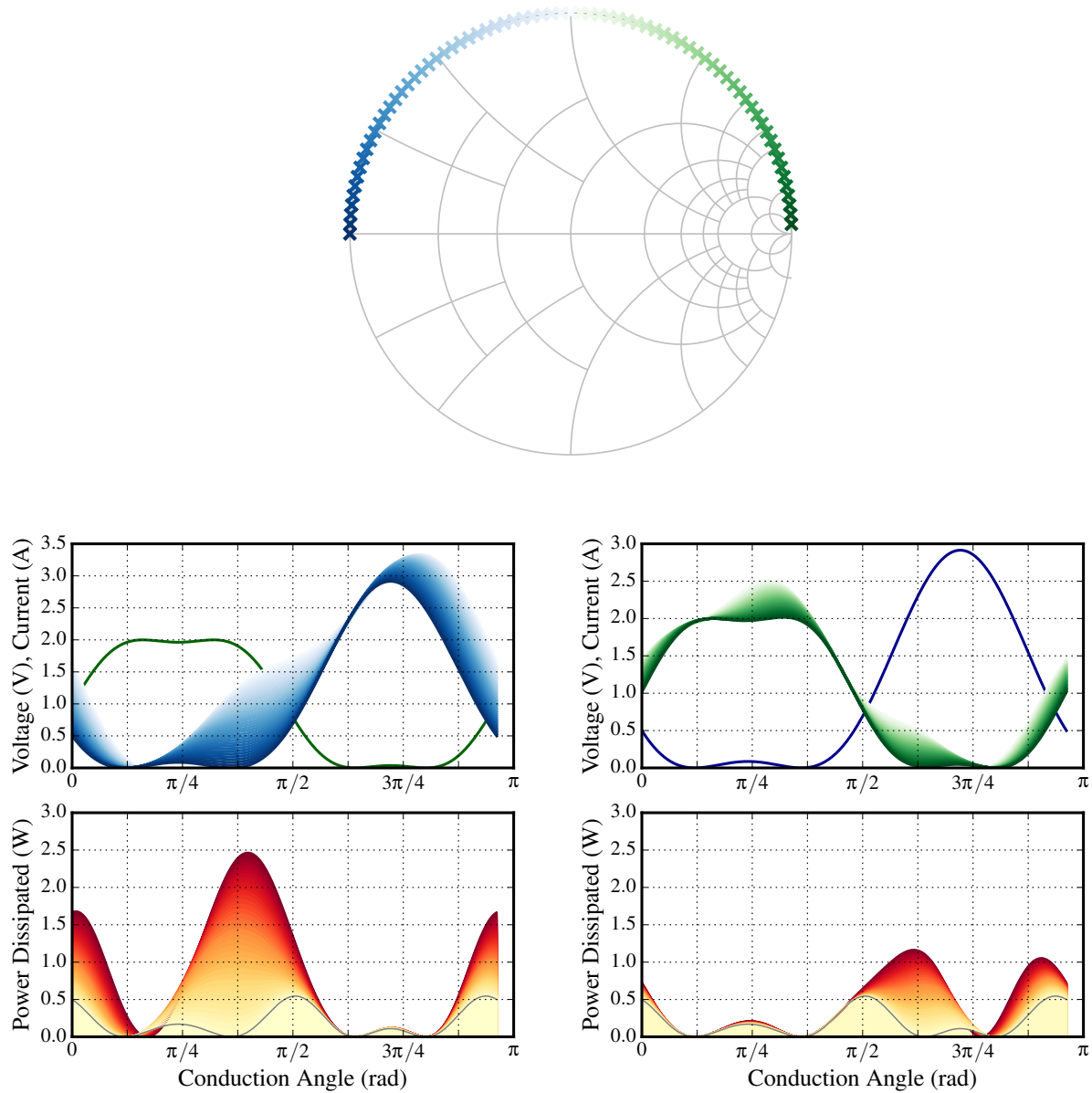


Figure 2.10: The effect of the shaped voltage (green) and current (blue) waveforms when the 2<sup>nd</sup> and 3<sup>rd</sup> harmonic are reflected out of phase with respect to the fundamental component. The optimum amplitude and phase of the harmonics which lead to the smallest degree of dissipated power [9] lead to the waveforms shown in the darkest green and blue, with the corresponding minimum dissipated power outlined in grey. The increasing overlap of voltage and current as the termination phase approaches 90° is shown in red, illustrating the need for precise harmonic phase reflections.

Consider two sinusoidal signals of the same fundamental frequency but offset by  $90^\circ$ , as shown in Fig. 2.8. In this figure, the  $2^{nd}$  harmonic is added to the waveforms with increasing amplitude. The resulting waveforms are shaped in such a way that the overlapping region is reduced. Another way to interpret this is less dissipation when  $2^{nd}$  harmonic power is injected.

Now consider that the  $2^{nd}$  harmonic power is not injected externally but instead generated by the transistor non-linearities when driven into compression at the fundamental. In this case, the harmonic waves are reflected by the output matching network and will either shape the current or voltage waveforms. For example, a  $3f_0$  open-circuit impedance will reflect  $3f_0$  voltage and shape the voltage waveform. By designing a drain network such that the  $2^{nd}$  and  $3^{rd}$  harmonic impedances present high-magnitude reflection coefficients of specific phase, high efficiency and output power can be achieved. Fig. 2.9 shows resulting waveforms from in-phase addition of odd harmonics. The closer the waveform is to a square wave, the higher the resulting efficiency.

It is interesting to observe the impact of the phase of the harmonic termination assuming it is a pure reactance. Fig. 2.10 shows the voltage in red and current in blue for a  $90$  degree change in harmonic termination phase from an ideal open/short to  $90$  degrees. The overlap between the two waveforms represents the dissipation indicating that only some harmonic impedances result in high-efficiency.

In order to achieve the proper shaping of the voltage and current waveforms, signal harmonics must add to the fundamental at a precise amplitude and phase. The impedance of the drain network which achieves the proper reflection of the harmonics is difficult to predict since it is dependent on non-linear parasitic reactances intrinsic to the device as well as parasitics presented by the network between the transistor fingers and the design plane. These parasitics are difficult to model accurately. Harmonic load-pull is a method for characterizing how harmonic impedances affect active device performance and is used throughout this work.

Harmonic load-pull is demonstrated in measurement on the same device previously characterized in fundamental load-pull. In lieu of tuners which can tune harmonic impedances independent of the fundamental, an open-circuit microstrip stub responsible for the termination of the  $2^{nd}$  harmonic



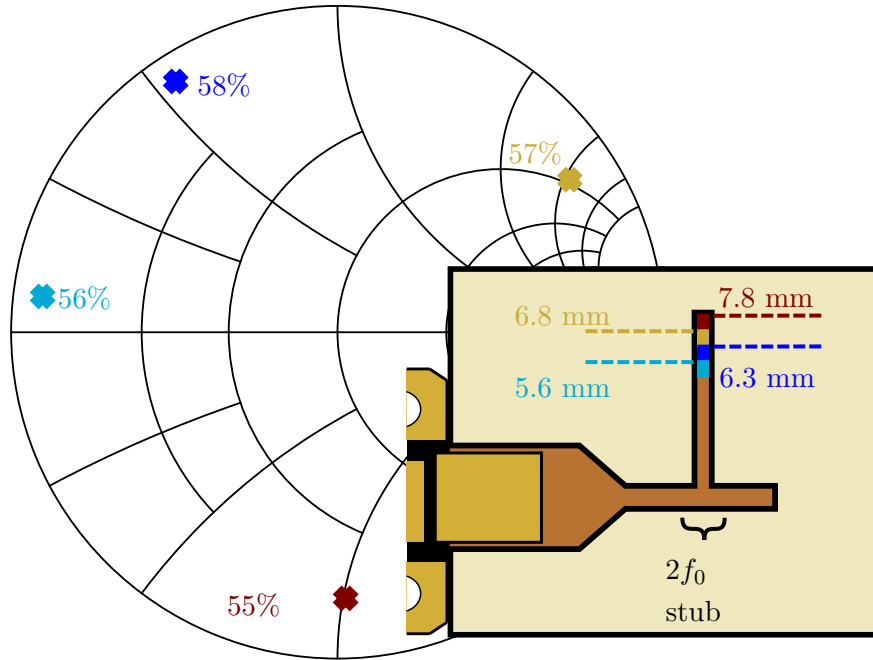


Figure 2.11: As a method for performing  $2f_0$  loadpull, 4 discrete  $2f_0$  impedances are presented to the package by varying the length of an open-circuit microstrip stub that is responsible for the phase of the  $2f_0$  termination. At each  $2f_0$  impedance (marked by an 'x' of color corresponding to the stub length labeled in the inset), an  $f_0$  loadpull is performed, and the maximum measured  $PAE$  is labeled by the corresponding cross.

impedance is tuned to 4 discrete lengths while  $\Gamma_{3f_0}$  is fixed (as done in [32]). The fixture is designed such that the length of this stub only affects the phase of the  $2^{nd}$  harmonic termination. The stub length is tuned by added copper tape to the end of the stub. For each of the 4 adjustments to the stub length, the fixture is measured and deembedded, and fundamental load-pull is performed. The resulting maximum  $PAE$  and corresponding  $\Gamma_{2f_0}$  for each case is shown in Fig. 2.11. These results motivate the need for in-package harmonic terminations since it can be seen that designing harmonic impedances beyond the package reference plane has little impact on PA efficiency.

### 2.3 OTHER MODELING AND CHARACTERIZATION APPROACHES

In addition to the load-pull described in Fig.2.3 with passive tuners, active load-pull systems are available that can present reflection coefficients larger than unity at the input and output of the device, at fundamental and harmonic frequencies. This is referred to as active load-pull [28].

In Chapter 4 of this thesis, an active harmonic load-pull system is used to validate non-linear simulations. In Chapter 6, the concept of active load-pull is used in the design of a PA which relies on an active  $2^{nd}$  harmonic termination.

The amplifier designs presented in this thesis also require careful passive circuit simulations beyond the highest harmonic frequency of interest. This includes full-wave simulations of components such as bond-wires, capacitors, transmission lines, packages. In this thesis, Ansys HFSS is mostly used for these types of simulations, as will be discussed in the following chapter.

In summary, this chapter overviews methods used for non-linear characterization throughout the thesis. Some limitations of non-linear models are highlighted as well as limitations of measurement-based technologies.

# 3

## PACKAGE MODELING

### CONTENTS

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2.3	OTHER MODELING AND CHARACTERIZATION APPROACHES . . . . .	20

The metal-ceramic packages that house high-power RF/microwave transistors are designed to be mechanically rugged and thermally efficient. The flange and the ceramic frame exhibit good thermal and mechanical properties, interconnects provide a transition of current from the active device to the package leads, and the package tab provides a conductor between the inside and outside of the package. From an electrical perspective, these structures constitute an electromagnetic environment that will affect the performance of the enclosed device. By understanding the package environment from an electromagnetic perspective, traditionally performance-limiting factors/parasitics can be used to the advantage of the active circuit design.

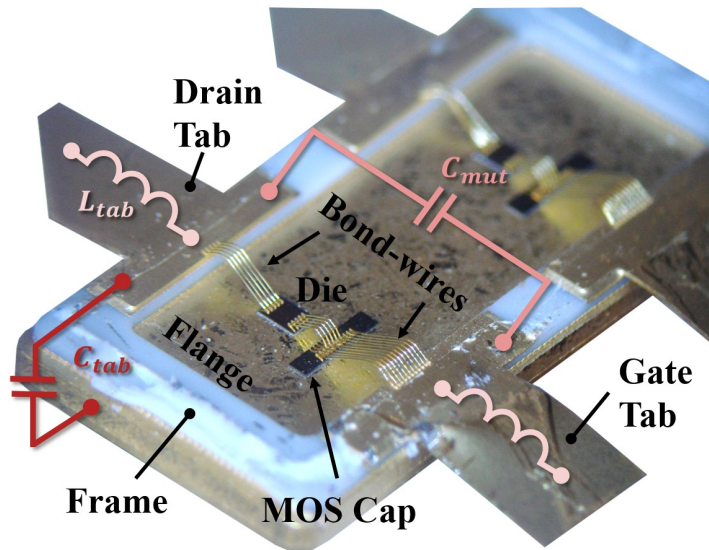


Figure 3.1: Commercially available packaged 10-W LDMOS power transistor showing the bond-wires that connect the gate and drain manifolds to the package lead via a shunt MOS capacitor that, together with bond-wire inductance, provides pre-matching at 2.6 GHz. The significant parasitic reactances, present in any metal-ceramic package, are labeled in various intensities of red corresponding to relative values of the parasitics.

### 3.1 PACKAGE MODELING

For high-efficiency PA design it is critical to be able to model the package environment accurately up to the highest harmonic of interest. Measurement-based approaches to package and in-package network modeling are commonly employed [33,34] however would require a large number of design iterations for networks that include harmonic terminations. Quasi-static methods can also be used to predict the impedance presented by in-package elements [35,36].

Full-wave simulations are necessary to properly model the geometrically complex nature of a transistor package. Of the 3D full-wave simulation algorithms, the Finite-Element Method (FEM) tools provide greater accuracy than available Finite-Difference Time-Domain (FDTD) tools for computational domains that include curved surfaces (such as those on bond wires) and inhomogeneous materials that are typically present within a transistor package [37]. Although FEM is more accurate and versatile than tMoM, it is more computationally demanding. This is of particular concern for modeling package networks since they consist of many (up to 100) individual elements

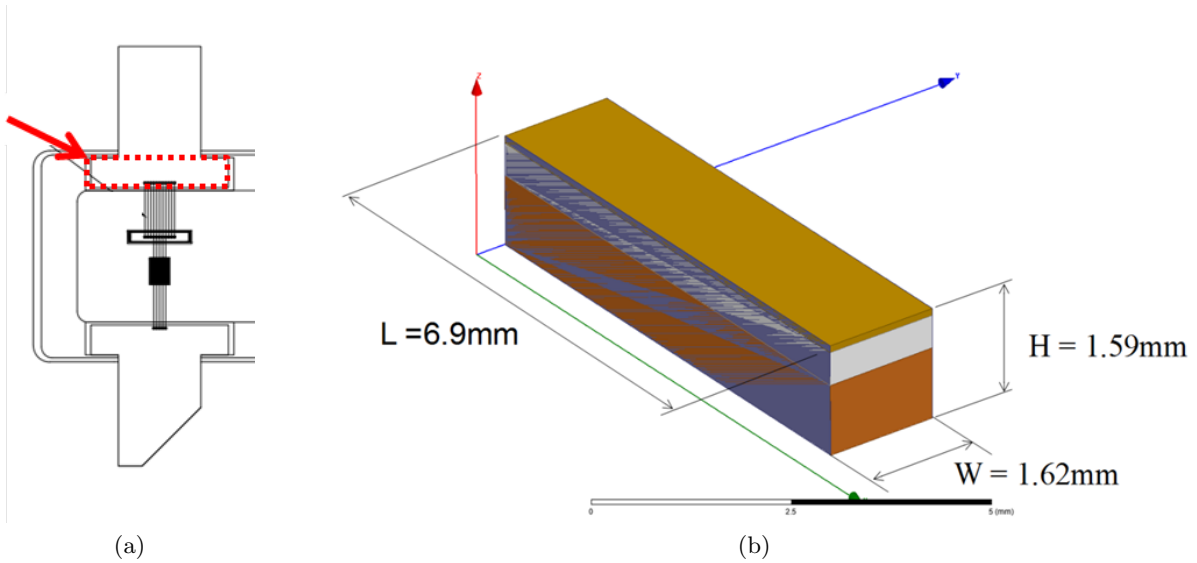


Figure 3.2: HFSS setup (b) of segment of package of H-37248-4 package where frame, lead, metalization, and flange overlap (a) shown by red dashed line.

(bond wires, capacitors, etc). An approach is developed in [38] in which package-internal matching networks are segmented into smaller portions and then appropriately combined.

In [37] it is shown that Finite-Element Method (FEM) is more accurate, especially at the harmonics of the than the Finite-Difference Time-Domain (FDTD) method or Method-of-Moments (MoM) considering the non-planar structures, curved surfaces of the bond wires, and inhomogeneous materials present within a package. The networks within a package can be very large and therefore computational time can be prohibitively long, in which case a technique to segment in-package networks is shown in [38, 39]. This work involves packages that only include a single die so distributed models are not necessary.

## 3.2 TAB CAPACITANCE

Under the assumption that the limited harmonic content output to the device is due to the parasitic capacitance presented by the device package, full-wave simulations are performed to understand the performance of the structure that houses the device. The segment of the commercial package in Fig. 3.7 where the frame, flange, metalization, and lead overlap was modeled in Ansoft HFSS (see

Fig. 3.2a).  $50\ \Omega$  lumped ports were placed between the long edges of this segment. The capacitance determined from  $Z_{21}$ , is compared to parallel-plate capacitance  $C_{gpad}$  due to the geometry, given by:

$$C_{gpad} = \frac{\epsilon A}{d} = 1.98\ \text{pF} \quad (3.1)$$

The capacitance extracted from HFSS simulations (Fig. 3.2) is found as:

$$C_{hpad} = \frac{1}{\omega \cdot \text{Im}\{Z_{21}\}} = 2.2\ \text{pF} \quad (3.2)$$

This corresponds to  $-jX_c(2f_0) = -j13\ \Omega$  and  $-jX_l(3f_0) = -j9\ \Omega$ , which are small impedances that will effectively short much of the harmonic power.

### 3.2.1 LUMPED CAPACITORS

Lumped capacitors are an essential element in transistor pre-matching. The capacitors are modeled throughout this work by the following: given a list of available MOS and single layer capacitors, a capacitor of desired value is chosen, and then are constructed in HFSS with the described dimensions for the given capacitor. The permittivity of the dielectric is then varied in HFSS until the extracted capacitance achieves the desired value. The HFSS setup includes this dielectric and top plate conductor atop the flange in an air box with radiation boundaries, with two lumped ports serving as the excitation. The loss tangent of the dielectric is assumed to be zero.

If HFSS lumped ports are parallel and close enough to each other, they can couple and simulate additional capacitance that is not physically present. It was seen that the electrical length between the ports was large enough to avoid this coupling. This was verified by placing a lumped port on

one side of the capacitor, and on the other side, extending the capacitor by a wavelength and de-embedding the added length. The simulated  $S$ -parameters for both cases were identical, indicating that the electrical length between the two lumped ports are large enough to avoid coupling between lumped ports, and therefore will be used since it is less time and computationally intensive than de-embedding waveports.

### 3.2.2 BOND-WIRES

It is of importance to model bond-wires in transistor packages, as they represent a significant and complex interaction of impedances. Simulated in HFSS was a straight PEC bond-wire of length  $l = 100$  mil, height from ground plane  $h = 4.35$  mil, and diameter of 2 mil to obtain the inductance  $L_{H_{wire}}$  (shown in Fig. 3.3a). This was compared to an analytical solution for a wire over a ground plane [40], defined as  $L_{G_{wire}}$ :

$$L_{G_{wire}} = l \left[ \ln \frac{4h}{d} + \ln \left( \frac{l + \sqrt{l^2 + d^2/4}}{l + \sqrt{l^2 + 4h^2}} \right) + \sqrt{1 + \frac{4h^2}{l^2}} - \sqrt{1 + \frac{d^2}{4l^2}} - \frac{2h}{l} + \frac{d}{2l} \right] = 1.06\text{nH} \quad (3.3)$$

$$L_{H_{wire}} = \frac{1}{\omega \cdot imY_{21}} = 1.16\text{nH} \quad (3.4)$$

An array of bond-wires were also simulated in HFSS and compared to measurement of the same array in [41]. The setup is shown in Fig. 3.3b, where the bond-wires land on a finite conductor boundary and excited by adjacent lumped ports. The measured inductances yields 0.22 nH, and full-wave simulated inductance yields 0.23 nH.

The parasitic associated reactances become relevant at higher frequencies, which was recognized in early theoretical work by Collin [42] and Grover [43] for simple inductance calculations. The partial inductance concept for an ‘‘open-loop’’ wire was discussed in [43] and [44], while [45] and [46] treat propagating modes on wires above substrates. Equivalent circuits based on quasi-static analysis (conformal mapping) are derived in [47], [48], and [49], with added FDTD in [50, 51], where 1-3 parallel bond wires connecting microstrip lines on substrates of different thicknesses are discussed theoretically.

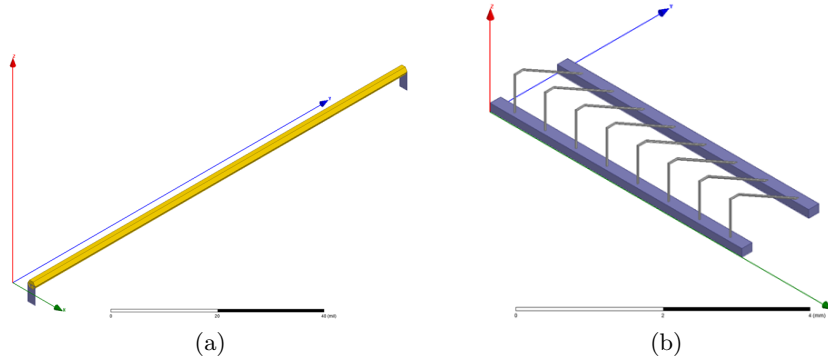


Figure 3.3: HFSS simulation of a straight PEC 100-mil bond-wire (a) and an array of bond-wires (b).

Multiple parameters may be used to affect bond-wire inductance. For a single bond-wire, geometric parameters such as those defined by JEDEC 5-point standard for modeling are commonly manipulated to achieve a certain inductance or interconnection. For multiple bond-wires, this becomes more complex. Work has been done to seek better formulations of mutual inductance by varying such parameters as wire length and angle [52]. The approach in [53] and [54] investigate non-parallel wires in terms of how the angle between multiple wires may be used to control current distribution and insertion loss.

In this work, motivated by the need to achieve precise impedance transformations in a space-limited semi-conductor package environment, the interaction of multiple bond-wires is examined in simulation. Bond-wire length, irrespective of wire profile, is an important design parameter as it has the most significant impact on inductance, and also will define its equivalent resistance and current handling capabilities. Bond-wire resistance,  $R_w$ , is defined in [40]:

$$R_w = \frac{4l}{\pi\sigma d^2} \left[ \frac{d}{4\delta} + 0.2654 \right] \quad (3.5)$$

where skin depth  $\delta = \sqrt{\frac{2}{\omega\mu\sigma}}$ , where  $l$  is the bond-wire length,  $\sigma$  is the metal conductivity, and  $d$  is the wire diameter. This resistance scales faster than inductance  $L$  as the length increases (as can be seen in Equation 3.4).

The consequence of larger  $R_w$  not only effects PA efficiency by virtue of dissipative loss, but it



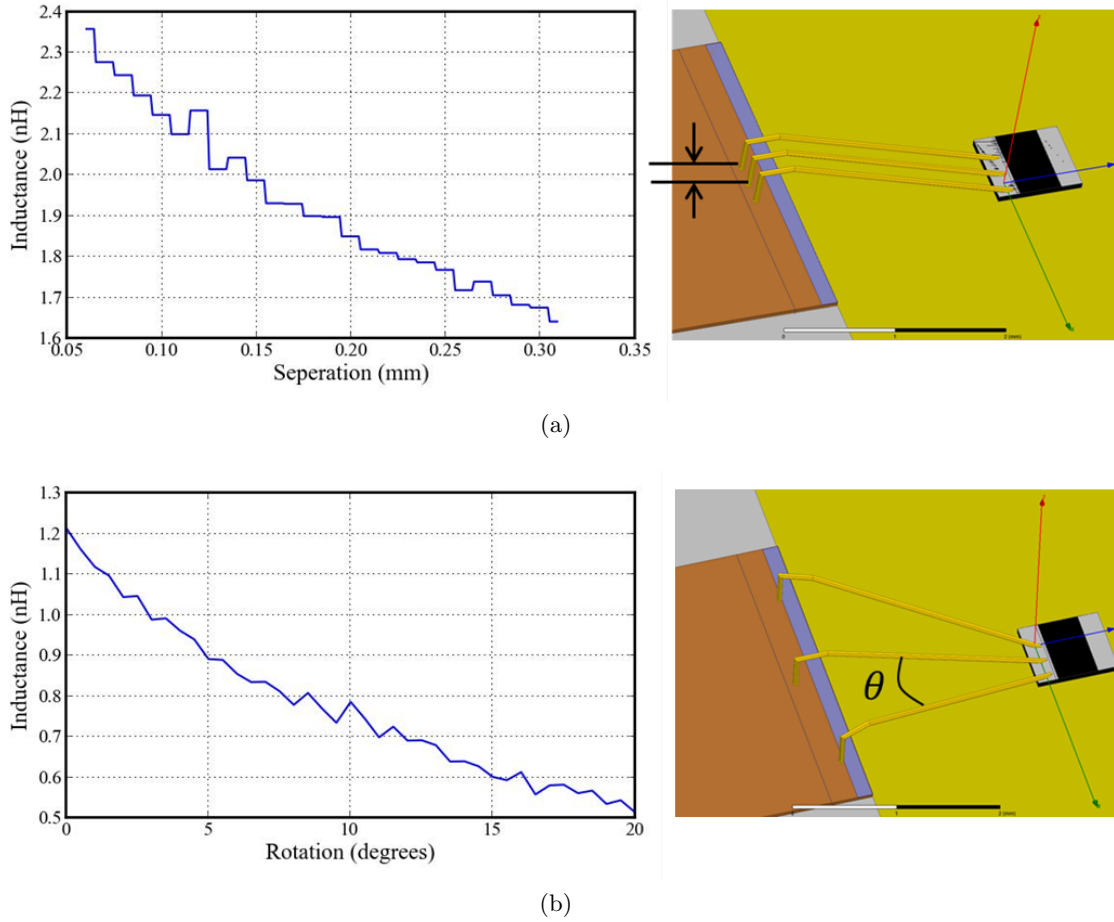


Figure 3.4: The equivalent series inductance of multiple bond-wires is examined in simulation by sweeping the (a) separation and (b) angle between wires.

will be shown in Chapter 4 to have a significant impact on harmonic impedances. Bond-wire length also affects the current handling of the wire, particularly with larger periphery devices. The fusing current  $I_f$ , or the current at which the wire will fail due to metallurgical failure, is defined as:

$$I_f = K d^{1.5} \quad (3.6)$$

where  $d$  is the wire diameter and  $K$ , dependent on wire material properties, is 183 for gold. For safety, half of  $I_f$  should be used as the maximum value of current. Longer wires will take a longer time to fuse than shorter wires. This max current does not depend on bond-wire profile.

Bond-wire radius can also be a useful design parameter. For example, as can be seen in Equations 3.6 and 3.5, smaller diameter wire, although at the expense of larger loss and lower current

handling, will allow a larger inductance for a given  $l$ .

In order to determine a typical range of inductances for bond-wires within a transistor package to better inform in-package design, a variety of bond-wire configurations (limited by the above constraints) were full-wave simulated using Ansys HFSS. The bond-wire profile, the number of bond-wires, and the separation distance and angle between them are varied. A subset of these configurations, shown in Fig. 3.5 are fabricated to test available practical geometries of a bond-wire within a package environment. It was then determined that bond-wire inductance within the circuit model for the given packages are restricted to a range of 0.1 - 1.5 nH. In addition to inductance, the bond-wire parasitic resistance is considered since it scales faster than the inductance with increasing bond-wire length [40].

### 3.3 LIMITATIONS OF COMMERCIAL PACKAGES

At RF/microwave frequencies, the package and package-internal elements (bond-wire interconnects, capacitors) will present some impedance. Package designers may intentionally design these elements to provide an impedance transformation from the low impedances of the active device to a higher impedance (around  $15\Omega$ ), allowing for easier design outside of the package. However, the effect of this impedance transformation at harmonic frequencies is not considered in commercial packaged devices. Without modeling and designing at harmonic frequencies, these commercial packages often present significant parasitic capacitances that short harmonic content. As a result, packaged transistors are significantly limited in the efficiency they can achieve.

The entirety of the passive environment package, including the package tab, package cavity, bond-wires, and capacitors, is simulated in HFSS. A waveport is defined as port 1 to excite a microstrip of the width of the package lead. Port 2 is defined by a lumped port at the edge of the die pad.

The impedance presented to the device by the commercial package as simulated in HFSS is plotted in Fig. 3.7. Notice that, at the fundamental, the package transforms a  $50\Omega$  environment to an impedance closer to the drain impedance of the device ( $4.1 + j11.4\Omega$ ). However at the  $2^{nd}$

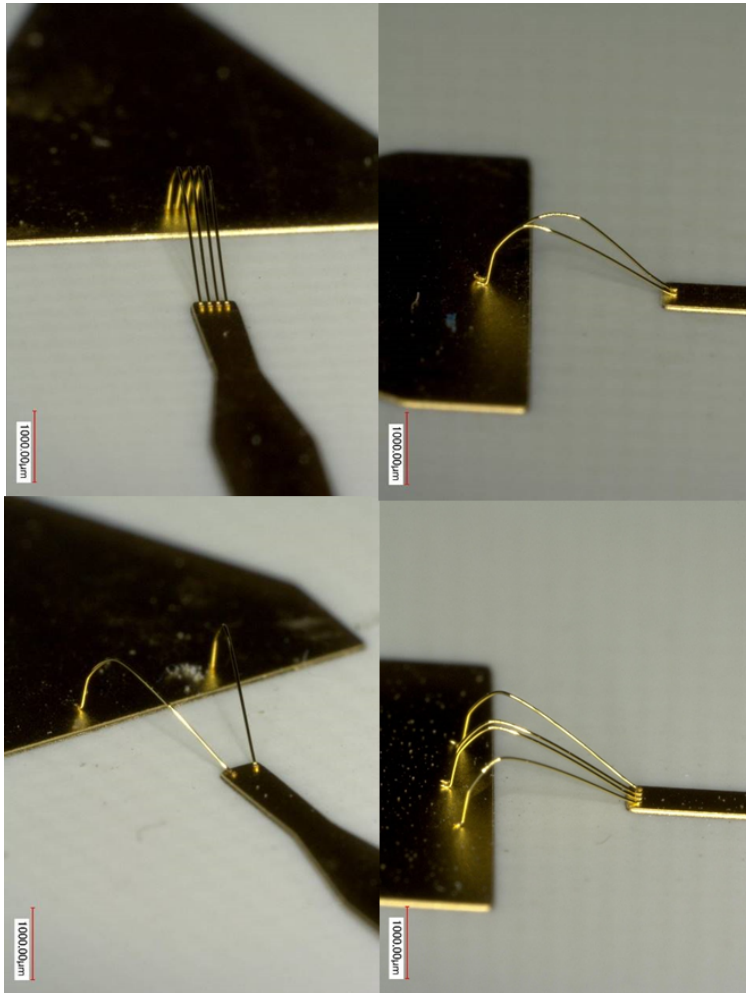


Figure 3.5: A variety of bond-wire profiles and configurations were simulated and fabricated to test available practical geometries.

and  $3^{rd}$  harmonic (2.6 GHz and 5.2 GHz respectively), this impedance is at the edge of the Smith chart which is undesirable for waveform shaping. The corresponding circuit model of the load-side network of the commercial package is shown in Fig. 3.8.

In summary, this chapter overview available lumped element components for in-package PA design. The analytical full-wave modeling necessary for accurate simulations of capacitances, bond-wires inductances, and resistances is validated. The circuit model of a package with such lumped elements is introduced, and design and validation is presented next.

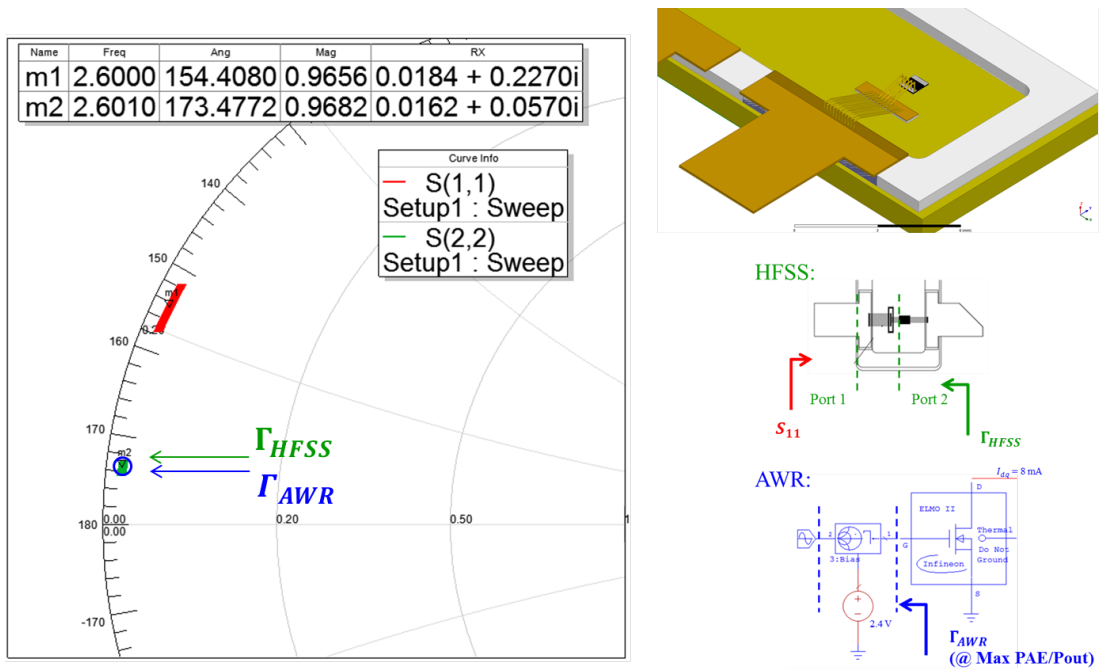


Figure 3.6: Simulation of the gate network of the commercial package from package lead to die plane, showing package pre-match ( $\Gamma_{HFSS}$ ). This is compared to the impedance determined from the non-linear model ( $0.8 + j2.85, \Omega$ ) of die that corresponds to max  $P_{out}$  ( $\Gamma_{AWR}$ ).

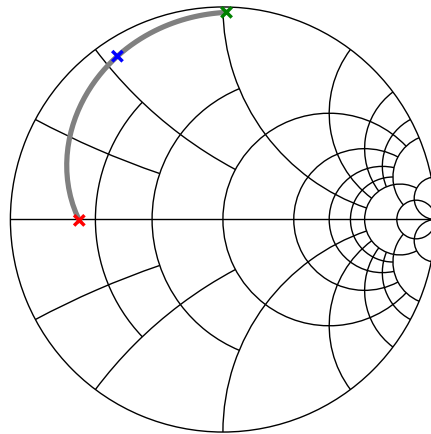


Figure 3.7: The HFSS simulated  $S_{11}$  of the load-side network package plotted in grey. Red, blue, and green crosses indicate the impedance at corresponding to  $f_0$ ,  $2f_0$ , and  $3f_0$  respectively.

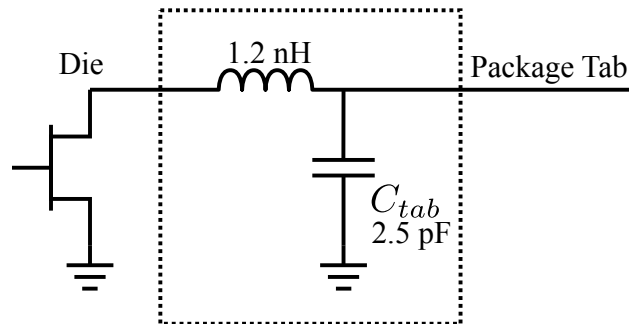


Figure 3.8: The HFSS simulated  $S$ -parameters of the load-side network (dashed line) of the commercial package are fit to a circuit model, with determined element values shown.

# PACKAGE DESIGN AND VALIDATION

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Designing in-package matching networks is challenging due to the volume-limited package environment. It is possible for a package to house quasi-TEM transmission line matching networks, however doing so would require very high permittivity substrates that would be too cost-prohibitive for many applications. The matching network must then be realized with bond-wires, capacitors, and the parasitics of the package. Therefore the network is restricted to a small set of topologies where the equivalent circuit elements are in turn limited in value. In this chapter, the network limitations are determined and presented, along with solutions to the issue of large package parasitic capacitances.

Certain elements, such as the device drain capacitance and the package parasitics, are fixed to values determined from the non-linear characterization techniques discussed in the previous chapter. The rest of the elements in the package equivalent-circuit model are designed in such a

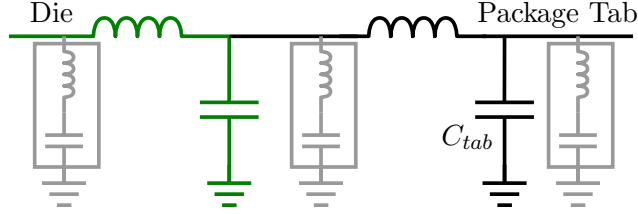


Figure 4.1: The in-package network topology for gate and/or drain, with the lowest complexity shown in black. The network can be extended to a  $2^{nd}$ -order low-pass filter with the possibility of higher orders for larger packages. A series shunt tank circuit (shown in grey) can be placed at each node if higher complexity is needed. The tab capacitance  $C_{tab}$  is fixed for a given package geometry.

way as to present desirable harmonic impedances for high-efficiency PA design. Such a design involves iteration between the circuit model, 3-dimensional bond-wire and capacitor design, full-wave simulations, and harmonic balance simulations.

The design methodology is first demonstrated on a package design that presents a pre-match at the fundamental and  $2^{nd}$  harmonic, which is measured and validated by multi-harmonic active load-pull. Next, multiple harmonically-terminated packages are designed to demonstrate in-package highly-reflective, precisely phased  $2^{nd}$  harmonic terminations. The chapter concludes with a technique to validate package designs and models to beyond the  $3^{rd}$  harmonic.

The  $L$  and  $C$  values in Fig. 4.1 are limited by practical considerations. The capacitances are limited to a list of fixed values and dimensions, as well as placement and orientation within a given package geometry. The size of the package and the die placement limits bond-wire length. The bonding machine limits the minimum distance between bond-wires, therefore limiting mutual inductance. Additionally, the 3-dimensional shape of the bond-wire cannot be arbitrary. Beyond the physical and practical limitations, one must also be aware of the electrical considerations. Lower inductances are desirable since they are realized by shorter and parallel bond-wires which in turn reduces insertion loss, increases current handling, and avoids the need for larger packages. However, generally speaking, large inductive reactances are often required to compliment the significant package capacitive reactances in order to increase harmonic impedances.

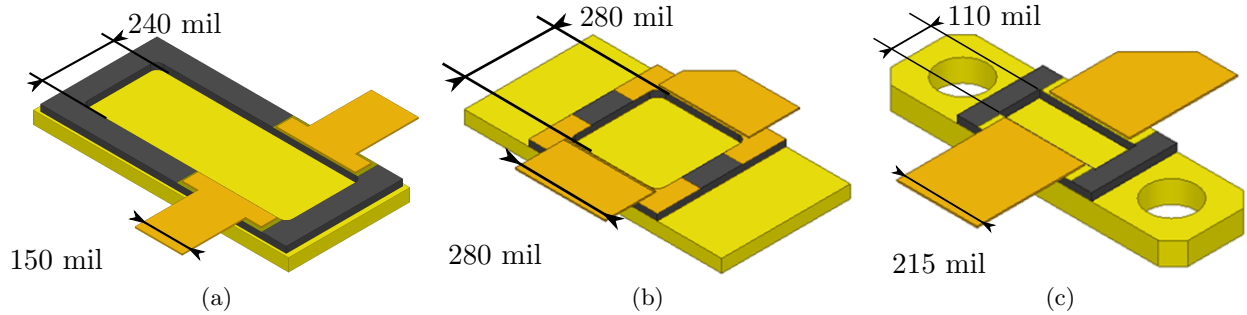


Figure 4.2: Transistor package 240 (a), package 280 (b), and package 110 (c), named for the length in mils between gate and drain tabs.

Table 4.1: Circuit element values for the three circuits in Fig. 4.3.

	$L_2$	$C_1$	$L_1$	$L_0$	$C_0$
<b>Circuit (a)</b>	0.3-1.5 nH	-	-	-	-
<b>Circuit (b)</b>	1.1 nH	0.3-1.5 pF	1.1 nH	-	-
<b>Circuit (c)</b>	1.2 nH	4.0 pF	1.0 nH	0.3-1.5 nH	0.3 pF

## 4.1 IN-PACKAGE MATCHING TOPOLOGIES

In order to provide a fundamental pre-match as well as harmonic terminations, a more complex topology may be necessary, with desirable independent control of the fundamental and its harmonics, as well as a large range of realizable impedances. Given lumped-capacitor and bond-wire inductor matching elements, several  $T$  and  $\pi$  circuit topologies are considered, as illustrated in Fig. 4.3. The range of impedances that can be presented outside of the package is simulated for different topologies and values of  $L$  and  $C$ , keeping  $C_{tab}=1.8$  pF. For these simulations, the tuner reflection coefficient magnitude is constrained to 0.4 and Table 4.1 gives the range of element values.

The simplest commonly used topology is a single series inductor, with the intention to tune-out the tab capacitance, Fig. 4.3a. The range of fundamental impedances that can be achieved is sufficient to match to a typical high-power transistor, however the  $2^{nd}$  and  $3^{rd}$  harmonic impedances are limited and cannot be adjusted independently. The simplest extension is the addition of a shunt capacitor  $C_1$  which requires an additional bond-wire, resulting in an inverter circuit (Fig. 4.3b). For this case, the fundamental match does not vary significantly and the  $2^{nd}$  and  $3^{rd}$  harmonic impedance can be controlled independently from the fundamental and over a wide complex range.



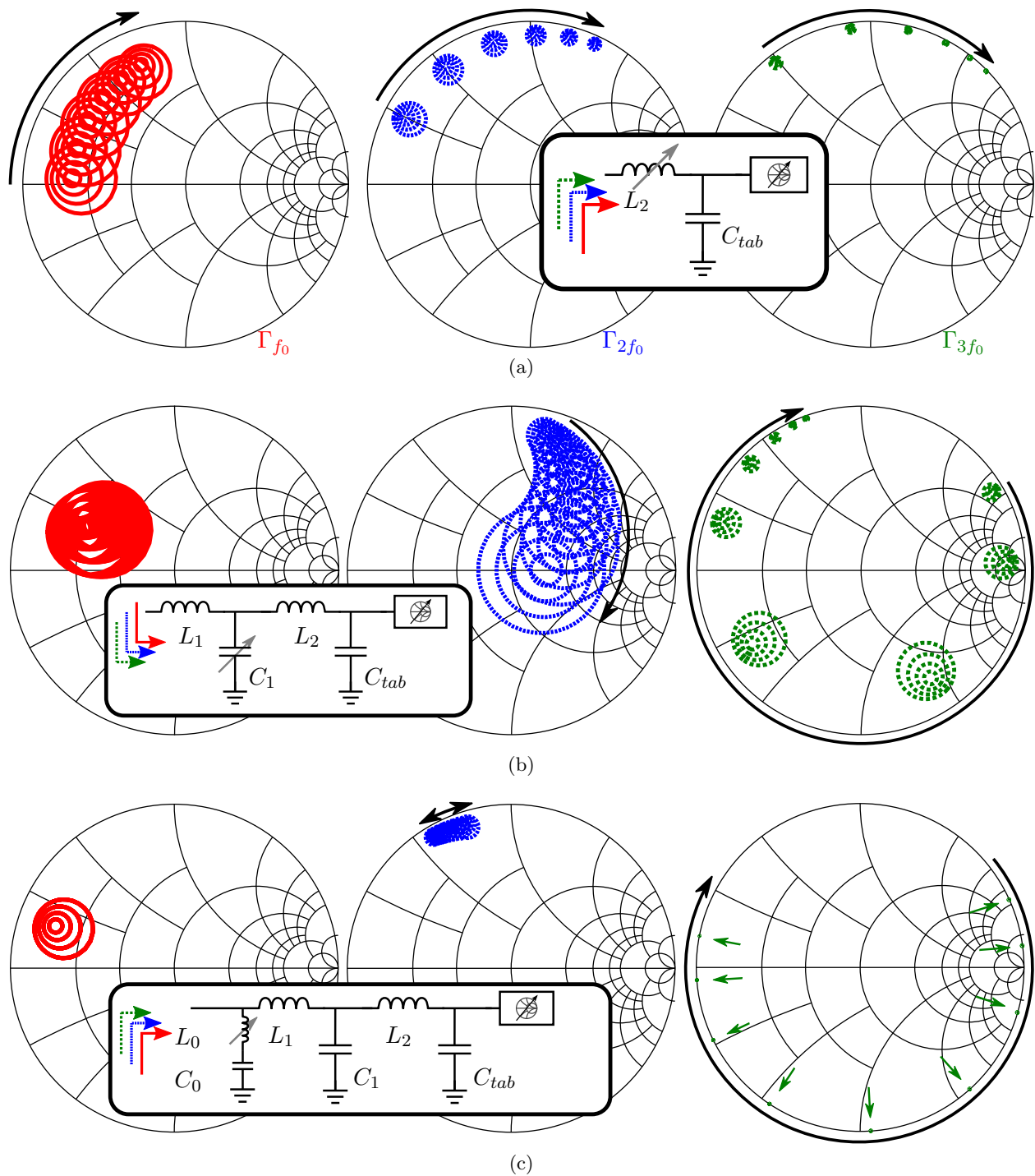


Figure 4.3: Impedances presented at the package output reference plane at the fundamental (red), 2<sup>nd</sup> (blue), and 3<sup>rd</sup> (green) harmonics when a single element of the network is varied according to Table 4.1. (a) Single series bond-wire, (b) *T*-network with a shunt capacitor, and (c) *T*-network with additional shunt resonator. The tuner reflection coefficient is limited to 0.4 in this example.

In Fig. 4.3c, a shunt  $LC$  network is added to independently control the  $3^{rd}$  harmonic over a large range of the Smith chart by varying only the resonator inductor  $L_0$ , while keeping the fundamental and  $2^{nd}$  harmonic impedances approximately fixed.

## 4.2 IN-PACKAGE HARMONIC TERMINATION FIDELITY

This section discusses how to achieve a sufficiently high reflection coefficient magnitude, or fidelity, of a harmonic termination within a package when the designer is limited to bond-wires, discrete MOS capacitors, and significant parasitic capacitances. A high-fidelity termination can be achieved with a shunt resonant  $LC$  network consisting of a bond-wire in series with a MOS capacitor. At resonance, the  $LC$  network presents a small impedance equivalent to the sub- $\Omega$  resistance of the bond-wire, which is a sufficiently high fidelity termination for waveform shaping. However, for terminations other than a short-circuit, the sub- $\Omega$  bond-wire loss can significantly limit termination fidelity since bond-wire inductances are limited to small values and depend on geometric profile. The degradation in harmonic termination fidelity due to bond-wire loss can be reduced by increasing bond-wire inductance at the expense of current handling and feasibility. The following section will further analyze this tradeoff in order to inform the design process.

For high-efficiency operation, it is useful to be able to present not only short-circuit termination but also an open-circuit. This is achieved within a package by a shunt  $LC$  resonator, and an impedance inverter realized by series  $L$  and shunt  $C$  network to transform the short to an open at the virtual drain. Consider the circuit shown in Fig. 4.4 where a shunt resonator can be designed to provide a short-circuit and the  $L_x, C_x$  network can be designed to transform the short to an open at the input of the network. At resonance, the imaginary component of the resonator impedance becomes zero, simplifying the impedance to  $R_{L_a}$ , i.e., the loss of the resonator bond-wire.

The  $L_x$ - $C_x$  network can be modeled as a transmission line with characteristic impedance  $Z_x = \sqrt{L_x/C_x}$ . The values of  $L_x$  and  $C_x$  can be chosen to create a lumped-element equivalent of a  $\lambda/4$  transmission line. In this case, the input impedance of the circuit is defined as  $Z_{in} = Z_x^2/R_{L_a}$ .

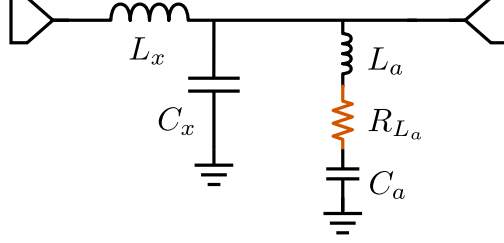


Figure 4.4: Lumped-element circuit model of an in-package open-circuit termination. At resonance, the shunt  $LC$  network presents a short-circuit to be transformed to an open-circuit by the impedance inverter formed by  $L_x$  and  $C_x$ . The resonator bond-wire loss is modeled by  $R_{L_a}$ .

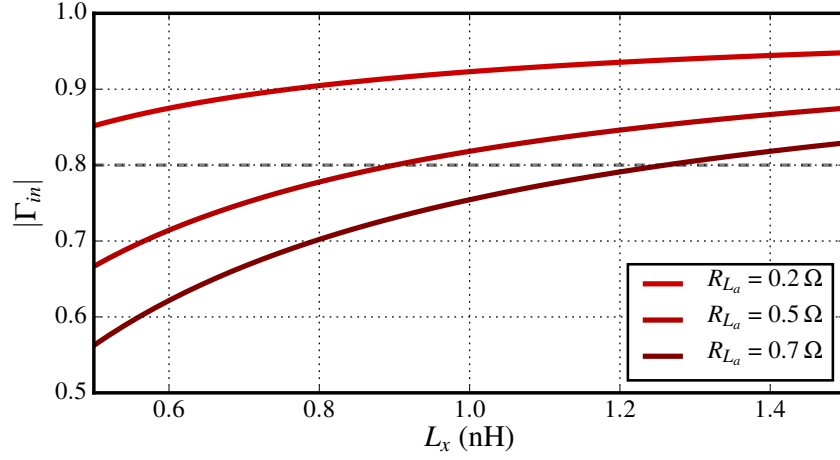


Figure 4.5: The reflection coefficient magnitude of the harmonic termination in Fig. 4.4 is plotted for a range of values for  $L_x$  and 3 different cases of resonator bond-wire loss. The  $|\Gamma| \geq 0.8$  condition to maintain reasonably high efficiency is plotted in dashed gray as a guideline for the trade-off between series bond-wire current handling and achieving sufficiently high termination fidelity.

Under the assumption that the bond-wire  $L_a$  is lossless ( $R_{L_a}=0$ ), any choice of  $L_x$  and  $C_x$  will provide an infinite impedance, as long as the network satisfies the conditions for an impedance inverter. However, with a non-zero  $R_{L_a}$ , the magnitude of  $Z_{in}$  is largely limited by the magnitude of  $Z_x$  and, consequently, the value of  $L_x$ . The larger the inverter inductance, the less of an impact the resonator losses will impact termination fidelity. However, bond-wires present a limited inductance, further limited for PA applications where current handling must be considered.

The fidelity of the harmonic termination is related to  $L_x$  in Fig. 4.5 for 3 different values for  $R_{L_a}$ . Although the magnitude of the termination is ultimately limited by the resonator bond-wire

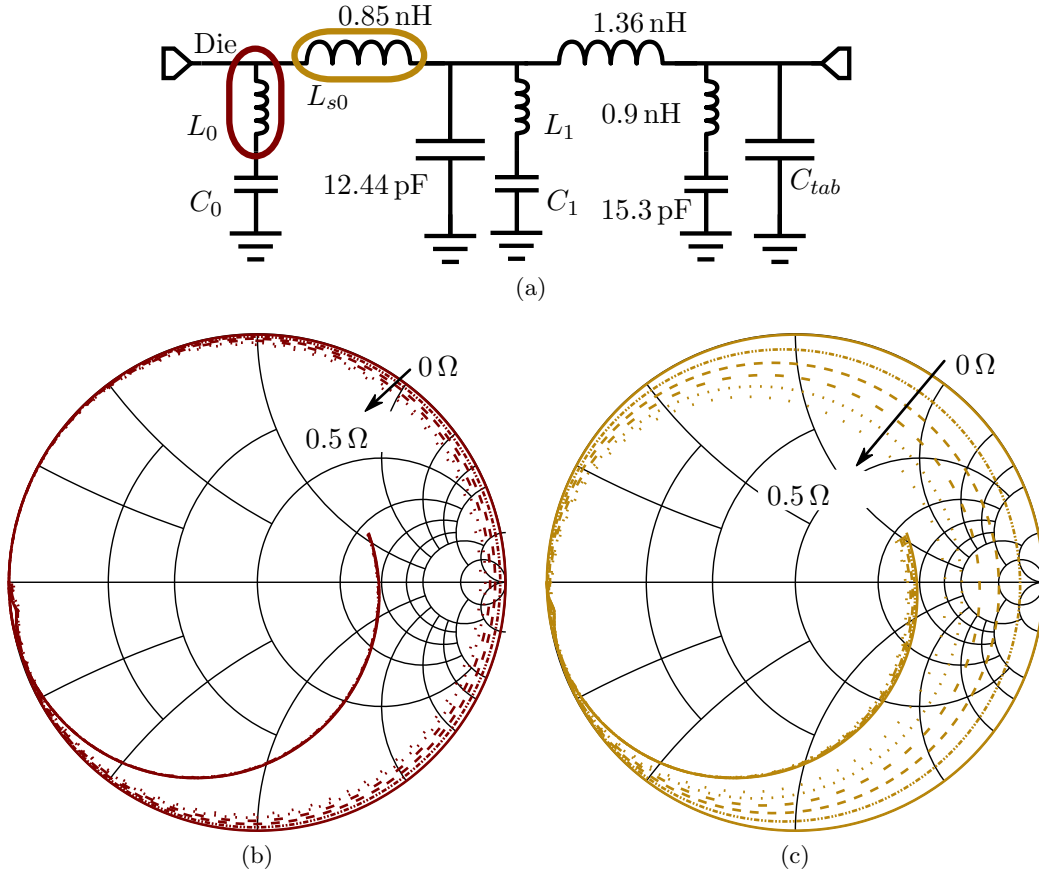


Figure 4.6: (a) An ideal lumped-element Class- $F^{-1}$  in-package matching network, with shunt the  $L_0C_0$  and  $L_1C_1$  resonators serving as the  $3f_0$  and  $2f_0$  termination, respectively. The values for the resonators are listed in Table 4.2 for 3 different cases. The impedance presented to the die, using the *compromise* case values, is plotted with resistance increasing from 0 to  $0.5\ \Omega$  in  $0.1\ \Omega$  steps for bond-wire  $L_{s0}$  (b) and  $L_0$  (c)

loss, the sensitivity of the termination to the loss can be reduced by increasing  $L_x$ . In practice this may be difficult since it is a series bond-wire and therefore must seek high current handling, which would dictate a lower  $L_x$  in order to allow multiple parallel bond-wires at this node.

A reasonably high efficiency can be achieved for a harmonically-terminated PA as long as  $|\Gamma_L(2f_0)| \geq 0.8$  [55], providing a guideline for the trade-off between bond-wire inductance and current handling, and harmonic termination fidelity. This condition is plotted in Fig. 4.5 by a gray line. By understanding the role of the inverter impedance on harmonic termination fidelity, one can seek a trade-off between termination fidelity and bond-wire inductance/loss.

The bond-wire resistance of the inverter additionally restricts the reflection coefficient magnitude of the open-circuit termination. Consider an example class- $F^{-1}$  drain network shown in Fig. 4.6, where a  $2f_0$  open and  $3f_0$  short are presented to the virtual drain. The  $L_0$ - $C_0$  and  $L_1$ - $C_1$  resonators are responsible for the  $3f_0$  and  $2f_0$  terminations, respectively. In this example, the loss of the  $L_{s0}$  and  $L_0$  bond-wire is swept from 0 to  $0.5\ \Omega$  and the resulting network input impedance is plotted. The increased resistance on the  $L_0$  bond-wire (responsible for the  $3f_0$  short) does not affect the  $3f_0$  termination. A resistance of  $0.5\ \Omega$  on  $L_{s0}$  reduces  $|\Gamma_{2f_0}|$  from 1.0 to 0.6. Even a modest resistance of  $0.2\ \Omega$  significantly degrades the fidelity of the termination. This illustrates how certain network designs, although at this stage seem to present the desired impedances while abiding by the previously described constraints, must consider realistic losses introduced by realizing the desired inductances with lossy bond-wires in order to inform possible redesign.

### 4.3 HARMONICALLY PRE-MATCHED PACKAGE

An intermediate step to full in-packing matching network design is to enable effective harmonic terminations outside of the package. For this demonstration, the package in Fig. 4.2c is considered because it is sufficiently large but has a small tab capacitance. Since only pre-matching is performed, and because of the space constraint, the simple topology from Fig. 4.3b is selected, as shown in Fig. 4.7. A circuit is designed to pre-match both fundamental and 2<sup>nd</sup> harmonic, enabling harmonic load-pull with sufficient flexibility of the  $2f_0$  constellation.

Load- and source-pull simulations with a non-linear model of the die determine the  $f_0 = 2.6\ \text{GHz}$  and  $2f_0$  impedances for maximum  $PAE$  at Class-AB bias ( $V_d = 28\ \text{V}$ ,  $I_{dq} = 85\ \text{mA}$ ). The target load and source-pull impedances are close to each other in this case,  $Z_L(f_0) = 4.4 + j11.8\ \Omega$  and  $Z_S(f_0) = 4.2 + j2.9\ \Omega$ , and the same ideal circuit model is first designed for both sides by iterating between full-wave HFSS and circuit simulations. The circuit transforms a tuner constellation at the fixture plane to a value closer to the target source and load fundamental impedances shown with a black cross in Fig. 4.8. The simulation constellation in Fig. 4.8 shows the die plane impedances at

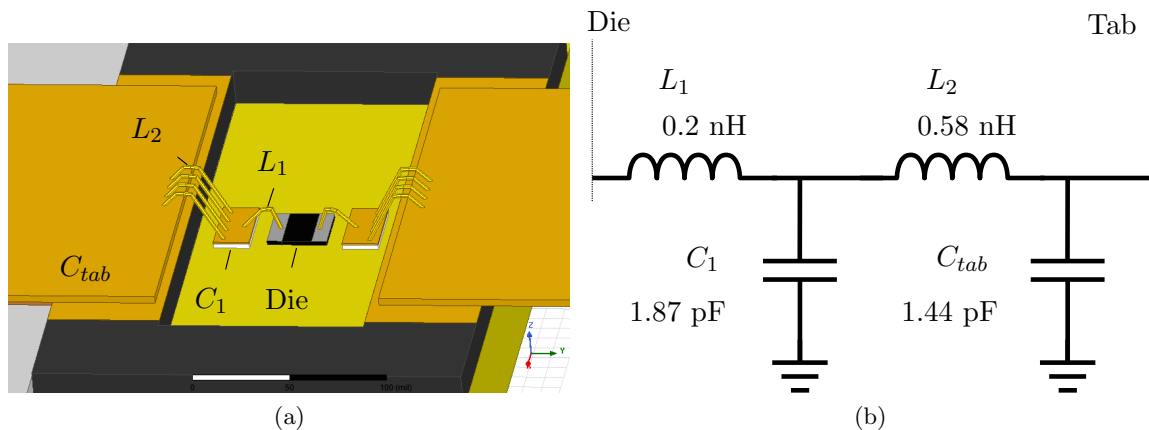


Figure 4.7: Harmonic pre-match package layout as simulated in HFSS (a) and the equivalent circuit at both the gate and drain (b).

Table 4.2: Three cases for harmonic resonator values

	$L_0$	$C_0$	$L_1$	$C_1$
L-dominant	11.73 nH	0.24 pF	26.38 pF	0.24 pF
C-dominant	0.20 nH	14.07 pF	0.20 nH	31.66 pF
Compromise	1.38 nH	2.02 pF	0.69 nH	8.67 pF

$f_0$  and  $2f_0$ .

A multi-harmonic passive loadpull was performed to obtain the contours shown in Fig. 4.9. Good agreement is seen with simulations, indicating the package presents the expected impedance to the die. A peak  $PAE = 63\%$  is measured at the package plane, a 4 point increase compared to the same die in the commercial package. Note that the  $2f_0$  loadpull contours of this pre-matched package show a greater impedance range for achieving a high  $PAE$  when comparing  $2f_0$  load-pull the commercial package (Fig. 2.11).

#### 4.4 HARMONICALLY-TERMINATED PACKAGE DESIGN

The technique discussed in the previous section is applied to design packages in which the 2<sup>nd</sup> harmonic impedance presented to the 10-W LDMOS die is of high magnitude and precise phase, and is controlled independently from the fundamental matching network. Five packages are designed (A-E) with the same fundamental pre-match but different 2<sup>nd</sup> harmonic impedances, shown in Fig.

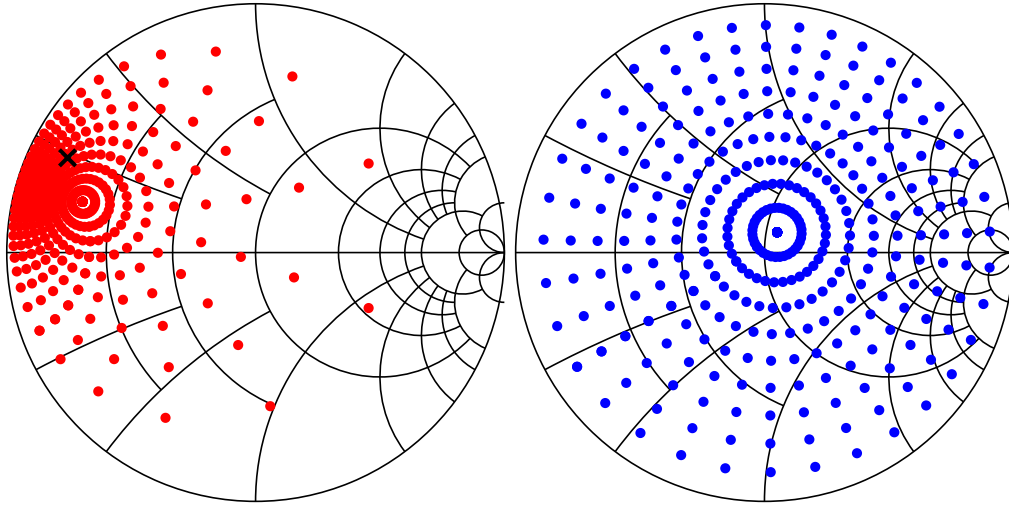


Figure 4.8: Simulated  $f_0$  and  $2f_0$  tuning range at die reference plane, considering both the LP fixture (simulated in Axium) and the package including in-package network (simulated in HFSS). The black 'x' on the  $f_0$  Smith chart indicate the max PAE impedance as determined in simulated LP for this die.

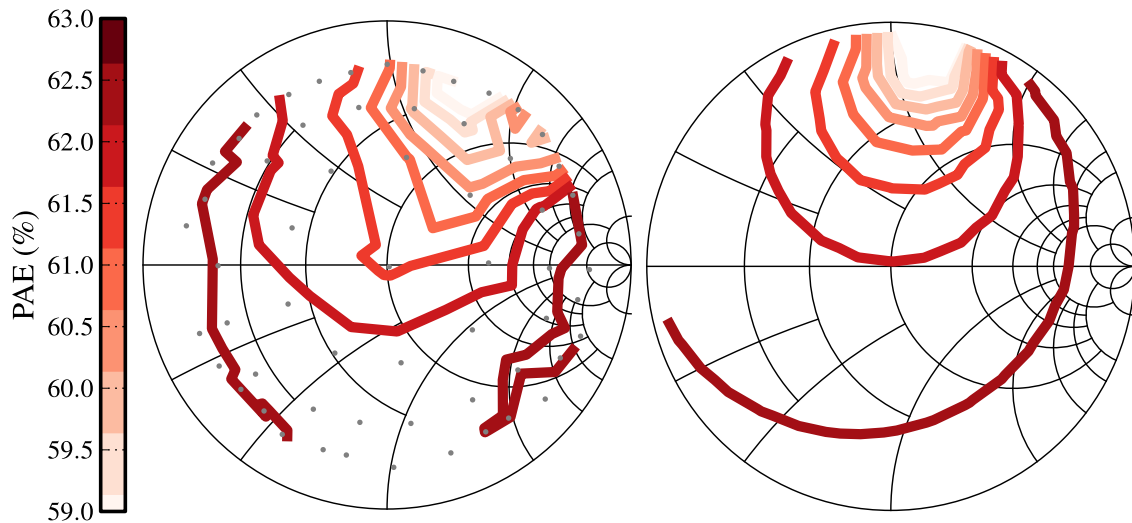


Figure 4.9: Measured (left) and simulated (right) loadpull contours at  $2f_0$  on  $17\Omega$  Smith charts, referenced at the package reference plane. Measured load tuner impedances are shown in grey.

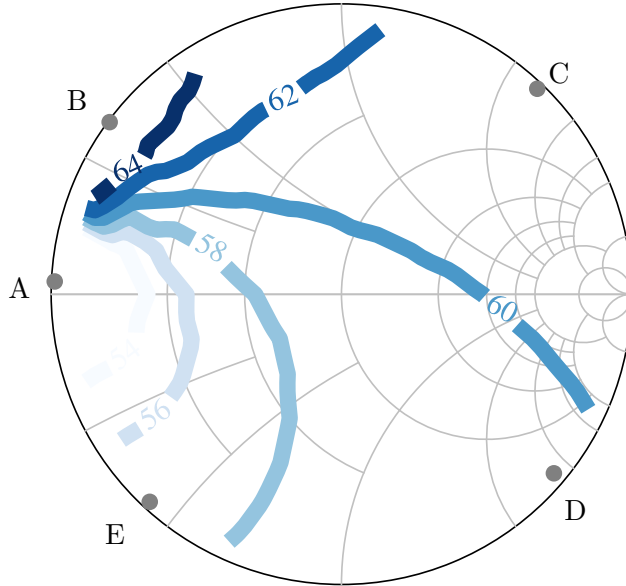


Figure 4.10: Simulated  $PAE$  load-pull contours at  $2f_0$  for the 10-W LDMOS device at the die reference plane at 2.6 GHz. The  $2f_0$  terminations for each of the 5 package designs are indicated by the grey dots (A-E).

4.10 together with simulated  $PAE$  contours at  $2f_0$ . The fundamental impedance is fixed to provide a prematch to the simulated load-pull value of  $Z(f_0) = 7 + j5 \Omega$ .

The package design flow is as follows:

- A standard package (for example, that of Fig.6(b)) is first chosen with dimensions that can accommodate higher-order filter designs, but do not require long bond-wires with excessive loss.
- Full-wave HFSS simulations are performed to determine the package parasitics as shown in Fig.3.1. For the package in Fig. 4.2b, the value is 5.6-pF, with a mutual capacitance between the leads of 0.1 pF. The latter has an impact on  $S_{21}$  at the harmonic frequencies.
- The MOS capacitor dielectric loss is extracted as a resistance, in this example  $R_{diel} = 0.2 \Omega$ .
- Starting from the fundamental and harmonic load and source-pull device impedances obtained from the device model (points A through E in Fig. 4.10 for the 2<sup>nd</sup> harmonic), realizable values of bond-wire inductances (0.2 to 3 nH) and available MOS capacitors (0.24 to 8 pF), ideal gate and drain matching circuits are designed for the constrained topology of Fig. 4.1.



Table 4.3: Circuit model element values for designs A-E

Common Element Values					
$L_{g0}$	$L_2$	$C_1$	$L_1$	$C_{tab}$	$C_{mut}$
0.8 nH	1.5 nH	7.11 pF	1.5 nH	5.6 pF	0.1 pF
Unique Element Values					
	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>
$L_0$	1.2 nH	2.0 nH	1.0 nH	0.4 nH	0.7 nH
$C_0$	0.78 pF	0.78 pF	0.32 pF	0.64 pF	0.93 pF

- From the ideal circuit, the lumped elements are implemented with bond-wires, MOS capacitors, and the package parasitics. This requires full-wave analysis since the profile of each bond-wire and the placement of the MOS capacitors and die within the package affects the lumped-element values.
- After taking into account current handling, geometric and manufacturing constraints, the effect of mutual reactances, and impedance sensitivity to machining tolerances, it is often the case that the initial circuit cannot be realized. Multiple iterations between full-wave, linear and nonlinear circuit simulations are done until the desired impedances are achieved, sometimes requiring a change in circuit topology.

The circuit model parameter values for the final, manufacturable, in-package networks are listed in Table 4.3. The networks are designed such that  $L_0$  and  $C_0$  can be tuned for each harmonic termination while the rest of the elements remained constant for each design to maintain a similar fundamental pre-match.

## 4.5 PASSIVE PACKAGE VALIDATION

Since one cannot measure directly the impedance presented by the in-package network to the die, a method was needed to verify that the fabricated package presents the expected impedance to the die and must do so up to harmonic frequencies. A validation method is discussed in [34], where

the active device within the package is replaced by a pedestal, and small-signal measurements are compared with full-wave simulations. However, a pedestal constitutes a short to ground, presenting a highly-reflective impedance that limits the validation accuracy, particularly at higher frequencies (harmonics).

Here we present a multi-harmonic validation method for a package model in which the active device in a package Fig.4.11a is replaced by a MOS capacitor of similar size and known value Fig.4.11b, allowing small-signal measurement of the full package to be directly compared to simulation. With package design  $B$  of the previous section. Higher-order parasitics within a package, namely mutual inductance between non-parallel bond-wires and mutual capacitance between the gate and drain tab, will be more clearly observed in measurement.

#### 4.5.1 FULL-WAVE SIMULATIONS

Since the validation package is purely passive, the entire package can be simulated without the use of internal ports in Ansys HFSS, with the model shown in Fig.4.12. Wave ports are placed at the gate and drain tab edges and de-embedded to the package plane. The geometry is meshed relative to the electrical length at the  $3^{rd}$  harmonic since the accurate knowledge of harmonic impedances is important for the design of an efficient PA. Full-wave simulations enable modeling of geometry effects such as angle between multiple connected electrically in parallel and varied lumped element and package heights

It is interesting to observe the surface current density magnitude at the second harmonic, shown in Fig. 4.12. The surface current density is high on the input bond wires to  $C_D$ , and progressively reduced in magnitude through the matching circuit. The current on the shunt inductor  $L_0$  is pronounced since this is the second harmonic termination network, with a mean value of about 600 A/m for 10-W excitation at the input port (Gate). It also becomes obvious when looking at the asymmetric geometry of  $L_0$  and  $L_1$  that mutual inductance plays a role that cannot be neglected, especially at the second harmonic. The closer of the two wires of  $L_1$  has a surface current mean value of about 250 while the further one is about 100 A/m, due to mutual inductance. Notice the

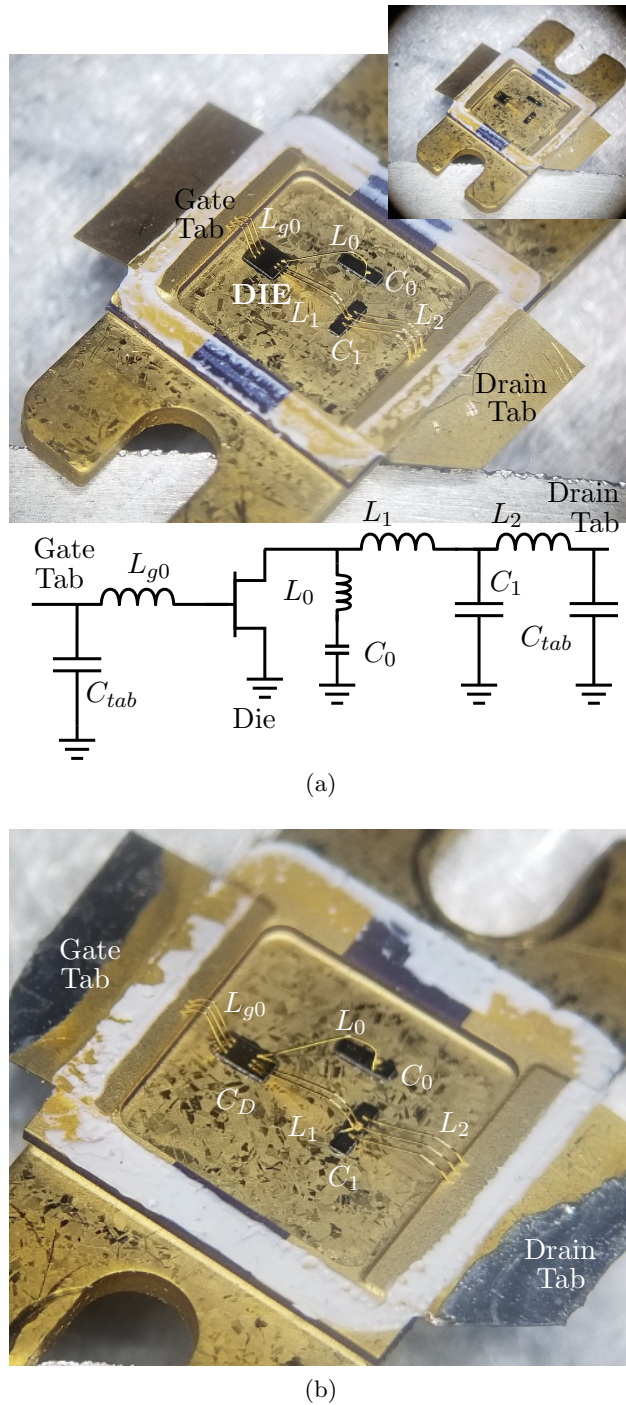


Figure 4.11: (a) Transistor package for an Infineon 10-W LDMOS device with a fundamental of 2.6 GHz. The package is custom designed for a fundamental pre-match and a  $2^{nd}$  harmonic termination both internal to the package. (b) Passive validation package, where the active device is replaced by a capacitor of similar size and known value. Circuit diagrams are also shown, where the inductors represent bond-wires and the drain and gate tabs are represented by capacitors.

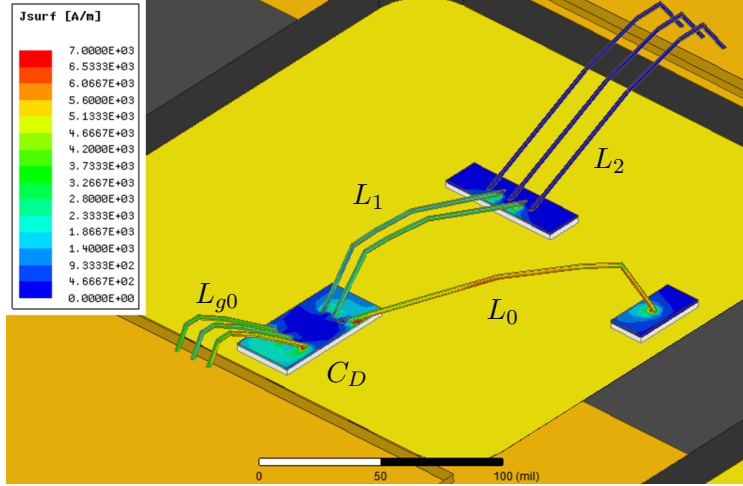


Figure 4.12: HFSS model of the passive-only in-packaged matching circuit showing a plot of  $2f_0$  of surface current magnitude along the bond wires and on the capacitor plates. The current along  $L_0$  is pronounced (600 A/m), since it is responsible for the  $2f_0$  drain termination. Notice that there is more current on the bond-wire closest to  $L_0$  than the other bond-wire at that point in the network. This is due to mutual inductance.

practically negligible  $2^{nd}$  harmonic current on  $L_2$ . The effect of mutual inductance and mutual capacitance is next taken into account when comparing with measured data.

#### 4.5.2 EXPERIMENTAL VALIDATION

The passive package is placed into a microstrip fixture that tapers from the 280-mil wide lead to a  $50\Omega$  environment, as shown in Fig.4.13. Thru-Reflect-Line (TRL) calibration is performed on the fixture to de-embed the measured  $S$ -parameters to the package plane. The simulated response of the circuit in Fig. 4.11b compared well with measurements at the fundamental but shows significant discrepancy at higher frequencies, pointing to the need of including mutual reactances. The most significant coupling is between bond-wires  $L_0$  and  $L_1$  as well as capacitive coupling between package tabs. The circuit was modified to include these mutual reactances as shown in Fig. 4.14, and  $L_{mut}$  and  $C_{mut}$  tuned to match measurement. Table 4.4 shows the resulting element values.

It is of interesting note that the mutual inductance  $L_{mut}$  between bond wire(s)  $L_0$  and  $L_1$  are significant since the coupling between them is a function of magnetic flux, which is in turn a function of the distance and angle between them. Therefore a mutual inductance between the two

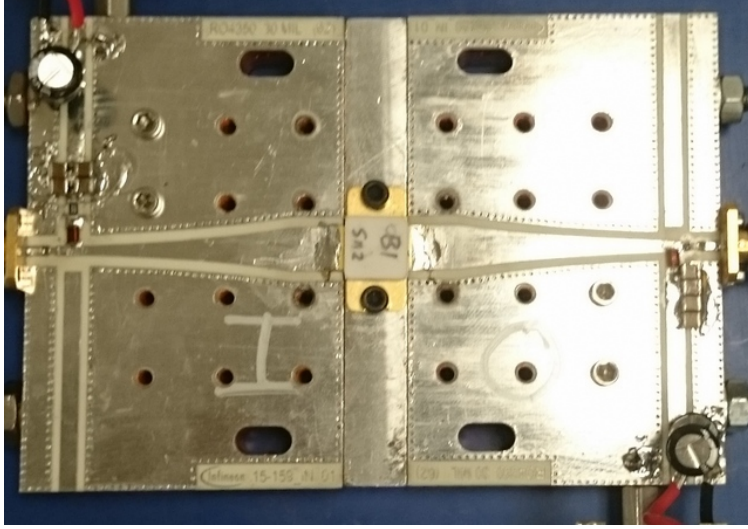


Figure 4.13: Microstrip fixture used for TRL calibration and measurement of the validation package. The package is mounted on a 280-mil wide microstrip line and tapered to a  $50\ \Omega$  environment. Bias-tees are integrated into the fixture anticipating large-signal measurements with the active package but are not necessary for the validation process.

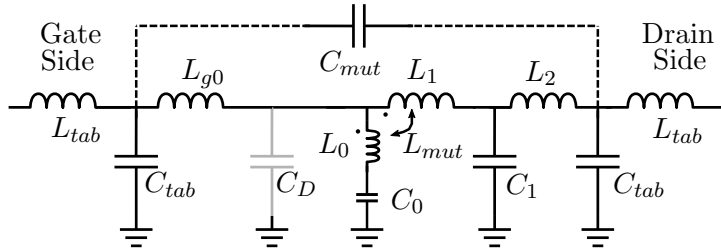


Figure 4.14: Equivalent circuit model of passive package shown in Fig. 4.11b. The active device in Fig. 4.11a is replaced by a capacitor  $C_D$  of similar size and known value, represented by capacitor  $C_D$  in grey.

Table 4.4: Circuit model element values

$L_0$	$L_{g0}$	$L_1$	$L_{mut}$	$L_{tab}$	$L_2$
2.0 nH	1.1 nH	0.8 nH	0.31 nH	0.13 nH	1.4 nH
$C_0$	$C_1$	$C_D$	$C_{mut}$	$C_{tab}$	
0.78 pF	7.11 pF	2.58 pF	0.1 pF	5.6 pF	

different sets of bond-wires is to be expected, since  $L_0$  is large and is rotated  $45^\circ$  relative to  $L_1$ . The element  $C_{mut}$  is also not negligible.

Fig. 4.15 and Fig. 4.16 show the results of measured example  $S$ -parameters compared to two simulations: the circuit model from Fig. 4.11b which does not include mutual reactances and the

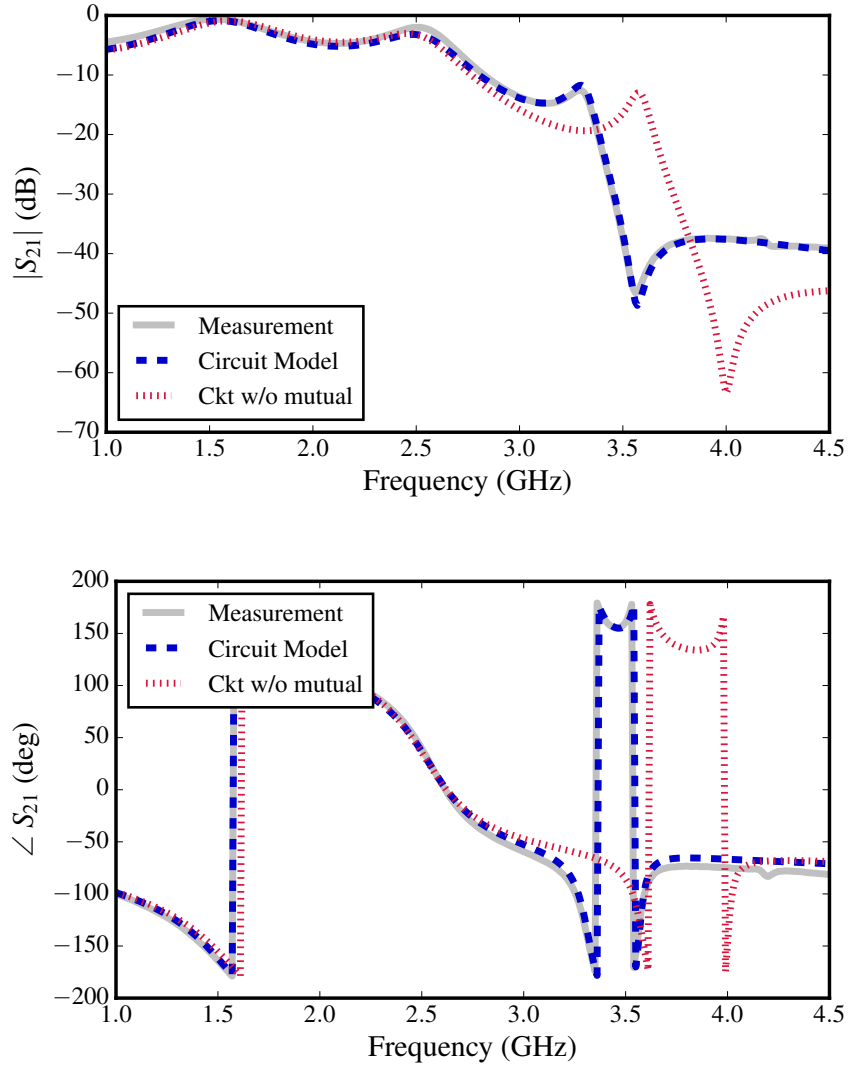


Figure 4.15: Measured (solid line) vs. simulated (dashed line)  $S_{21}$  of the equivalent package circuit model from Fig.4. The elements  $C_{mut}$  and  $L_{mut}$  are omitted from this circuit model and also plotted (dotted line) to illustrate the distinct impact of these values on the impedance presented to the packaged device.

more complete circuit model from Fig. 4.14 obtained from full-wave simulations. The amplitude of the input reflection coefficient shows reasonable agreement with the simpler circuit up to slightly above the fundamental frequency of 2.6 GHz while there is significant discrepancy above 3 GHz. Similarly, the phase of the transmission coefficient cannot be predicted with a simpler model above 3 GHz which will critically affect harmonically-terminated PA design.

In summary, this chapter presents a technique to validate a transistor package model by re-

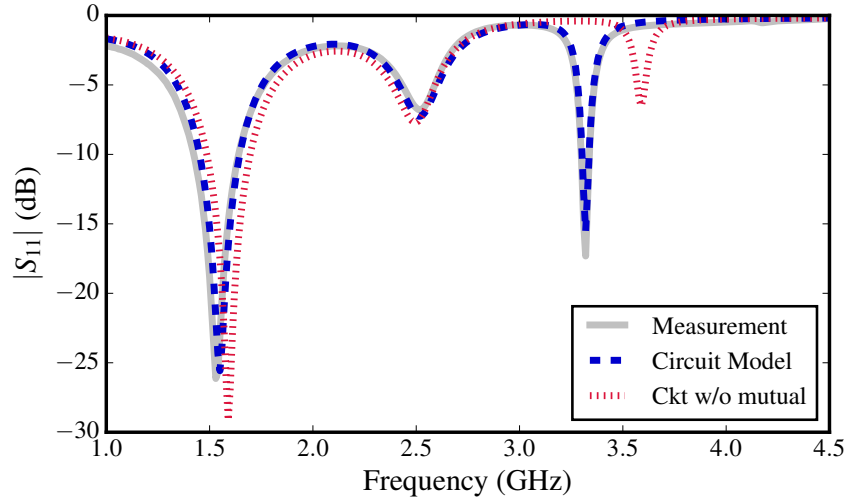


Figure 4.16: Measured (solid line) vs. simulated (dashed line)  $|S_{11}|$  of the equivalent package circuit model from Fig.4. The elements  $C_{mut}$  and  $L_{mut}$  are omitted from this circuit model and also plotted (dotted line) to illustrate the distinct impact of these values on the impedance presented to the packaged device.

placing the active device with a metal-oxide-semiconductor (MOS) capacitor of similar size and known value, allowing small-signal measurement of the full package. Specifically, number, shape, and length of bond-wires, specific values of shunt capacitors, and mutual reactances are determined to present precise complex impedance at the fundamental and  $2^{nd}$  harmonic. The impedances are determined by transistor source and loadpull. The technique is demonstrated with a 10-W Infineon LDMOS device at a fundamental frequency of 2.6 GHz, in a custom-designed package with both fundamental and  $2^{nd}$  harmonic pre-match and termination impedances implemented within the package. Full-wave simulations are shown to be essential to accurately model the passive elements above 3 GHz. The presented technique is an easy and straightforward experimental method that can be used to validate package design that performs more than just fundamental pre-matching.

## 4.6 ACTIVE PACKAGE MEASUREMENTS

The physical realizations of the package designs, with relative placement of bond-wires and capacitors relative for the 10-W die, are shown in Fig. 4.17. The HFSS simulated impedance presented

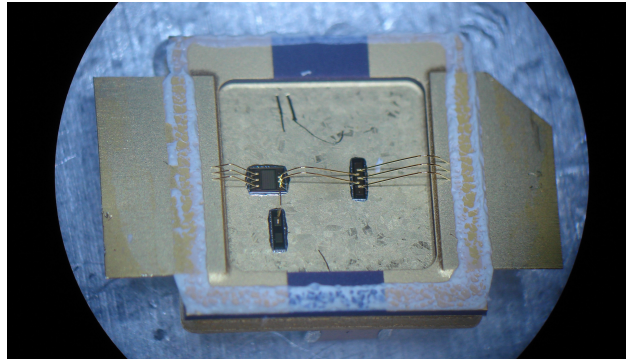
to the die drain by the representative package design  $B$  is shown in Fig. 4.18 in dashed grey line. The simulated  $f_0$  and  $2f_0$  PAE contours, are also shown in the figure with the red and blue crosses indicated the  $f_0$  and  $2f_0$  achieved impedances that lie very close to the load-pull contours. Fundamental load-pull measurements are performed using the fixture shown in Fig. 4.13, where exponentially-tapered microstrip lines on a Rogers 4350B 30-mil substrate transform  $50\text{-}\Omega$  to the  $17\text{-}\Omega$  characteristic impedance of the package tab at the package reference plane.

Fig. 4.19 presents measured efficiencies for the various package designs that correspond to different second harmonic terminations. The fundamental impedance is also shown (colored squares), and as expected, this impedance does not vary significantly while the harmonic impedance moves around the edge of the Smith chart. The resulting PAE varies by up to 15 percentage points, while the fundamental load remains the same, showing the dramatic effect of in-package harmonic termination on PA efficiency.

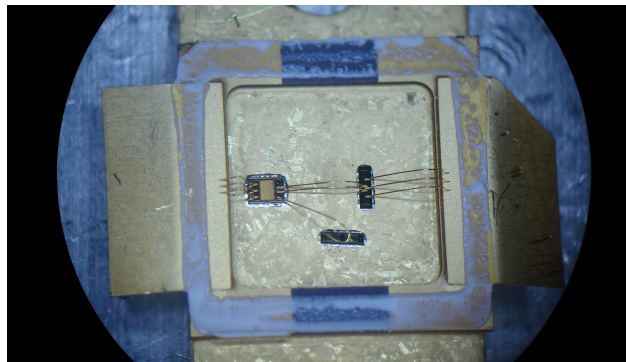
It is interesting to compare these results to those shown in Fig. 2.11. When the  $2^{nd}$  harmonic is tuned externally to the die in the commercial package using discrete  $2f_0$  load-pull, we observe only 3 percentage points variation in PAE. The in-package design shows slight improvement in PAE, ultimately limited for this device at this frequency due to the relatively large  $C_{out}$  and low  $f_t$  typical of LDMOS devices.

In summary, this chapter presents analysis and design of several circuit topologies for in-package PA matching using only capacitors and bond-wires. A purely passive validation circuit is also presented, pointing to the need for full-wave simulations. Several topologies with varying harmonic terminations are experimentally validated showing an efficiency change of 15 percentage points as a function of  $2f_0$  impedance. These results are reported in [56] and [57].

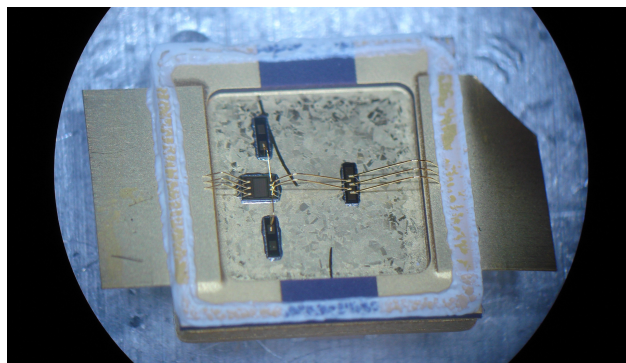




(a)



(b)



(c)

Figure 4.17: Matching networks from Table 1 realized within a package. Three distinct packages networks are shown, with varying element values: (a) designs A and C, (c) design B, and (b) designs D and E.

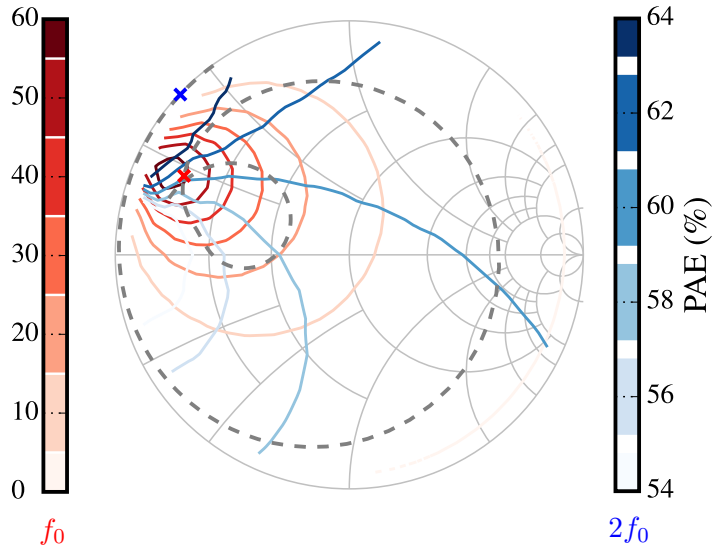


Figure 4.18: Load-pull contours for constant  $PAE$  for varied fundamental (red scale) and  $2^{nd}$  harmonic (blue scale) load impedance. The impedance presented to the device drain terminal by the in-package passive circuit from Fig. 4.11b over the 1 to 8 GHz frequency range is shown by the dashed gray trace, with the  $f_0$  and  $2f_0$  impedances indicated by the red and blue crosses, respectively.

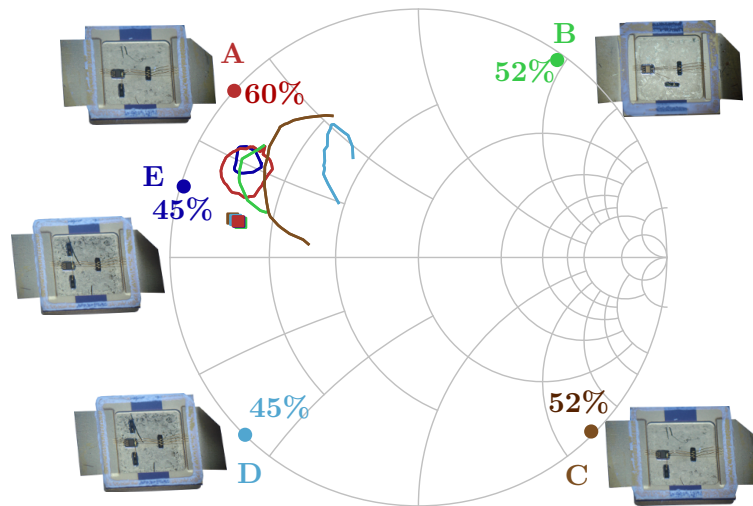


Figure 4.19: Fundamental frequency constant  $PAE$  contours (referenced at the die plane) for each package shown in colors corresponding to each package design. The maximum  $PAE$  measured during  $f_0$  loadpull of each package is shown beside its corresponding  $2f_0$  termination (colored circle). The  $f_0$  impedance presented to the drain of the die for each package design is shown by colored squares.

# POWER AMPLIFIER IN A PACKAGE

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In the previous chapters, the modeling, design, simulation, fabrication, and validation of in-package matching networks has been discussed and demonstrated up to the  $2^{nd}$  harmonic. In this chapter, in-package design will include not only a precisely phased  $2^{nd}$  reflection but also a matched fundamental and a  $3^{rd}$  harmonic termination to fully realize a waveform engineered PA within a package.

Previous work has addressed varying aspects of such a design but never a full PA. In-package harmonic pre-matching in [58,59] and harmonic terminations in [60,61] rely on Alumina microstrip circuits placed within the package. Harmonic pre-matching exclusively using bond-wires, capacitors, and package parasitics has been demonstrated in [62–64], but in these works the harmonics were

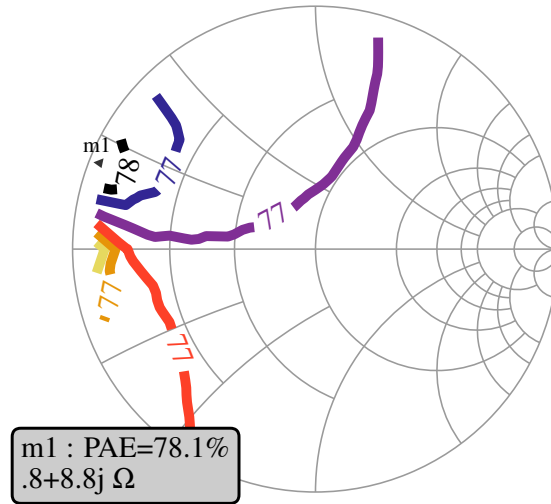
not specifically presented with a high-magnitude reflection coefficient. Similarly, in [65], the  $2^{nd}$  harmonic impedance is pre-matched within a package used in a two-stage Doherty PA. Internally-matched Class-E PAs demonstrated in [66,67] do not specifically control the phase of the harmonic impedances. An outphasing switched-mode PA integrated within a large custom package (1.3 cm  $\times$  1.4 cm) is demonstrated in [68] with a microstrip combiner. The results in [58]- [68] are all demonstrated with GaN devices.

A PA with a complex fundamental match and  $2^{nd}$ ,  $3^{rd}$  harmonic terminations realized with bond-wires and package parasitics is first demonstrated with the same LDMOS device as used in previous chapters. The same approach will next be demonstrated on a GaN device where higher harmonic content is expected to be due to GaN's typically lower drain capacitance, where in-package harmonic control is more effective and more important. The use of GaN presents unique design considerations, such as a higher output impedance, the need for an in-package stability network, and the preference for voltage peaking operation.

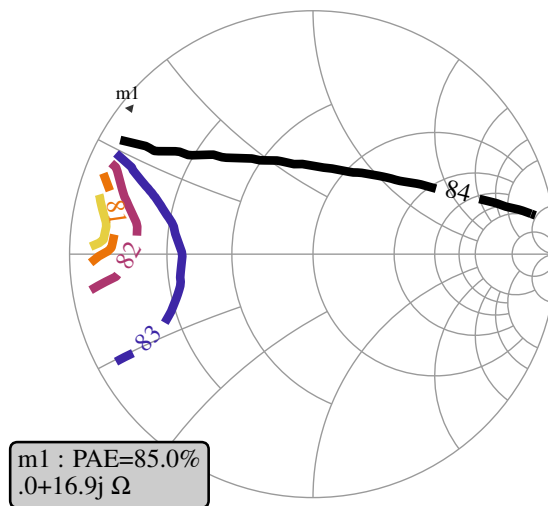
## 5.1 CLASS-F LDMOS PACKAGE

A class-F package is demonstrated using the same LDMOS device as in previous chapters. In class-F mode of operation, the voltage is a square wave in time domain, while the current is half of a sine wave. This mode of operation is chosen since LDMOS devices are more efficient under current peaking conditions than under voltage peaking characteristic of class- $F^{-1}$  operation [69]. The design frequency is chosen to be 1 GHz since at higher frequencies the large output capacitance of the device limits the harmonic content necessary for class-F operation. This is illustrated in Fig. 5.1, where the top Smith chart shows a  $3^{rd}$  harmonic LP for  $PAE$  at 1.5 GHz. The efficiency does not exceed 78% and varies by only 1 percentage point for many  $3f_0$  impedances. In contrast, a  $3f_0$  LP at 1 GHz shows both a higher  $PAE$  and several percentage point variation as the  $3^{rd}$  harmonic impedance is varied, indicating sufficient harmonic content for waveform shaping.

In class- $F$  mode, the time-domain overlap between voltage and current is minimized by squaring

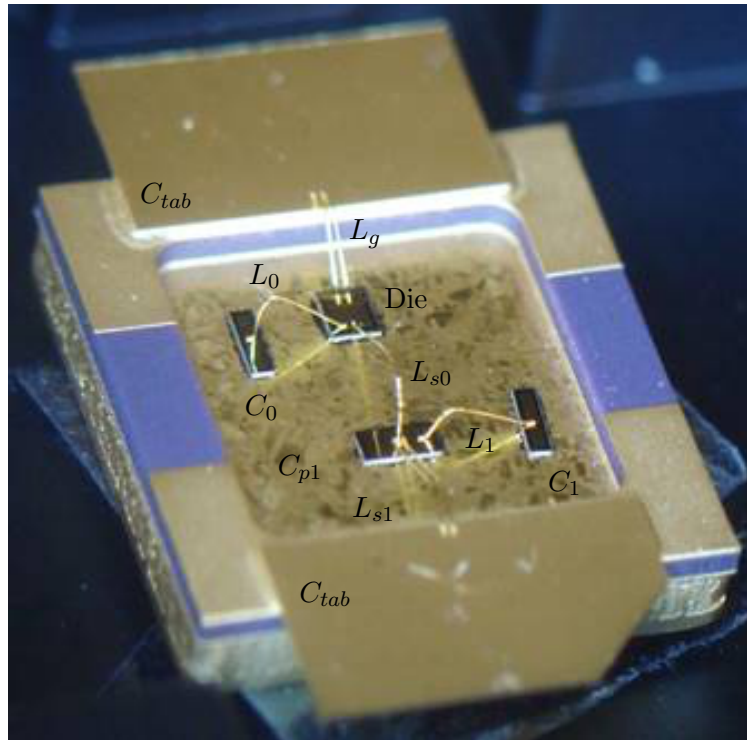


(a)

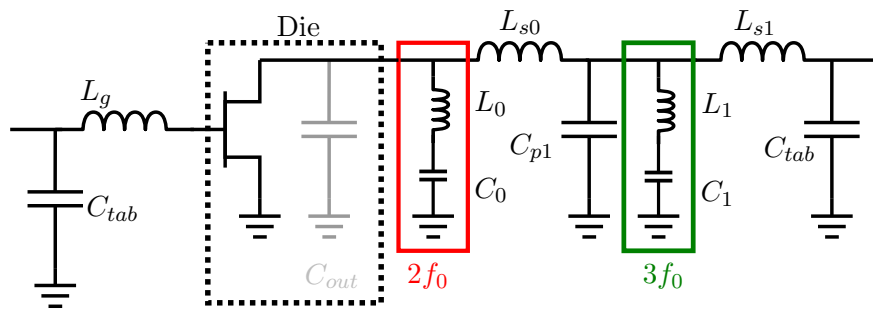


(b)

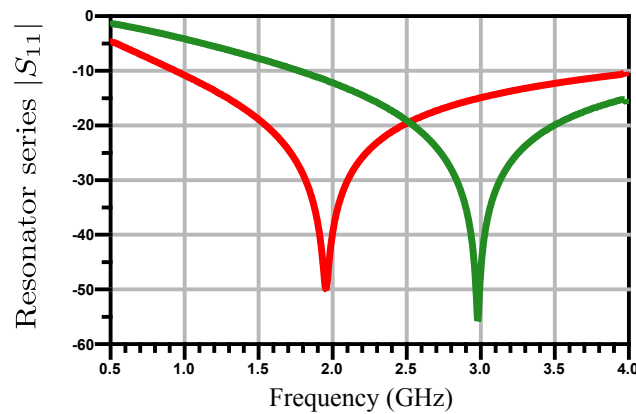
Figure 5.1: Simulated  $3f_0$  load-pull contours for  $PAE$  at the die plane of the LDMOS device used in the Class-F package with a fundamental of (a) 1.5 GHz and (b) 1.0 GHz, where it can be seen that even at 1.5 GHz, there is insufficient harmonic content for waveform shaping. A design frequency of 1.0 GHz is chosen since a variation of 5 points of  $PAE$  is seen in (b).



(a)



(b)



(c)

Figure 5.2: (a) Photo of the fabricated Class-F package design (which uses the standard package in Fig. 4.2b which has a 280-mil wide tab), and (b) the equivalent circuit model (b), with element values shown in Table 5.1. The  $2f_0$  and  $3f_0$  resonators are shown in the red and green boxes, respectively.  $L_{s0}$  and  $C_{p1}$  are designed to provide the phase transformation of the  $3f_0$  short to an open at the virtual drain considering the device output capacitance (shown in grey). (c) The simulated return loss of each in-package resonator.

Table 5.1: Circuit model element values for Class-F Package

$C_{tab}$	$L_g$	$L_0$	$C_0$	$L_{ls0}$
5.6 pF	1.43 nH	1.63 nH	4.01 pF	2.5 nH
$C_{p1}$	$L_{s1}$	$L_1$	$C_1$	
21.29 pF	1.31 nH	1.53 nH	1.84 pF	

the voltage at the virtual drain of the device. A short circuit is presented at even harmonics, while an open circuit is presented at odd harmonics. In practice, a short at  $2f_0$  and open at  $3f_0$  is sufficient, as the device gain drops significantly after the third harmonic. In a package, these harmonic terminations are realized with lumped elements. An  $LC$  circuit consisting of a bond-wire connected to a shunt MOS capacitor is placed in shunt immediately after the die to present a short  $2f_0$ , as shown in Fig. 5.2b. The elements  $L_1$  and  $C_1$  are chosen to resonate at  $3f_0$  but require a phase shift to be transformed to an open-circuit at the virtual drain. The combination of elements  $L_{s0}$  and  $C_{p1}$ , as well as  $C_{out}$  and the  $2f_0$  resonator, serve as an impedance transformer for the  $3f_0$  resonator.

The values for the resonator elements are chosen to maximize inductance while considering the trade-offs between Q-factor, loss, and package and mechanical limitations as discussed in Chapter 4. All of the elements contribute to the fundamental pre-match. With the desired ideal network known (values shown in Table 5.1), the package network design procedure detailed in previous sections is followed to produce the final package design shown in Fig. 5.2a. Fundamental load-pull is performed on the Class- $F$  package using passive Focus tuners. Power measurements are de-embedded to the package plane. The resulting  $PAE$  contours are plotted in Fig. 5.3 showing a maximum  $PAE$  of 67 % and an output power of 12 W for an LDMO PA in a single 10 x 10 mm<sup>2</sup> package.

## 5.2 CLASS- $F^{-1}$ GAN PACKAGE

Gallium Nitride is a wide bandgap semiconductor (3.4 eV in GaN versus 1.1 eV in Silicon) and operates at a high voltage. Typical drain supply voltages for high-power lower-frequency GaN

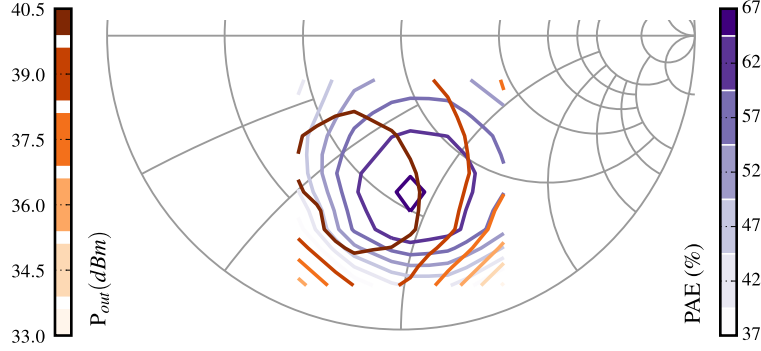


Figure 5.3: Class- $F$  package load-pull contours of constant PAE and  $P_{out}$  measured and de-embedded to the package plane. Input power is constant at 22 dBm.

transistors are 50 V with breakdown in excess of 140 V. For higher frequency devices, the gate length is reduced and as a consequence the operating voltage as well as the breakdown becomes smaller. For example, the nominal operating voltage for 150-nm GaN-on-SiC is 28 V with a breakdown of 60 V. Therefore GaN devices favor voltage instead of current peaking, corresponding to a class- $F^{-1}$  instead of class-F waveforms. In class- $F^{-1}$  mode, even harmonics are reflected by an open-circuit impedance to achieve the voltage-peaking operation and the odd harmonic impedances are short-circuited to achieve current squaring.

### 5.2.1 DESIGN METHODOLOGY FOR GAN CLASS- $F^{-1}$ IN A PACKAGE

In order to achieve class- $F^{-1}$  operation, we investigate the equivalent circuit shown in Fig. 5.4. The  $C_{out}$  is the equivalent output capacitance of the transistor. The series resonances  $L_2/C_2$  and  $L_3/C_3$  are coupled through the series inductor  $L_x$  and together present the correct terminations to the 2<sup>nd</sup> and 3<sup>rd</sup> harmonics [70]. The input admittance  $Y_{in}$  in the Laplace domain is given by:

$$Y_{in}(s) = sC_{out} + \frac{sC_2}{\left(\frac{s}{\omega_{02}}\right)^2 + 1} + \frac{1}{sL_x + \frac{1}{g_L + sC_{tab} + \frac{sC_3}{\left(\frac{s}{\omega_{03}}\right)^2 + 1}}} \quad (5.1)$$

where  $g_L$  is the normalized load admittance connected in parallel to  $C_{tab}$ , and  $\omega_{02}$  and  $\omega_{03}$  are the resonant frequencies for the  $L_2/C_2$  and  $L_3/C_3$  resonators respectively. For a class- $F^{-1}$  termination,



we require that the admittance at the 3<sup>rd</sup> harmonic is infinite. Doing so to Equation 5.1, in phasor form, yields

$$Y_{in}(j\omega_3) = \infty = j\omega_3 C_{out} + \frac{j\omega_3 C_3}{\left(j\frac{\omega_3}{\omega_{03}}\right)^2 + 1} + Y_{rem} \quad (5.2)$$

where  $Y_{rem}$  is the remainder of the third term in Equation 5.1. Therefore by choosing values for the  $L_3/C_3$  circuit is resonant at 3<sup>rd</sup> harmonic ( $\omega_{03} = \omega_3$ ), a short circuit will be presented to the drain. This gives a required relationship between  $L_3$  and  $C_3$ . The 2<sup>nd</sup> harmonic admittance is zero (open circuit) resulting in the following equation for the input admittance at the virtual drain:

$$Y_{in}(j\omega_2) = 0 = j\omega_2 (C_{out} + C_a) - j\frac{1}{\omega_2 L_x} \quad (5.3)$$

where

$$C_a = \frac{C_3}{1 - \left(\frac{\omega_2}{\omega_{03}}\right)^2} \quad (5.4)$$

From Equation 5.3, we see, interestingly, that the 2<sup>nd</sup> harmonic impedance depends on  $L_x$ ,  $C_{out}$ , and the  $3f_0$  resonator. With the latter two values already determined,  $L_x$  is simply given by:

$$L_x = \frac{1}{\omega_2^2 (C_{out} + C_a)} \quad (5.5)$$

The remaining undetermined components are used to present a complex fundamental match determined by load-pull. In practice, the series inductance  $L_x$  can become large (e.g. 1.5 nH in the case for class- $F^{-1}$  terminations) and difficult to obtain with bond-wires. For a more practical implementation, in an alternative circuit, the series inductor can be replaced by a T-circuit consisting of two smaller valued series inductors with a shunt capacitor between them. These topologies are used for obtaining initial values for the circuit elements for an in-package class- $F^{-1}$  PA using a GaN device.

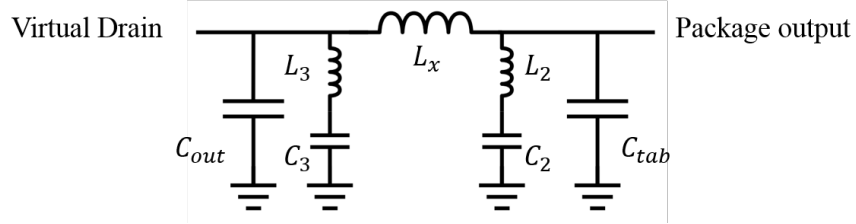


Figure 5.4: Equivalent circuit for a class- $F^{-1}$  in a package.

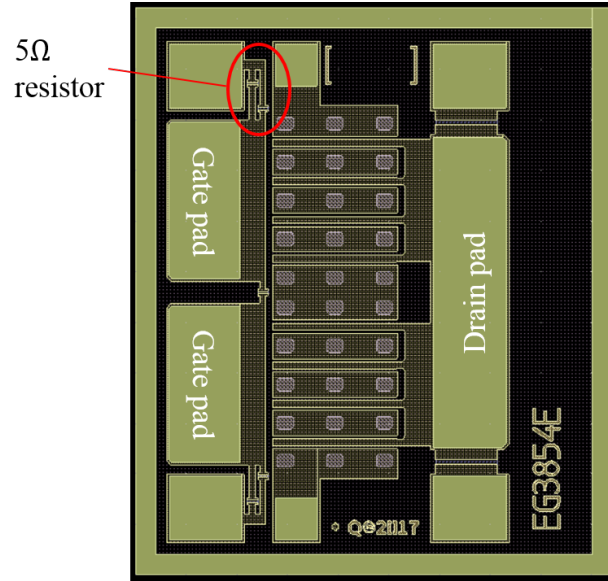


Figure 5.5: Layout of the 25-W Qorvo GaN die with gate and drain pads labeled. The die includes 2 cells of 4  $375\text{-}\mu\text{m}$  gate fingers, with gate bondpads to each cell. The gates of the cells also lead to additional, parallel bondpads connected by a  $5\ \Omega$  TaN resistor. Courtesy of Qorvo.

### 5.2.2 CLASS- $F^{-1}$ GAN PA DESIGN

A harmonically-terminated transistor package will be demonstrated with a 25-W Qorvo GaN die (Fig. 5.5) at the same frequency of the previous designs (2.6 GHz). The die includes 2 cells of 4  $375\text{-}\mu\text{m}$  gate fingers, with gate bondpads to each cell. The gates of the cells also lead to additional, parallel bondpads connected by a  $5\ \Omega$  TaN resistor. A bias point of  $V_{ds} = 50\ \text{V}$ ,  $I_{ds} = 20\ \text{mA}$  is chosen since it is near cutoff and therefore will produce significant  $2^{\text{nd}}$  harmonic power. The  $Y$ -parameter extraction method detailed in [71] is used to approximate the device non-linear output capacitances  $C_{out}$ . The resulting value over swept  $V_{gs}$  is shown in Fig. 5.6.

Load-pull is performed on the device to determine the desired impedances to be presented by

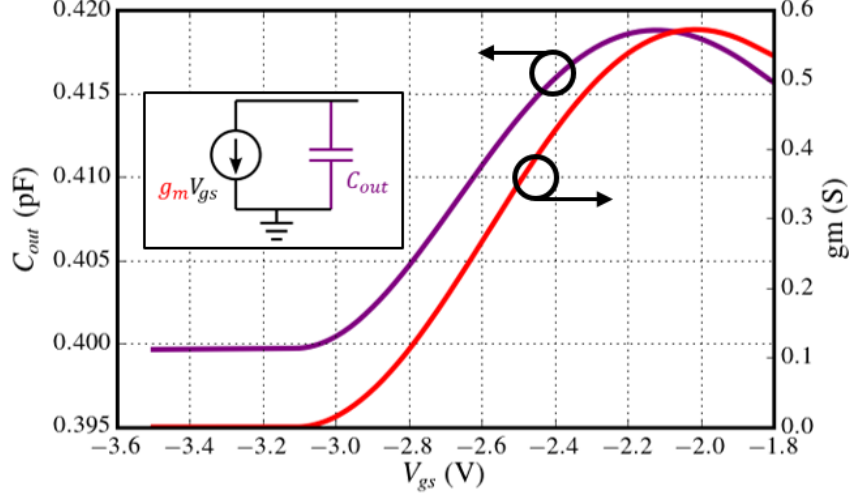
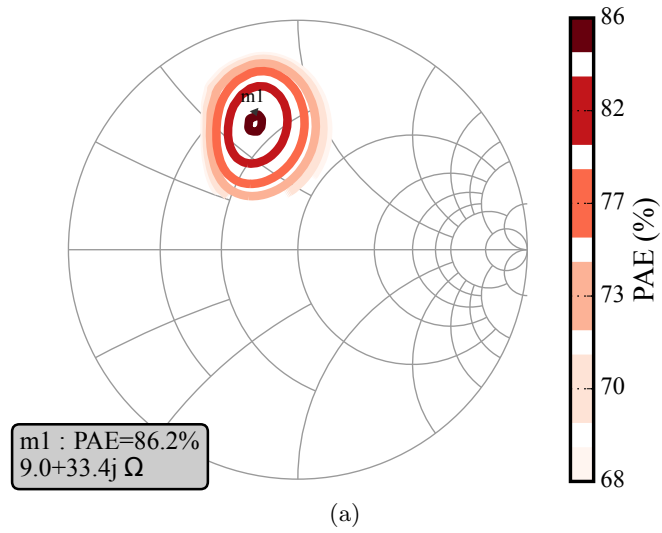


Figure 5.6: The extracted output capacitance  $C_{out}$  with swept gate voltage. At the chosen bias point,  $C_{out}$  is approximated to be 0.41 pF. This is where the slope of  $C_{out}$  is the greatest, indicating a large degree of non-linearity and therefore harmonic content.

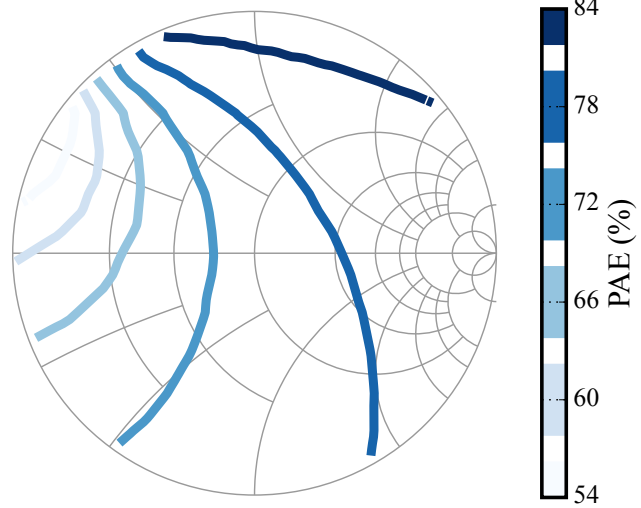
the drain network. The non-linear circuit given by the manufacturer models only the transistor (up to the gate and drain fingers). The gate and drain manifolds are simulated in Sonnet software, a finite-element EM solver chosen since it was seen that, due to the electrically small geometry of a transistor die, the ports in other solvers couple and present additional capacitances that are not physical. Load-pull is then performed on the transistor model including the FEM simulations of the drain pad. The resulting  $PAE$  contours at each harmonic are shown in Fig. 5.7.

The load-pull contours indicate that there is sufficient harmonic content for waveform shaping. The  $2f_0$  LP is performed with  $3f_0$  terminated at  $50\Omega$ . In Fig. 5.8, the  $2f_0$  LP contours are de-embedded beyond  $C_{out}$  to the virtual drain of the device. The de-embedded contours indicate that the device prefers a  $2^{nd}$  harmonic open and therefore class- $F^{-1}$  operation, as already argued is the case for GaN transistors [72]. The commercial package of the previously used LDMOS device (Fig. 3.7) is used in the following design, since it has a large cavity and therefore allows for a more complex matching network. With a known  $C_{out}$  and  $C_{tab}$ , the methodology of the previous section is utilized to solve for the remaining elements in the drain network for a class- $F^{-1}$  solution. These resultant values are given in Table 5.2.

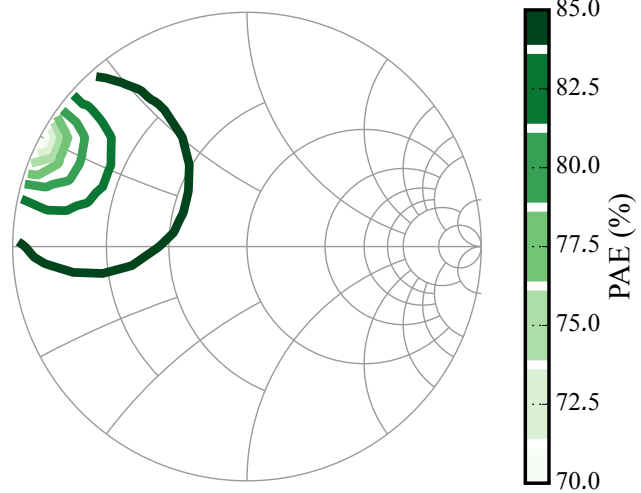
The physical in-package realization of the circuit model network is shown in Fig. 5.9. The profile



(a)



(b)



(c)

Figure 5.7: The simulated *PAE* contours at the die reference plane for LP at (a)  $f_0$ , (b)  $2f_0$ , and (c)  $3f_0$ .

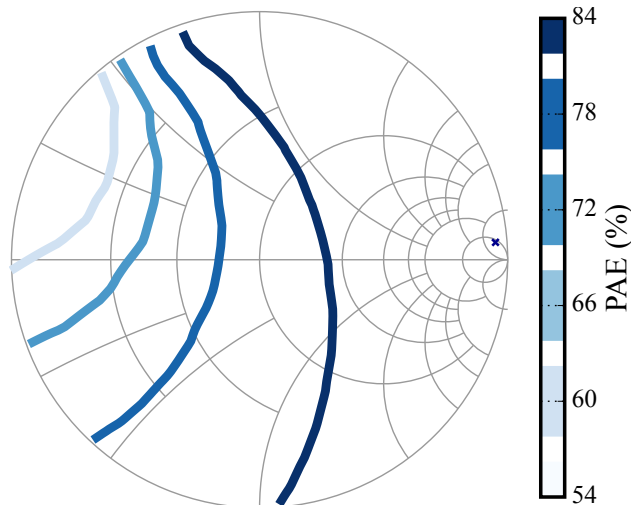


Figure 5.8: The  $2f_0$  LP contours of constant  $PAE$  of Fig. 5.7b deembedded to the virtual drain, indicating that the device prefers a  $2f_0$  open, with the cross symbol indicating the peak efficiency impedance.

	$C_{tab}$	$L_3$	$C_3$	$L_x$	$L_2$	$C_2$		
Synthesized	1.9 pF	0.27 nH	1.5 pF	0.84 nH	0.42 nH	2.4 pF		
	$C_{tab}$	$L_3$	$C_3$	$L_x$	$L_2$	$C_2$	$L_{x2}$	$C_x$
Adjusted	1.9 pF	0.32 nH	1.0 pF	0.76 nH	1.0 nH	1.0 pF	0.87 nH	3.0 pF

Table 5.2: Circuit model element values for the class- $F^{-1}$  package output network, as determined from Sec. 5.2.2 (synthesized) and as adjusted for practical implementation (adjusted).

in each bond-wire array is designed and simulated in HFSS in individual segments until it presents the desired inductance, then tuned once placed in the package due to both the placement of the bond-wire landing and the coupling between other elements. The finalized profiles also adhere to those that can be constructed by bonding machines. For example, the bond-wires should be at least 6 mils apart on each pad.

In the  $L_3$  bond-wire (responsible for the  $3f_0$  short), each individual bond-wire has a different profile considering the geometry of the die bond-pads, the placement of the  $L_x$  bond-wires, and the placement of the  $C_3$  capacitor. The  $L_{x2}$  bond-wires are angled to both reduce mutual coupling (allowing a  $3^{rd}$  bond-wire) and to allow for a better current distribution on the tab and therefore lower insertion loss [54].

The topology is revised from that of Fig. 5.4 in order to make the network symmetric, since

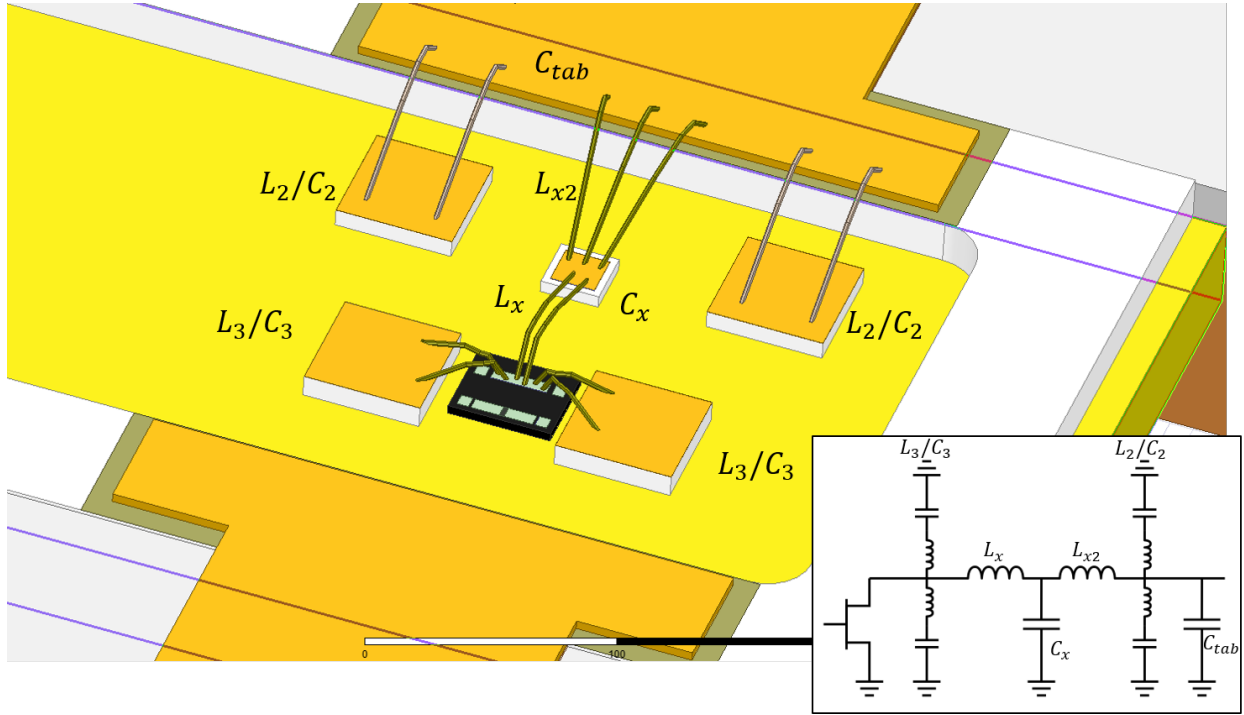


Figure 5.9: The physical realization of the drain network using package parasitics, device intrinsic capacitance, bond-wires, and capacitors to present Class- $F^{-1}$  impedances to the virtual drain.

it was found that symmetric current distributions throughout an in-package network results in reduced insertion loss. Multiple bond-wires to minimize bond-wire loss at each node and also betters current handling. However, this reduces total inductance requiring longer bond-wires and relying on mutual inductance.

Even with multiple bond-wires at every node, the equivalent loss of each bond-wire array is approximately  $0.2\Omega$ . Although this is a relatively low resistance (made by intentionally using multiple bond-wires), the impact on harmonic termination fidelity is significant. This is illustrated in Fig. 5.10, where the left Smith chart shows the input impedance of the drain network with the ideal lossless circuit model. The Smith chart in Fig. 5.10b shows the impact of an additional  $0.2\Omega$  resistance of the bond-wires. It is evident that the  $2^{nd}$  harmonic impedance is significantly reduced in reflection coefficient magnitude which reduces efficiency by up to 10%. Although the same  $0.2\Omega$  loss was applied to each inductor in the circuit model, the loss had the most dramatic impact on the  $2^{nd}$  harmonic termination. This is due to the impedance inverter formed by the  $L_x$ - $C_x$ - $L_{x2}$

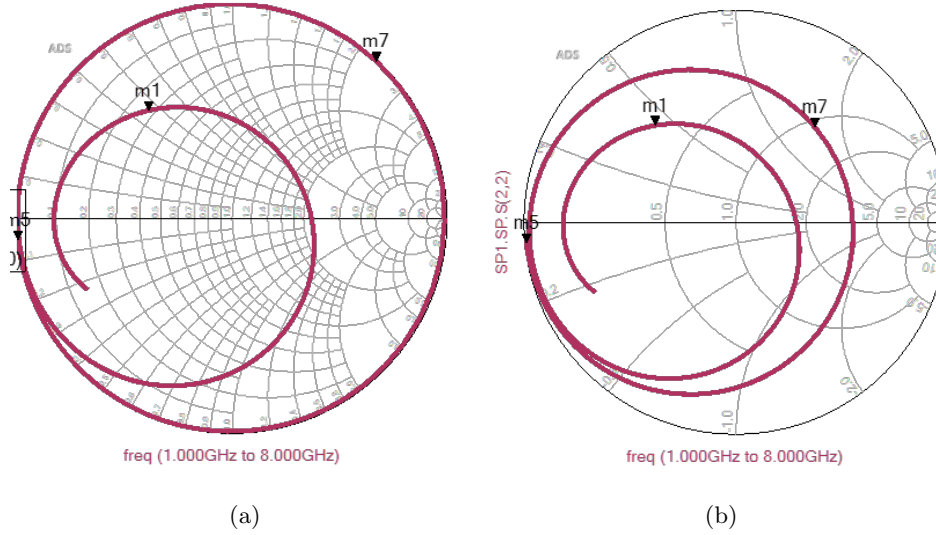


Figure 5.10: (a) The input impedance of the drain network using the ideal, lossless circuit model. (b) The impedance presented by the device using the same circuit model but with an additional  $0.2\ \Omega$  reflecting the HFSS simulated drain network of Fig. 5.9. The markers m1, m7, and m5 indicate  $f_0$ ,  $2f_0$ , and  $3f_0$  impedance, respectively.

network, as explained in Section 4.2.

has the most dramatic impact on the due to the impedance inverting network formed by Lx-Cx-Lx2. considering the impedance inverter formed by the lx-cx-lx2 network.

This drain network is the result of iteration between the source network as well, since the design of the gate network also affects allowable length of the series drain bond-wires and the placement of  $L_3/C_3$  resonator. The source network is a  $2^{nd}$ -order low-pass filter which matches to the complex  $S_{11}$  of the device and is shown in Fig. 5.11 before the addition of the stability network.

### 5.2.3 IN-PACKAGE STABILITY

By matching a transistor within a package, before the PCB and bias network, the PA becomes more prone to instability. Although an external stability network can be used to reduce gain at low frequencies, unconditional stability is difficult to guarantee at the fundamental if the stability network is introduced to an already matched PA. The criteria for stability used in this analysis is a  $k$ -factor greater than 1 throughout the entire range of frequencies where the device has gain.

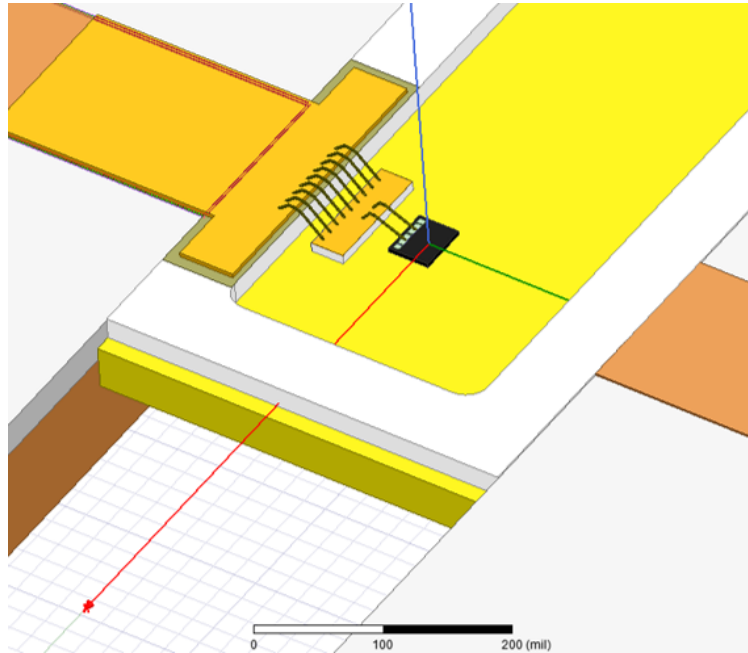


Figure 5.11: The physical realization of the gate network in HFSS (before the addition of the stability network) which matches to the complex input impedance of the device without the use of an package-external matching network.

Without the presence of any stabilizing network, the device is prone to instability, as can be seen in the plot of the  $k$ -factor of Fig. 5.12a when the device is input and output matched. The commonly used technique of an input parallel  $RC$  network is then applied external to the package (Fig. 5.12b) which satisfies the stability criteria for all but the range of frequencies near the design frequency of the package. It was seen that no choice of  $R$  or  $C$  could increase the  $k$ -factor in this frequency range without prohibitively reducing gain.

A package-internal stability network is added to affect the  $k$ -factor directly. The network is restricted to small-valued, series inductance (bond-wire) and a shunt capacitance. In the presented solution, the die on-chip resistor to a bond-pad is also used, creating a shunt  $RLC$  network to be bonded to the gate offset gate pads of the die (Fig. 5.5). Such a network eliminates the need for an external network since, through the proper design of the elements, gain is reduced significantly at low frequencies (less than 2 GHz) while gain is reduced at higher frequencies only enough to meet the stability criteria. Shown in Fig. 5.12c is the circuit model and simulated  $k$ -factor of the package design with the revised gate network.



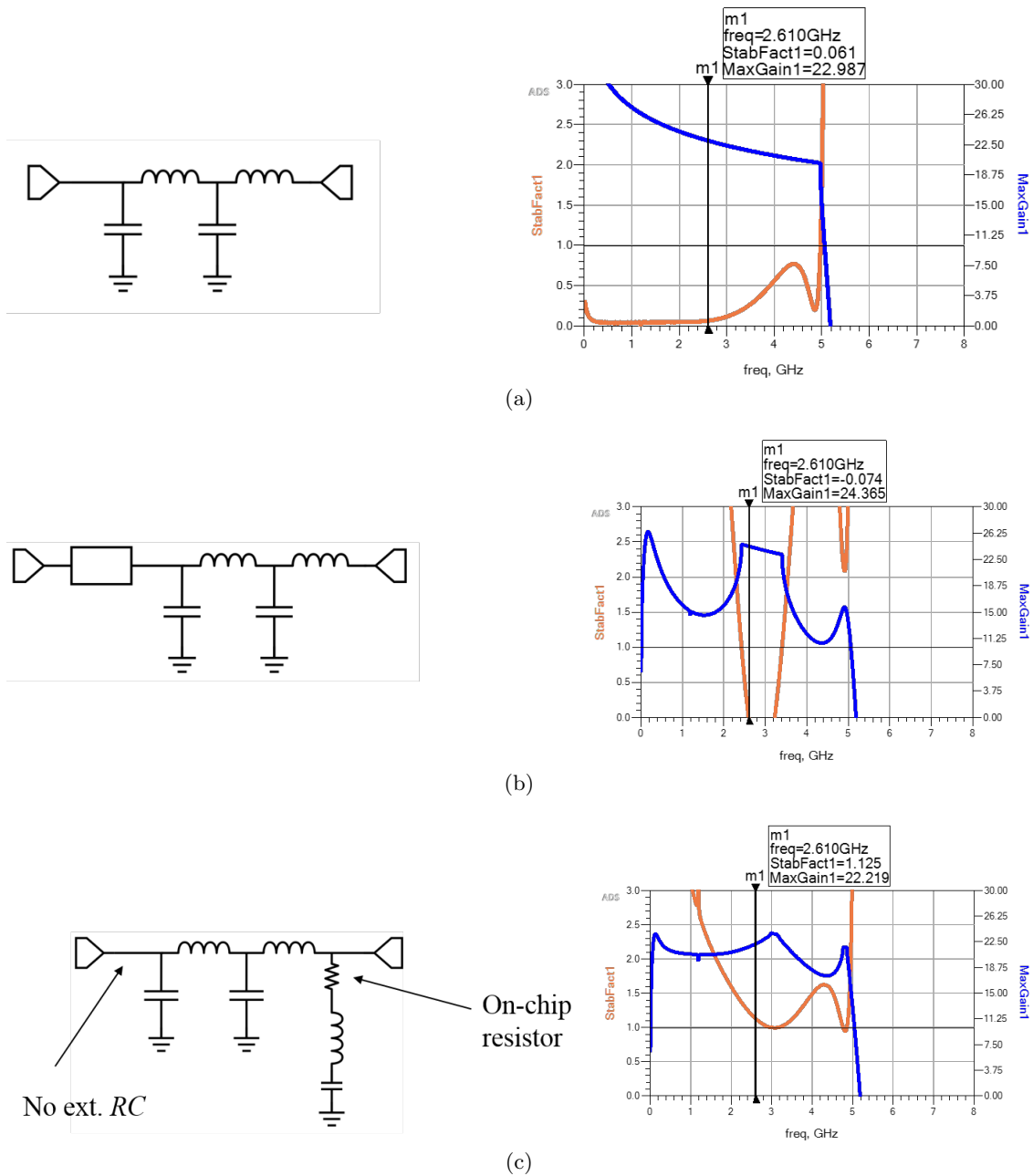
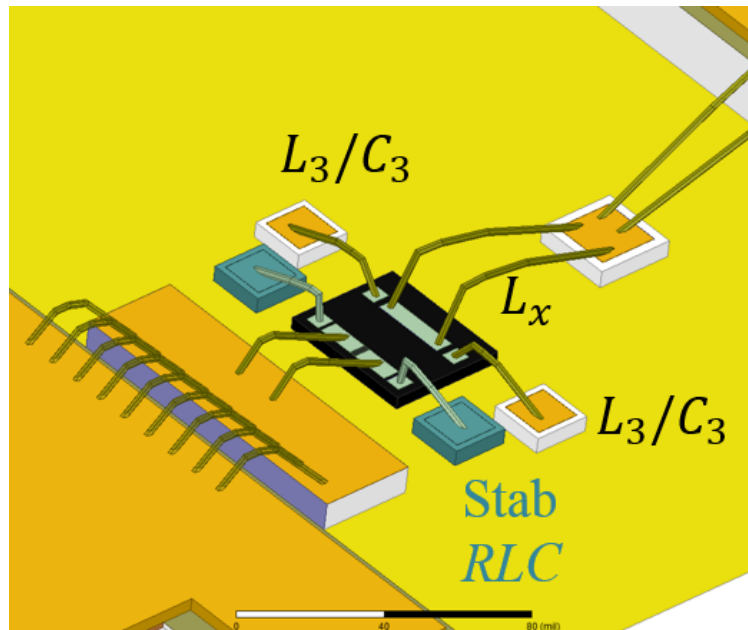
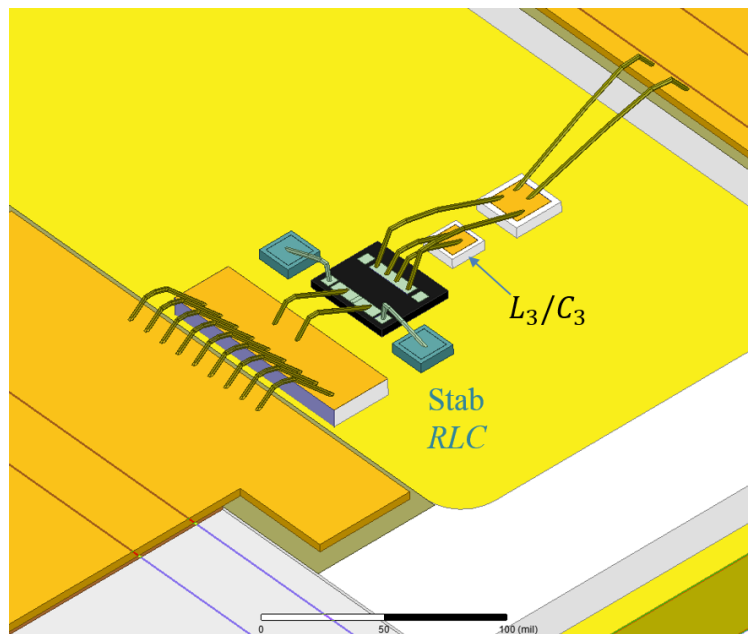


Figure 5.12: The simulated  $k$ -factor (orange) and  $G_{max}$  (blue) of the chosen GaN device over a wide range of frequencies for the scenario with (a) no stability network, (b) external stability network consisting of a parallel  $RC$  network ( $R = 20 \Omega$ ,  $C = 0.1 \text{ pF}$ ), and (c) an internal stability network by a shunt  $RLC$ . In each case, the transistor is presented with the designed gate and drain matching networks



(a)



(b)

Figure 5.13: The physical realization of the source network including internal stability network of Fig. 5.12c for 2 different manifestations of the drain network  $3f_0$  resonator: (a) without adjusting the drain network of Fig. 5.9 but with undesirable coupling between the gate and drain network, and (b) redesign of the  $3f_0$  resonator with undesirable coupling of the resonator to the drain fundamental match.

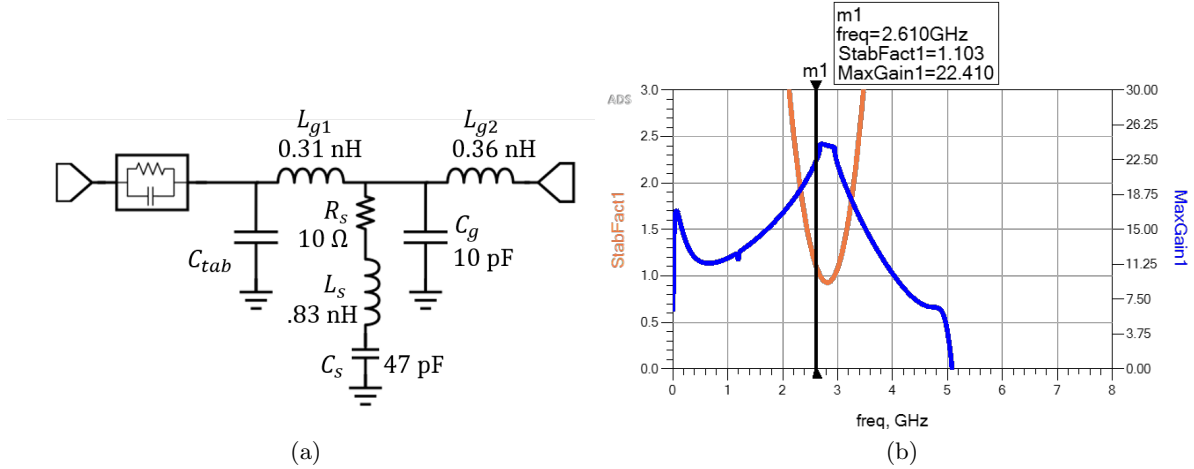
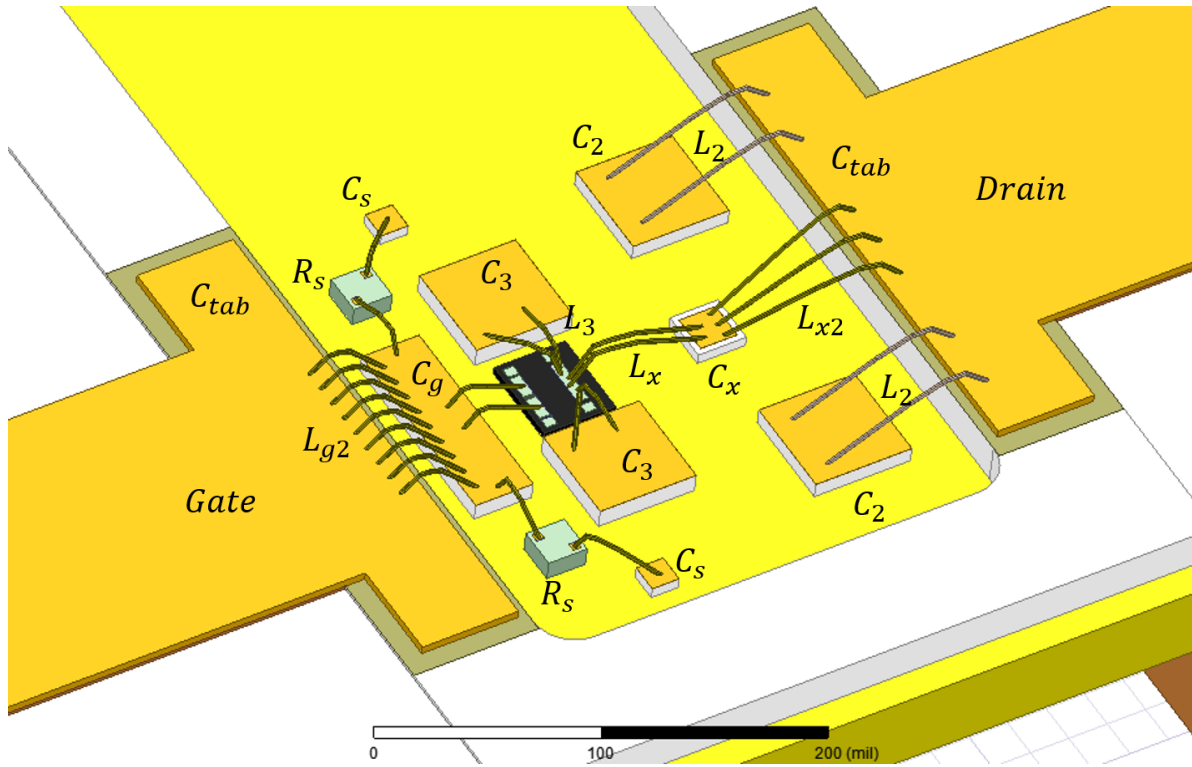


Figure 5.14: The final circuit model of the gate network including in-package stability elements (a) with the corresponding  $k$ -factor (orange) and  $G_{max}$  (blue) is plotted over a wide range of frequencies (b).

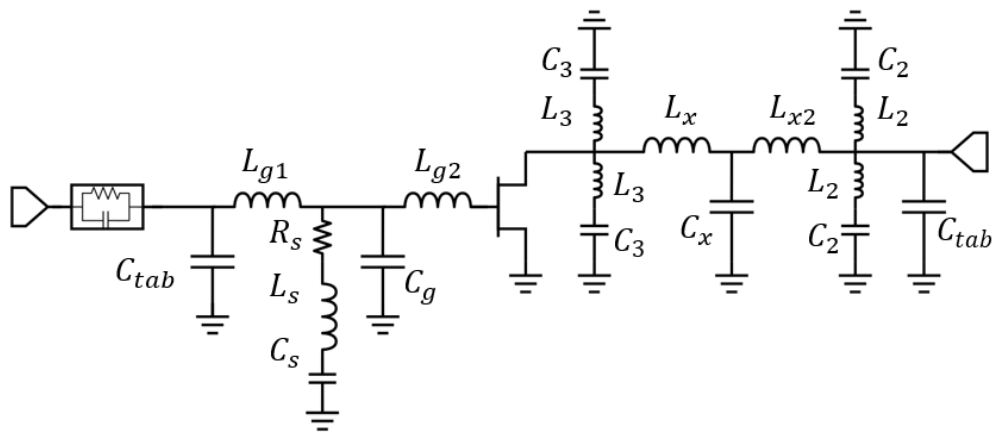
Seen in Fig. 5.13 is the first realization of the gate network including the package-internal stability network of Fig. 5.12c. Although this gate network provides unconditional stability and a good input match, in the physical scenario (Fig. 5.13a), it will couple to the drain network and thus detune all the matching networks and potentially introduce a feedback loop leading to instability. This illustrates the challenge of iterative design between harmonic balance, circuit model, and HFSS with the introduction of every element. The drain  $3f_0$  resonator can be redesigned as shown in Fig. 5.13b, however any non-perpendicular orientation of  $L_3$  and  $L_x$  results in a mutual inductance that will significantly detune the drain network match.

The input network is redesigned by introducing the stability network on the gate-side capacitor to further the distance from the drain network. This improves stability to a smaller degree than the previous iteration, therefore an external  $RC$  network must be added. Additionally, an off-chip bondable resistor is required. The revised topology and resulting  $k$ -factor are shown in Fig. 5.14. Additionally, this stability network leads to lower efficiency than the one of Fig. 5.12c.

The entirety of the GaN class- $F^{-1}$  packaged PA is shown in HFSS in Fig. 5.15 along with the equivalent circuit model. The simulated large-signal performance, using the device non-linear model and the full-wave simulations of the package networks surrounding the die, is plotted and shown in



(a)



(b)

Figure 5.15: The entire Class- $F^{-1}$  package design shown in HFSS (a) with equivalent circuit model shown in (b).

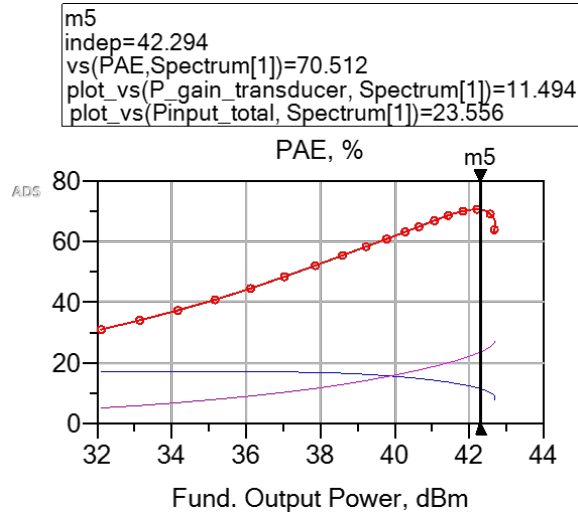


Figure 5.16: Harmonic balance simulation using the HFSS-simulated  $S$ -parameters of the package network shown in Fig.5.15a and the non-linear model device. The input power is swept and the  $PAE$  (red), input power (pink) and transducer gain (blue) is plotted.

Fig. 5.16. At the time of writing, the package is being fabricated. Measurements are forthcoming.

### 5.3 CONCLUSION

Presented in this chapter is the design of two packages, each fully matched at the fundamental frequency while also terminating the  $2^{nd}$  and  $3^{rd}$  harmonics in an open or short at the transistor virtual drain. The first of the presented packages houses an LDMOS transistor, while the second designed around a GaN HEMT. Although the LDMOS device prefers current peaking, while the GaN device prefers voltage peaking, and therefore the circuits will differ, both designs require a large degree of full-wave simulations, non-linear characterization, and design iterations.

It was seen that LDMOS is most efficient under class-F (current-peaking) conditions, which greatly benefits from in-package designs since a  $2f_0$  short-circuit impedance can be presented directly at the output of the die by designing a bond-wire/capacitor shunt resonator on the die bond-pad. However, LDMOS is ultimately limited in efficiency considering its large drain capacitance ( $C_{ds}=4.3$  pF) and therefore limited output harmonic content.

The GaN device prefers a  $2f_0$  open-circuit at the virtual drain corresponding to class- $F^{-1}$ ,

which is difficult to achieve with in-package elements since highly-reflective impedances can only be realized with low impedance circuits to ground. Large impedances with large reflection coefficients therefore must be subject to the accumulated loss of the entire in-package network, making high-fidelity open-circuit terminations difficult to achieve. Additionally, the larger fundamental output impedance of GaN proved to be a challenge for this relatively low power level since it leads to the need for larger series inductances (longer bond-wires). Interestingly, this is less of a challenge for higher power devices since the output impedance will be lower.

In addition to demonstrating fully matched PAs within a package with small size and high efficiency, a contribution of this chapter is a new type of in-package stability network which proved to be effective in stabilizing a device that could not be stabilized with external stability networks.

# 6

## HARMONIC INJECTION

### CONTENTS

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As discussed in the previous chapters, to improve efficiency of microwave power amplifiers (PAs), the active device is driven into saturation and the generated harmonics are reflected by the output matching network in such a way that voltage and current waveforms are shaped for minimal overlap during a period [73]. When sufficient harmonic content is available for waveform shaping, the device is operated in a strongly non-linear regime and needs to be linearized for low-distortion signal amplification [71]. Typically digital pre-distortion is required, adding complexity especially for wideband signals. Harmonic injection (HI) at the input has also been investigated for improving linearity for both tube [74] and solid-state [75] amplifiers. In [7], the phase and amplitude of the 2<sup>nd</sup> harmonic were chosen to optimize efficiency without regard for linearity. HI was also used to improve linearity without regard for efficiency [76]. Both efficiency and linearity improvement of a PA operating in CW mode are discussed in [77]. This improvement, however, is compared to a PA

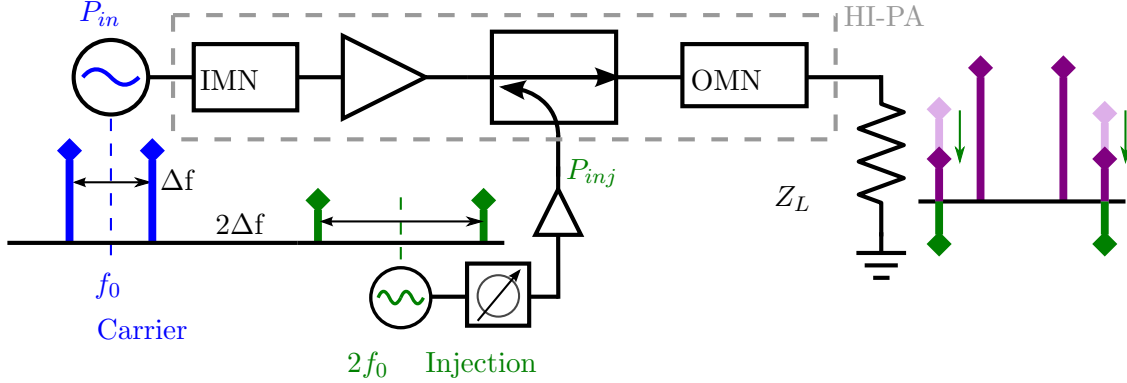


Figure 6.1: Block diagram of the HI-PA. When driven into compression with a two-tone signal, the PA operates efficiently but not linearly. By injecting into the output a two-tone signal with a doubled carrier frequency ( $2f_0$ ) and tone spacing ( $2\Delta f$ ),  $IMD_3$  can be reduced while maintaining efficiency through waveform shaping.

that does not include harmonic terminations.

To demonstrate the advantages of an HI-PA, this work directly compares PA performance with passive and active  $2^{nd}$  harmonic terminations. A harmonically-terminated PA is designed to maximize power-added efficiency ( $PAE$ ) and then measured under load-side harmonic injection (Fig. 6.1) to demonstrate an improvement in linearity while maintaining high efficiency. The phase and amplitude of the injected signal are dynamically adjusted during power sweeps showing reduction in AM/AM distortion. With a two-tone input signal of varying separation, a reduction in third-order intermodulation distortion ( $IMD_3$ ) by more than 10 dB is achieved while maintaining drain efficiency  $\eta_D = 93\%$  at peak power for the main PA. For this operating point, the total efficiency, which includes the input powers at the fundamental and  $2^{nd}$  harmonic, is measured to be 80%.

## 6.1 HI-PA DESIGN

The main PA at 2.2875 GHz is designed with a packaged Wolfspeed 10-W GaN HEMT CGH40010F. We consider a 6-MHz signal bandwidth for the target application NASA's S-Band Space Network channel. The device is biased in Class AB ( $V_{DD} = 28$  V,  $I_{DQ} = 67$  mA) and the output matching is designed as a trade-off between PAE and output power using load-pull. A 3-port injection network is integrated into the HI-PA matching network to allow  $2f_0$  injection without affecting  $f_0$



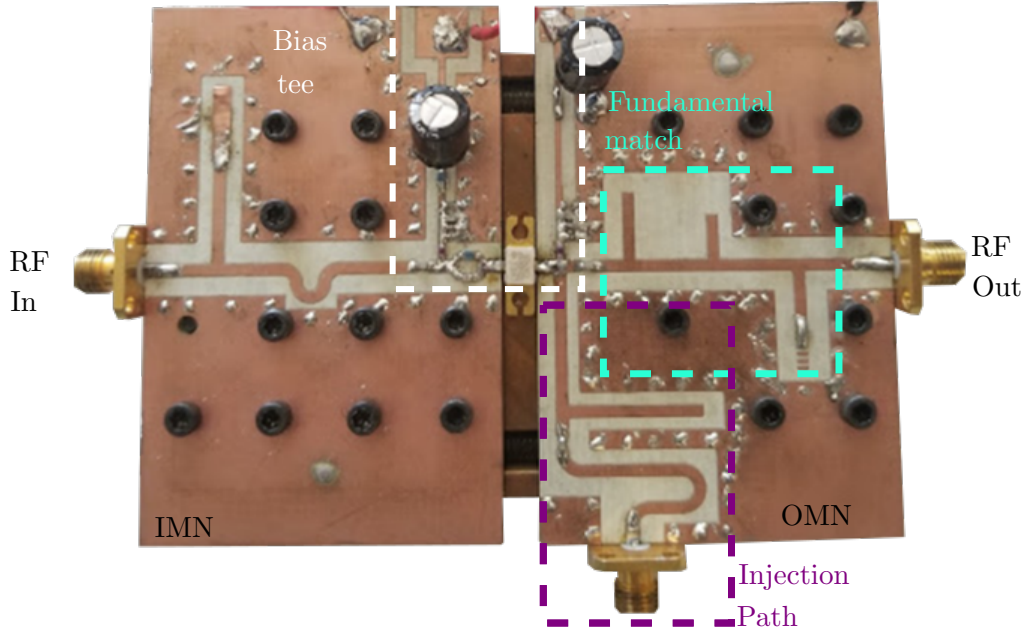


Figure 6.2: Photograph of the fabricated 2.3-GHz HI-PA on Rogers 4350B substrate and copper baseplate. The board size is 106 mm  $\times$  76 mm.

impedance, Fig. 6.2. The PA was tested alone and with the  $2f_0 = 4.575$  GHz injection path enabled and the results compared in experiment.

### 6.1.1 BIAS-TEE DESIGN

Considering the significant  $2f_0$  content in the drain circuit, the bias network (Fig. 6.3) is designed to have a high impedance at both  $f_0$  and  $2f_0$ . Furthermore, for minimal impact on the injected signal, the impedance at  $2f_0$  should be close to an open-circuit impedance. This is achieved by choosing  $L_b$  to be the Coilcraft 0603CS 5.6 nH inductor considering that the parasitic capacitance between the inductor windings in parallel with the self inductance resonates at  $2f_0$ . The simulated impedance presented by the bias line to the RF path is shown in Fig. 6.4. Shunt capacitor  $C_b$  with a series resonance at  $f_0$  serves to short any fundamental content beyond the RF choke. The  $DC$ - $RF$  isolation of the designed bias network, Fig. 6.3, is achieved through careful layout with electromagnetic co-simulations.

The baseband impedance of the bias-tee must be as small as possible in order to minimize memory effects induced by the bias line [78]. An inductor is used instead of a quarter wavelength

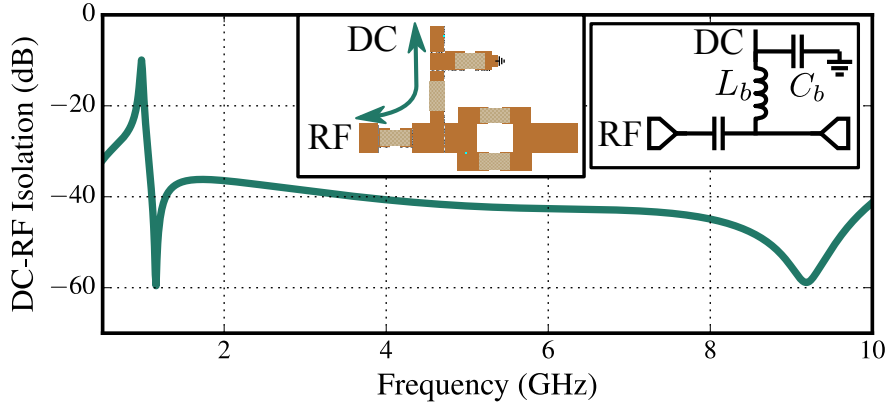


Figure 6.3: Isolation between the DC and the RF path from 0.5 to 10 GHz, showing a high bias-line impedance across a bandwidth of greater than 10 GHz (including up to  $3f_0$ ).

line in order to increase the bandwidth of the bias tee, but the windings of the inductor will increase resistance. However, since the self-resonance of an inductor is inversely proportional to its self-inductance [79], the choice of a bias-line inductor with a resonant frequency at  $2f_0$  leads to fewer windings (lower baseband impedance) than the traditional approach of using an inductor with an  $f_0$  resonance. Consider the bias tee in Fig.6.3 where  $L_b$  has a parallel resonance of  $f_0$  instead of  $2f_0$  by using a 27 nH inductor instead of a 5.6 nH inductor of the same Coilcraft series. The baseband resistance of the bias line for this case is compared in Fig.6.5 to the designed bias line. In using the  $2f_0$  resonant inductor, the baseband resistance remains below  $0.2\Omega$  from DC to up to 5 times the signal bandwidth. Although both choices of  $L_b$  lead to a high bias-line impedance at the design frequency, the baseband characteristic of the designed bias-line is more desirable for improved PA linearity performance.

### 6.1.2 OUTPUT NETWORK DESIGN

Simulated source-pull (SP) and load-pull (LP) are performed in Keysight ADS with the manufacturer-provided nonlinear model. Since the bias network affects the fundamental impedance, a two-tone 10-MHz load-pull is performed with a reference plane located after the bias tee and the results for PAE and  $IMD_3$  are shown in Fig. 6.6. The matching network is implemented on microstrip Rogers 4350B 30-mil substrate and the input is matched for gain.

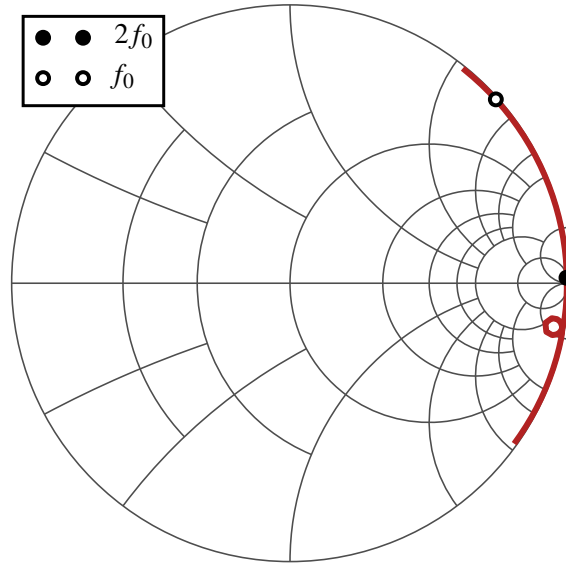


Figure 6.4: The impedance presented by the bias line to the RF path, plotted from 2 to 10 GHz. The bias line is high-impedance over a large range of frequencies, with  $2f_0$  near an open circuit.

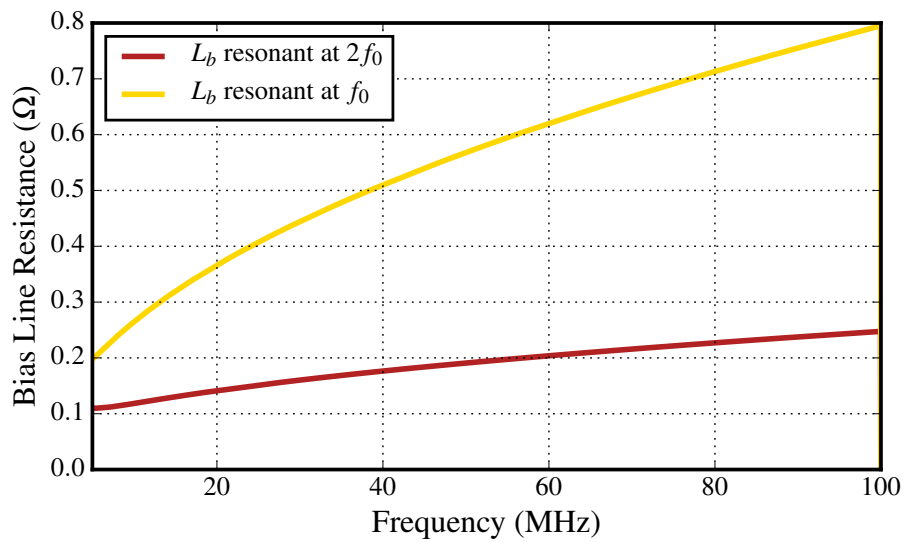


Figure 6.5: The baseband resistance of the bias-line for the case where  $L_b$  is parallel resonant at  $f_0$  (red) and  $2f_0$  (yellow). Although both choices of  $L_b$  lead to a high bias-line impedance at the design frequency, the latter results in a bias-line that has a 2-3 times lower baseband impedance than a traditionally designed bias-line.

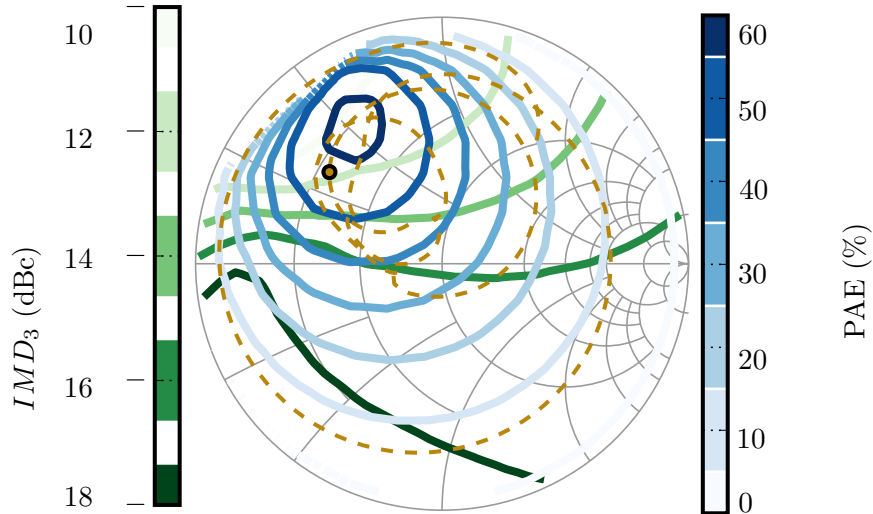


Figure 6.6: Simulated 10-MHz spaced two-tone LP PAE and  $IMD_3$  contours at the reference plane between the bias-tee and the PA output. The  $S_{11}$  of the EM-simulated matching network is also plotted from 1-8 GHz (gold dashed) with a marker (gold circle) at the design carrier frequency.

The  $2f_0$  is injected through a diplexing network that presents an open at  $f_0$  and a passive  $2f_0$  terminated at the device drain. The microstrip network together with an unloaded (open) SMA connector is designed to terminate the  $2^{nd}$  harmonic in a high-efficiency region of the load-pull contours. Therefore, by disconnecting the  $2f_0$  injection source, a direct comparison can be made between a PA with passive and active harmonic terminations. With  $50\ \Omega$  connected to the injection path, the  $2^{nd}$  harmonic is pre-matched to  $47\ \Omega$  during  $2f_0$  injection. The injection path includes a DC block, and is meandered to fit the OMN within a  $2'' \times 3''$  form factor. The  $S$ -parameters of the injection path are plotted in Fig. 6.8. A bandwidth-limiting factor for harmonic injection lies in the bandwidth of the diplexor and therefore input and injected signal bandwidth must be considered in the diplexor design. Additionally, it is desirable in terms of linearity that the diplexor presents similar transmissive and reflective behavior across the entire bandwidth. The designed diplexor provides reflection coefficients of  $-25\ \text{dB}$  across a  $60\ \text{MHz}$  bandwidth at each band ( $f_0$ ,  $2f_0$ , and  $3f_0$ ).

The  $2^{nd}$  harmonic must be introduced as close to the device as possible to minimize injection signal attenuation and therefore the required injected power. The simulated impedance of the entire drain network under both conditions (loaded and unloaded injection port) is shown in Fig.

6.9, also showing the impedance at  $2f_0$ . The  $3^{rd}$  harmonic is terminated for peak efficiency and the injection path does not affect its impedance.

Since the device is biased in a class-AB bias, significant  $2f_0$  power will be generated. By additionally injecting external harmonic power, an active impedance is synthesized at the  $2^{nd}$  harmonic and therefore can present impedances outside of the unity radius Smith chart. In Keysight ADS harmonic-balance, the  $2f_0$  power and phase was swept. An ideal lossless directional coupler is placed at the device output in order to sample separately the  $2f_0$  power from the device and the injected  $2f_0$  at the device plane. With the phase and amplitude of the generated and injected harmonic sampled, the actively synthesized impedance can be determined. The  $\eta_{total}$  was then simulated during the injection sweeps (assuming  $\eta_{inj}=50\%$ ) to produce the injection contours shown in Fig. 6.7.

## 6.2 HI-PA MEASUREMENTS

A setup based on two synchronized National Instruments VSTs is used to characterize the HI-PA. An external RF source (HP 83650A) generates the  $f_0$  carrier, which is locked to the local oscillator of a VST. The first VST is locked at  $2f_0 = 4.575$  GHz, derived from  $f_0$  with a frequency multiplier (Mini-Circuits ZX90-2-36+) and an high-pass filter (Mini-Circuits VHF-3800+). In this way, two carriers,  $f_0$  and  $2f_0$ , are phase-coherent and phase-aligned. The RF generation and acquisition (after calibrating the VSTs), are synchronized with a trigger and a 10 MHz reference clock. An instrumentation driver (Mercury Systems SM0825-40) amplifies the  $f_0$  signal up to 29.5 dBm at the PA input. The second signal at  $2f_0$  is amplified by a bench-top driver (Keysight 83020A). The measured CW performance with the injection port unloaded (passive  $2f_0$  termination) is plotted from 2 to 2.4 GHz in Fig. 6.10, demonstrating  $G = 12$  dB,  $P_{out} = 41.5$  dBm, and  $\eta_D = 72\%$  at the design frequency.

To account for the input DC power, as well as the powers at  $f_0$  and  $2f_0$ , we define a total

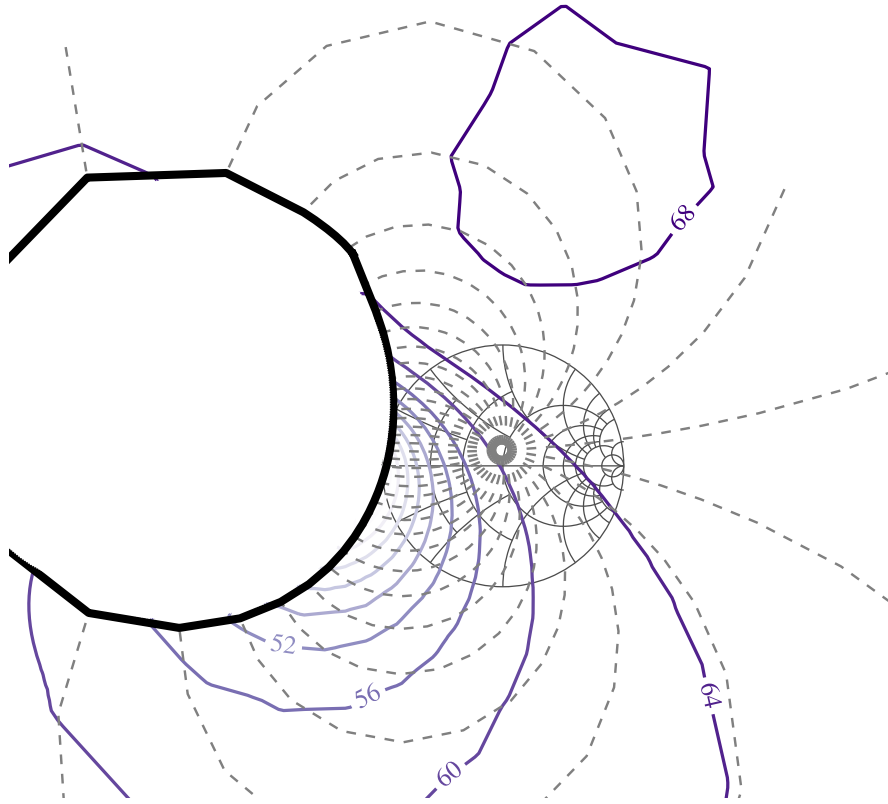


Figure 6.7: Simulated  $\eta_{total}$  contours (assuming  $\eta_{inj}=50\%$ ) constructed by sampling the forward and backward  $2f_0$  power at the device plane. The dotted lines indicate constant injected phase. With no injection, the  $2^{nd}$  harmonic impedance assumes the passive  $47\ \Omega$  passive pre-match impedance.

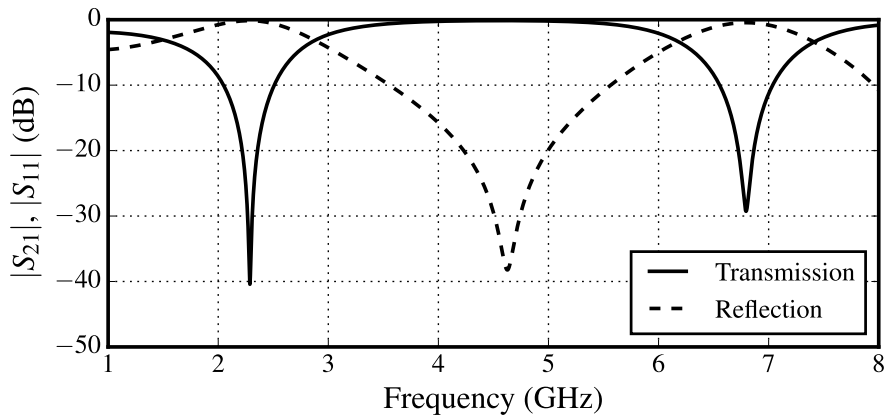


Figure 6.8: S-parameters of the injection path showing diplexing characteristic of the OMN. The injection path presents an open at  $f_0$  and  $3f_0$ , while presenting  $50\ \Omega$  at  $2f_0$ .

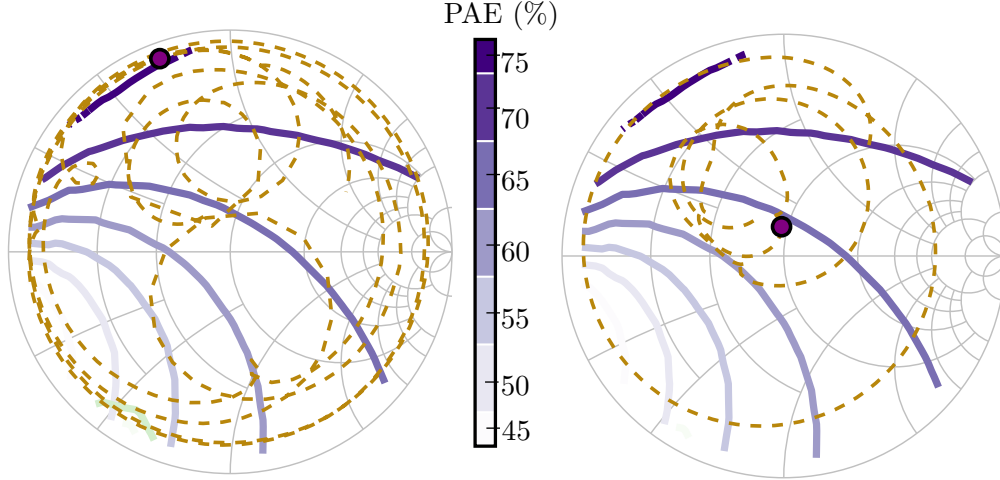


Figure 6.9: The  $2f_0$  PAE contours are plotted with a continuous line (purple). The impedance presented by the output network including the injection port SMA connector when the injection port is unloaded (left) and loaded (right) is plotted from 2-8 GHz (gold, dashed trace), with  $\Gamma_{2f_0}$  marked by a circle (purple).

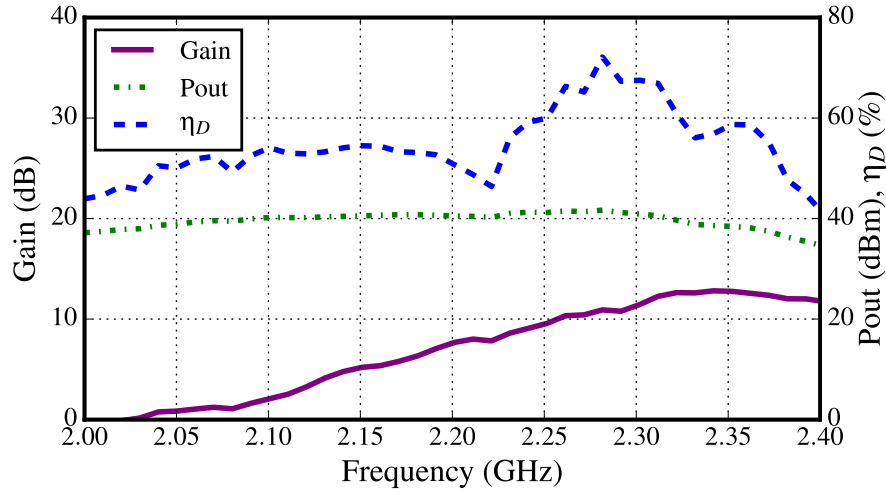
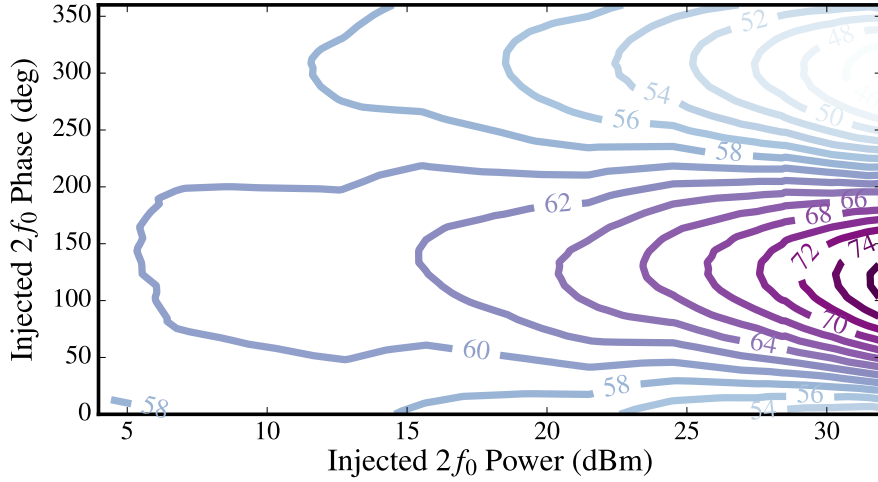


Figure 6.10: Measured CW gain,  $P_{OUT}$ , and  $\eta_d$  of the PA. The efficiency of the PA is fine-tuned to peak at the targeted frequency  $f_0 = 2.2875$  GHz.

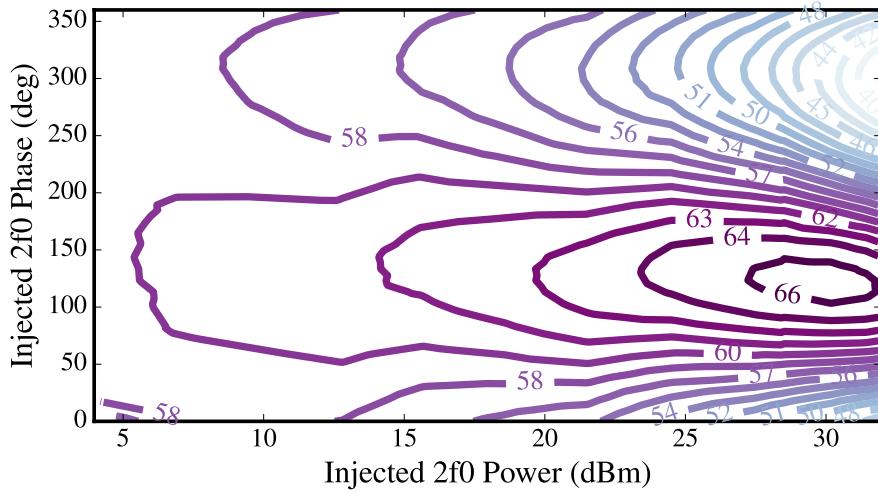
efficiency  $\eta_{total}$  as:

$$\eta_{total} = \frac{P_{out}(f_0)}{P_{dc} + P_{inj}/\eta_{inj}} \quad (6.1)$$

where  $P_{inj}$  is the injected  $2f_0$  power and  $\eta_{inj}$  is the drain efficiency of the injection path active components. With injection enabled, the measured  $\eta_{total}$  as a function of injected phase and amplitude is shown in Fig. 6.11 for two values of injection-path efficiency:  $\eta_{inj} = 100\%$  and  $50\%$ .



(a)



(b)

Figure 6.11: Measured contours of constant  $\eta_{total}$  assuming an injector efficiency of (a) 100% and (b) 50%, with swept injected phase and power at a fixed CW input signal at 30 dBm. Note that lower injected power is necessary to reach the maximum  $\eta_{total}$  when considering a non-ideal  $2f_0$  injection.

For a 50 point reduction in  $\eta_{inj}$ , total efficiency reduces by seven points and the maximum  $\eta_{total}$  contour is achieved at a lower  $P_{inj}$ . Additionally, the  $\eta_{total}$  contours can be related to  $P_{out}$  contours plotted in Fig. 6.12 to show that  $2f_0$  injection can also increase  $f_0$  output power by improving the efficiency of the main PA.

Referring to Fig. 1, a two-tone signal at  $f_0$  with  $\Delta f$  spacing is input to the PA, while a second two-tone signal, centered at  $2f_0$  and with  $2\Delta f$  spacing, is concurrently injected at the HI port.



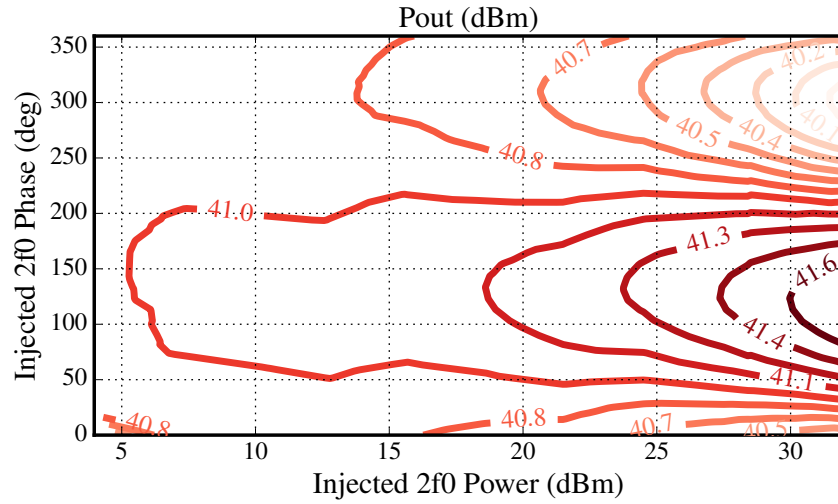


Figure 6.12: Measured contours of constant  $P_{out}$  with swept injected phase and power at a fixed  $f_0$  CW input signal at 30 dBm, showing injection can affect  $f_0$  output power by improving efficiency.

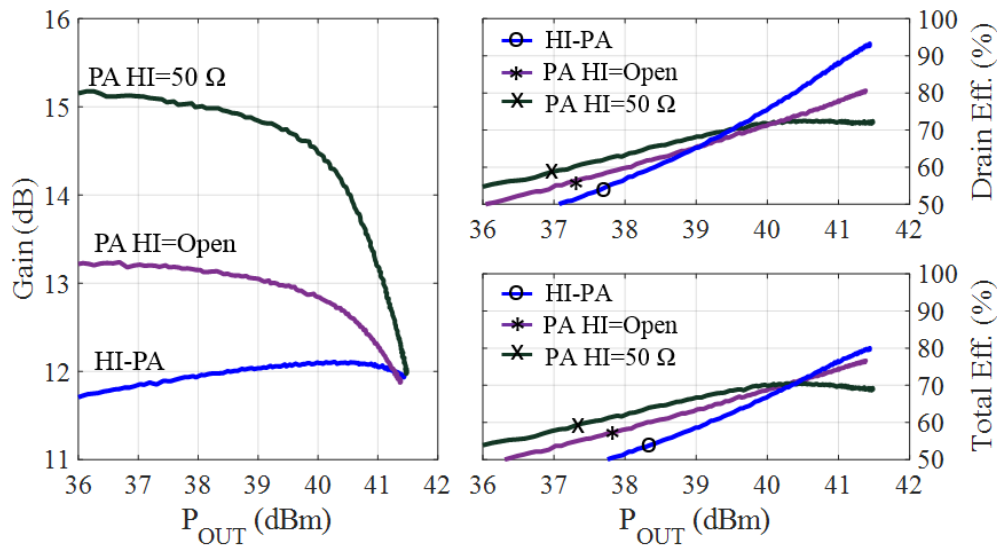


Figure 6.13: Measured modulated gain, drain and total efficiency of the amplifier at  $f_0$  with and without  $2^{nd}$  harmonic injection (open and  $50\ \Omega$  load on the HI port). Both the main and injected signals are amplitude modulated. When HI is employed, the gain is flatter while the efficiency is also improved as a result of waveform shaping with  $2^{nd}$  harmonic.

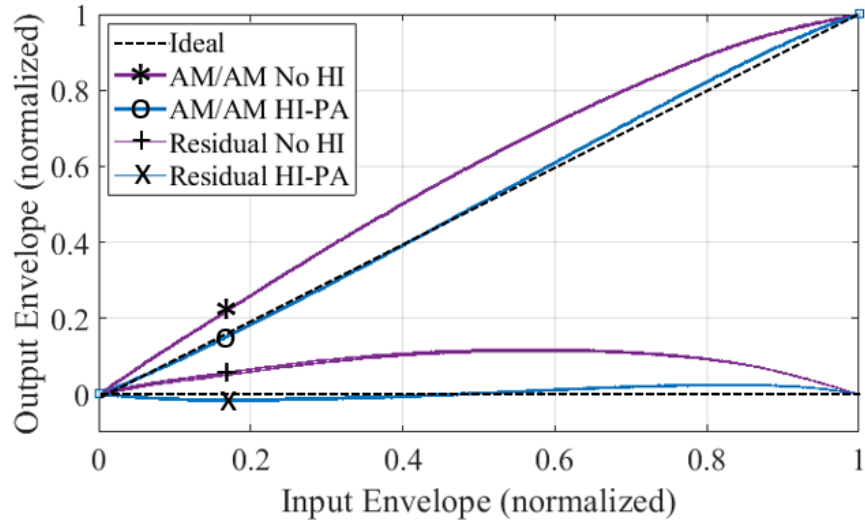


Figure 6.14: Normalized AM/AM characteristics of the PA with and without HI. The significant AM/AM distortion can be mitigated by  $2^{nd}$  harmonic injection. After HI, the residual distortion shows an odd-order nonlinearity that can be reduced with injection of higher order harmonics.

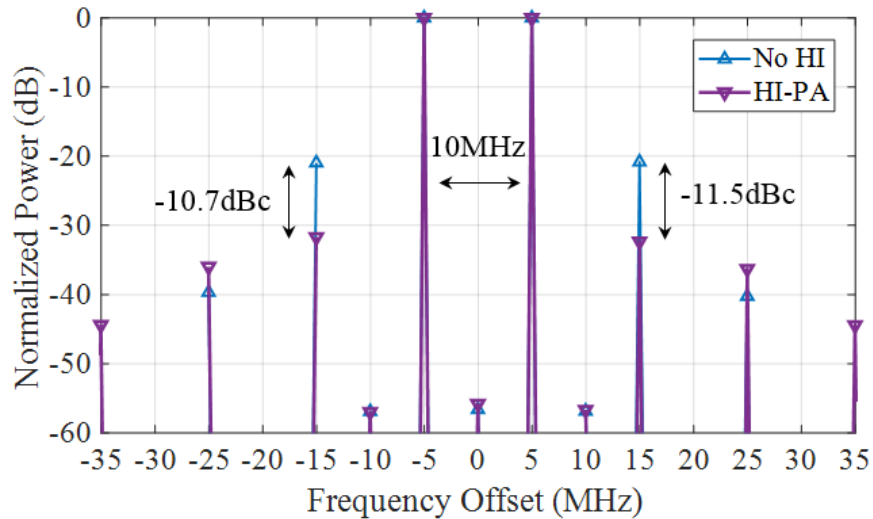


Figure 6.15: Normalized spectra showing a two-tone test at  $f_0$  with 10 MHz spacing and  $P_{OUT,MAX} = 41.5$  dBm. More than 10 dB improvement in the  $IMD_3$  is demonstrated by injecting a two-tone signal with 32 dBm power at  $2f_0$  while the upper  $IMD_5$  is below 30 dBc.

In this case, both the main and injected signals are amplitude modulated with a 3-dB peak-to-average ratio (PAR), resulting in higher efficiencies when compared to CW measurements because of the lower PA temperatures. The large signal performance, with and without HI, is shown in Fig. 6.13. With HI, gain is shown to be linearized with a maximum variation of  $\sim 0.3$  dB, while  $\eta_D$  and  $\eta_{total}$  at higher output power also improve as a result of waveform shaping. Measurements are also performed with the injection path unloaded, when it presents a passive  $2f_0$  termination as indicated by Fig. 6.9. Additionally, the PA is characterized for the case when the path is loaded with  $50\ \Omega$  and presents near- $50\ \Omega$  at  $2f_0$  to the device. These two passive harmonic loading conditions are compared directly to HI in Fig. 6.13.

### 6.3 LINEARITY MEASUREMENTS

The HI-PA linearity is studied with the normalized AM/AM plot of Fig. 6.14. Here, the compressing behavior of the PA is significantly reduced with HI as also visible in the residual AM/AM distortion. Note that the injected signal at  $2f_0$ , identical to the signal at  $f_0$  but with twice the bandwidth, reduces most of the compression, but injection of the  $3^{rd}$  harmonic is required to remove the residual distortion. Linearity is also verified in the frequency domain, Fig. 6.15, where the  $IMD_3$  products are reduced more than 10 dB while the  $IMD_5$  products remain below 35 dBc. Similar results are obtained for tone spacing from 100 kHz up to 10 MHz.

### 6.4 CONCLUSION

A high-efficiency GaN PA is designed with harmonics terminated passively using traditional elements such as microstrip lines and stubs. An unloaded SMA connector at an edge of the PA board is included in the design of the  $2f_0$  impedance that is terminated in a high-efficiency region of the Smith chart. The drain network is designed such that when the connector is loaded with a  $50\ \Omega$  system (e.g., another PA), the  $2f_0$  impedance returns to near- $50\ \Omega$ , serving as a  $2f_0$  pre-match for active impedance tuning. Under injection, an actively synthesized  $2f_0$  impedance is presented to

the device. By designing the drain network to present either a passive or active  $2f_0$  termination, the advantages and disadvantages of an HI-PA can be directly observed.

Although the scope of this work does not include the design of the active components which generate the  $2f_0$  injection, the theoretical efficiency of this path is considered in the calculation of the total HI-PA efficiency where it is seen that reducing  $\eta_{inj}$  from 100% to 50% reduces  $\eta_{total}$  by only 7 points while reducing the  $P_{inj}$  required for maximum  $\eta_{total}$  from 32 dBm to 29 dBm (3 dB reduction).

With an active  $2f_0$  termination, 2 dB greater gain and 3 points greater  $\eta_{total}$  are measured at peak power, assuming  $\eta_{inj} = 50\%$ . With a passive termination, the efficiency is greater at  $> 3$  dB backoff, however  $IMD_3$  is 10 dB greater. The AM/AM distortion is significantly reduced in the HI case, and any further reduction in distortion would require injection of the  $3^{rd}$  harmonic in addition to the  $2^{nd}$ . It has been shown that with harmonic injection, it is possible to achieve significantly lower  $IMD_3$  and AM/AM distortion for a two-tone modulated signal while maintaining the high efficiency of a harmonically-terminated PA. However, the  $\eta_{inj} = 50\%$  assumption may be difficult to achieve in practice considering that the injected power is at a doubled carrier frequency and is comparable in power to the  $f_0$  output. Achieving a sufficiently high  $\eta_{total}$  would likely involve careful co-design of the  $2f_0$  injector and the rest of the transmitter, where frequency upconversion and signal amplitude/phase control already occurs. Although this work provides insight into the main PA performance, the feasibility of maintaining high system efficiency, particularly with carrier frequencies beyond S-band, must be evaluated further.

# CONCLUSIONS AND FUTURE WORK

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## 7.1 THESIS SUMMARY AND CONTRIBUTIONS

Microwave power amplifier efficiency is challenged by parasitic reactances and loss between the design plane and the virtual drain, where theory for high-efficiency design is directly applied. The efficiency of active devices is often limited by the packaging or interconnect from the device to the rest of the system. In this work, the design plane is shifted closer to the virtual drain to enable greater control of harmonic impedances. In Chapters 1-3, the active and passive networks between the virtual drain and lead of a transistor package are modeled and characterized, including a discussion of the limitations of commercial packages on efficiency. There is a general understanding that packaged devices suffer from lower efficiency, but a comprehensive analysis can currently not

be found in the open literature. The goal of this thesis is to present methodology to any package and transistor with a known geometry and non-linear model.

With the active and passive package environment modeled, considerations for the design of in-package matching networks are explored in Chapter 4. A package design which allows greater external harmonic control is presented along with active multi-harmonic load-pull. The contributions of this work to in-package PA design are then described. Specifically, highly reflective and precisely phased  $2f_0$  impedances using in-package elements and parasitics are analyzed in theory and demonstrated in measurement, and published in [56]. By doing so, an LDMOS PA with package-internal matching is measured to have a state-of-the-art efficiency for an LDMOS-based PA above 2.4 GHz.

Due to the small size of transistor packages, when designing in-package PAs, electromagnetic coupling has a major effect and is difficult to fully take into account. Therefore there is a need to measure and verify harmonic impedances presented to the drain of a die by in-package networks and this work demonstrates a verification method in which the active device is replaced by a capacitor of similar size and known value.  $S$ -parameter measurements of the fabricated purely passive package can be directly compared to full-wave simulations up to the highest harmonic frequency and a technique is published in [57] and [80]. This work was recognized by a Best Student Research Paper award at IEEE WAMICON 2018.

A complete PA matching network including a complex fundamental match and  $2^{nd}$  and  $3^{rd}$  harmonic terminations is fully realized with 3-dimensional elements and presented in Chapter 5 with both an LDMOS and GaN device without the need for external, PCB matching. A compact LDMOS PA with in-package class- $F$  impedances is demonstrated at 1 GHz with harmonic control at 2 and 3 GHz at 10-W output power. This technique is extended by application to a 25-W GaN device at 2.6 GHz where the increased harmonic control takes advantage of the greater harmonic content of GaN devices. Both designs demonstrate for the first time control of up to 3 harmonics within a package. By fully matching a transistor to up to its  $3^{rd}$  harmonic within a package, we illuminate the need for an in-package stability network. A solution for stability using only bond-

wires, and bondable resistors and capacitors, is shown for the first time. This work is discussed in [80].

This thesis also presents a PA design which allows the direct comparison of efficiency and linearity performance of a packaged GaN device with passive and with active harmonic terminations. The drain network integrates a diplexing network, a  $3f_0$  termination, an  $f_0$  match and output port, and a  $2f_0$  input port. With  $2f_0$  input port unloaded, the  $2^{nd}$  harmonic is passively terminated in a high-*PAE* region of the unity Smith chart. When loaded,  $50\Omega$  is presented to the device, serving as a pre-match for the active impedance sweeps. The active terminations are achieved by injection of an external source with doubled the carrier frequency and bandwidth. The injected  $2^{nd}$  achieves waveform shaping through active impedance synthesis while also reducing in-band distortion products. Under injection, the PA was seen to have 10 dB lower *IMD*<sub>3</sub> and reduced AM-AM distortion while maintaining a similar total efficiency as in the passively-terminated mode. The results of this work is published in [81].

Other contributions of this thesis include a series of non-standard multi-harmonic measurements. Passive load-pull with harmonic terminations within the calibration standards was used for determining package limitations. Specialized active harmonic LP was applied validation of non-linear models, and included the design bias networks within the calibration standards which presented high impedances up to the highest harmonic. This was also applied to harmonic injection, which can also be viewed as active LP at the  $2^{nd}$  harmonic. Then unique setup for harmonic injection was developed with necessary phase alignment, phase-coherent doubled-frequency injection, including basband and carrier frequency. In this experiment, the de-embedding of power and impedance measurements of a drain network with 2 output ports was a key development in the design of a harmonic injection PA.

The general microwave knowledge was related to other topics, including a dual-band high-efficiency PA [82], PAs for a multi-moded wireless powering cavity [83], and an efficient PA for CubeSat transmitters [84].

## 7.2 FUTURE WORK

Ultimately the work presented in this thesis was on the intentional and precise design of bond-wires and package parasitics at high frequencies, which has a wide variety of applications. Most active devices require transition to PCB circuits.

It is of interest to apply in-package matching techniques to higher power applications. The work presented scales well with output power in GaN since higher power devices have lower output impedances, and since it was seen that packages present low impedance parasitics. It is easier for the in-package network design to match the low impedance of the die to the low impedance of the package. A smaller series inductance is required, which results in more practical bond-wires. This was seen in practice in Chapter 5 where the series inductances necessary to achieve the fundamental match for the LDMOS device was much smaller than those required to match the GaN device.

The scaling of this work to higher powers is further illustrated in Fig. 7.1. The drain network can be modeled by a parallel shunt resistor  $R_p$  and capacitor  $C_p$ . Generally speaking, transistor output power increases as the number and length of parallel gate/drain fingers increase, which will in turn increase  $C_p$  and decrease  $R_p$ . Considering a typical power density of LDMOS devices, the drain equivalent circuit with scaleable  $R_p$  and  $C_p$  is shown in Fig. 7.1. The scaling factor  $x$  is swept and plotted. Package size also increases as output power increases (more parallel transistors, larger peripheries) and therefore  $C_{tab}$  will also increase. As can be seen in this figure, the output impedance of a transistor and the input impedance of simple in-package network converge to each other in higher power scenarios.

The methodology of designing in-package networks is not restricted to matching networks of single-ended amplifiers. The same principles may be used to explore using bond-wires and capacitors to power combine multiple transistors within a package. This would be more advantageous than doing so outside of the package since the transistors could be power-combined more directly, without the loss of power or of impedance control as is seen with traditionally packaged devices. Similarly, this work has plentiful applications in load-modulated PA topologies, such as outphasing or Doherty



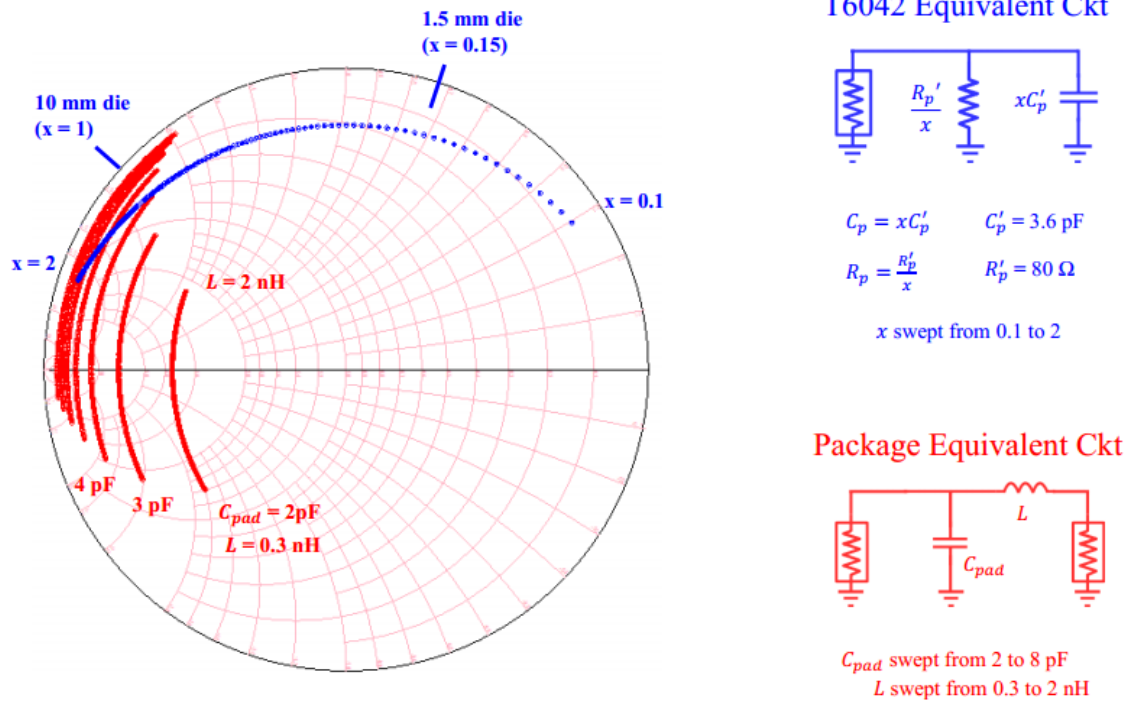


Figure 7.1: A scalable circuit model of a transistor drain is shown in blue, with values fit from a typical power density of LDMOS devices. The output impedance of the model as the scaling factor  $x$  is swept is plotted on the Smith chart in blue. This is related to the input impedance of a load-side package network, with  $C_{tab}$  increasing as package size increases.

PAs.

Many practical challenges were faced by using traditional in-package elements. For example, an inductance of 1.6 nH was needed in series for the design of the class- $F$  package. This relatively high inductance could only be realized with a single, large bond-wire, which in turn limited the current handling capabilities of the PA. Seen in Fig. 7.2 was the result of a fused bond-wire during large-signal operation. Another challenge is fabrication error. Shown in Fig. 7.4 is a scenario where there was an error in the assembly drawing (Fig. 7.3) for the package design which led to a misplacement of a capacitor in the low-pass filter match. With the series bond-wire  $L_{s0}$  fixed in length by the assembly drawing document, the loop height of the wire was lower than expected in simulation. The inductance of  $L_{s0}$  was 0.2 nH lower than desired, although ultimately did not noticeably affect the 1 GHz  $f_0$  match. Future work includes seeking elements alternative to bond-wires to realize desired inductances.

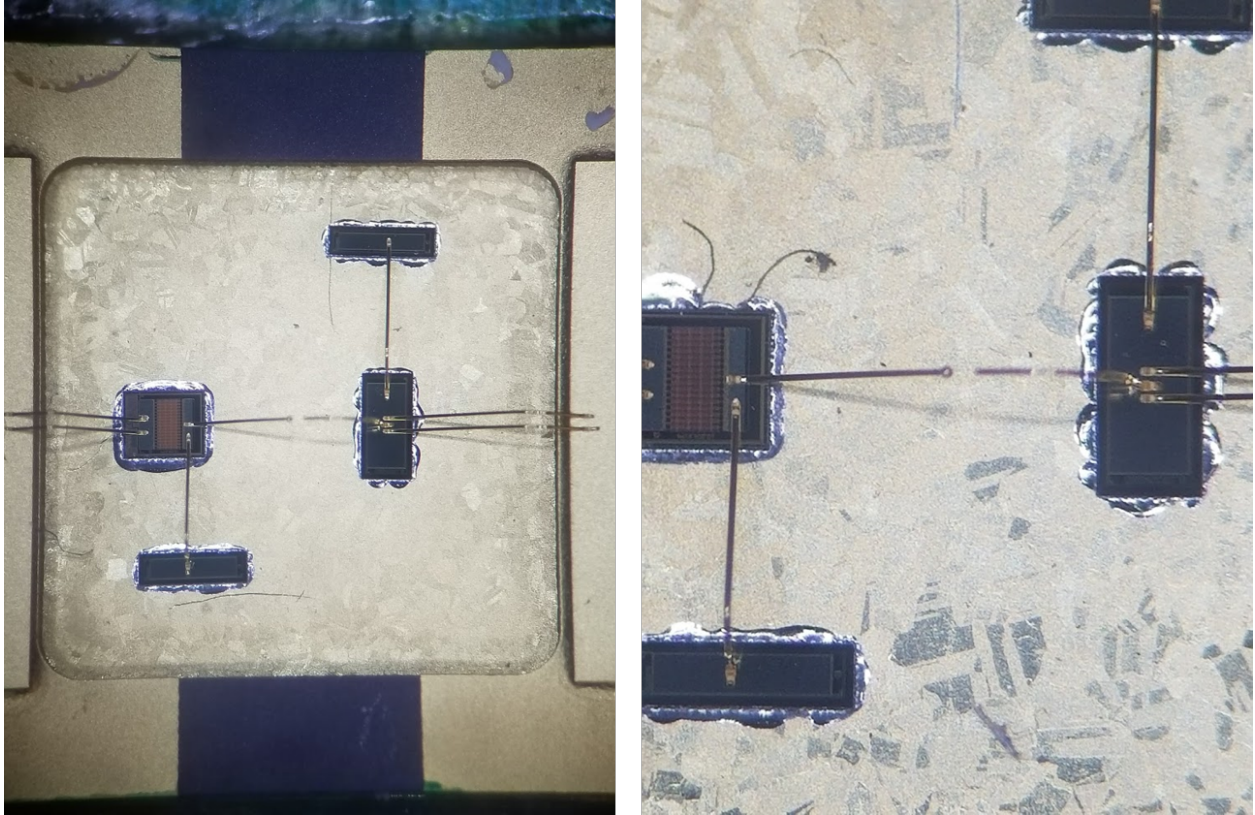


Figure 7.2: Photo of a series bond-wire melted during large-signal operation due to the limited current handling capabilities of series bond-wire inductances of greater than approximately 1 nH.

In-package networks could be made even more effective using alternative in-package components. The technique was limited by fact that bond-wires are small-valued inductances, non-rigid, and relatively lossy, serving as low- $Q$  inductors. An alternative to bond-wires with higher- $Q$ , lower loss, higher inductance could enable greater control of impedances within a package. A good solution is seen in the new inductors becoming available from 3D Glass [85], which have high  $Q$  factors since the inductors are realized with thick copper lines placed on glass (Fig. 7.5) and looped either in a single plane or 3-dimensionally. They also provide a much larger range of inductances than can be realized with a bond-wire and are small enough to fit within a standard transistor package.

Related to the active harmonic injection described in Chapter 6, basic signal performance was demonstrated with a simple two-tone signal. Although this is useful for quantifying linearity, in a real application the baseband signal would need to be up-converted with a  $2f_0$  LO and pre-processed

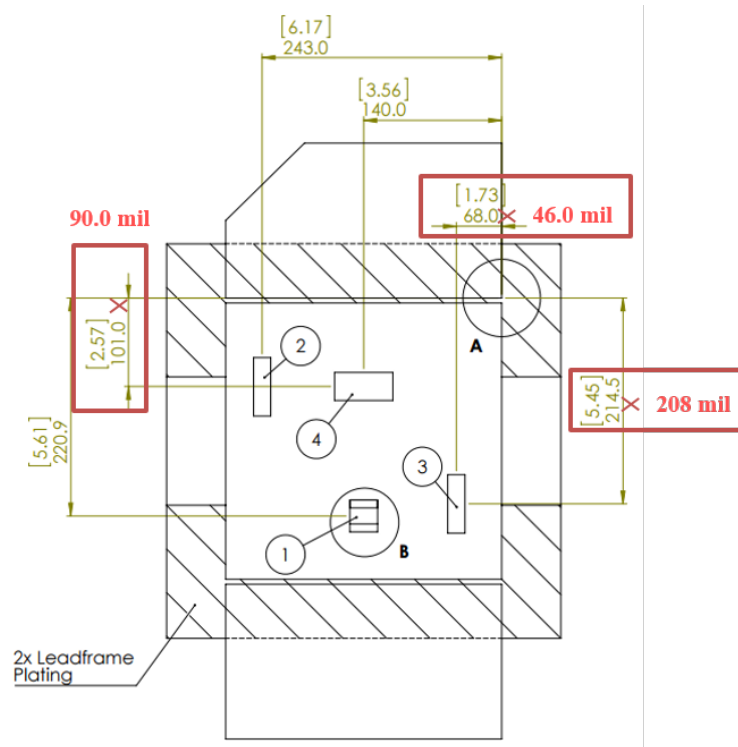


Figure 7.3: Assembly drawing of the Class- $F$  design, with contradicting dimensions made by designer error leading to fabrication inconsistency with the initially simulated design.

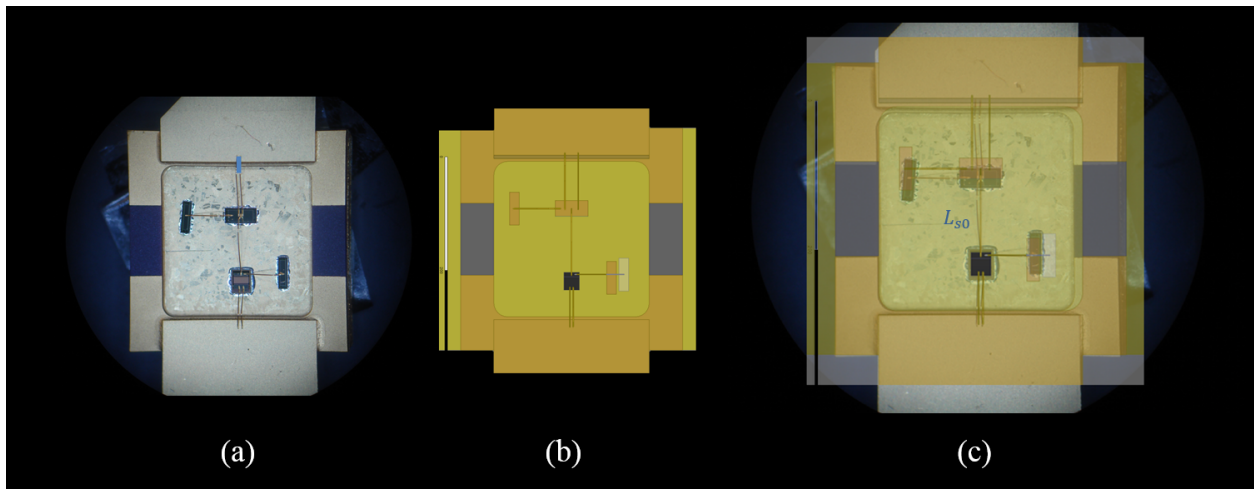


Figure 7.4: The result of the assembly drawing error shown in Fig. 7.3, with (a) photograph of the assembled class- $F$  package, (b) the intended design in HFSS, and (c) the HFSS image superimposed with the fabricated package. The erroneous placement of a capacitor led to a lower bond-wire loop height than expected and therefore a  $0.2 \text{ nH}$  lower inductance of the  $L_{s0}$  inductor.

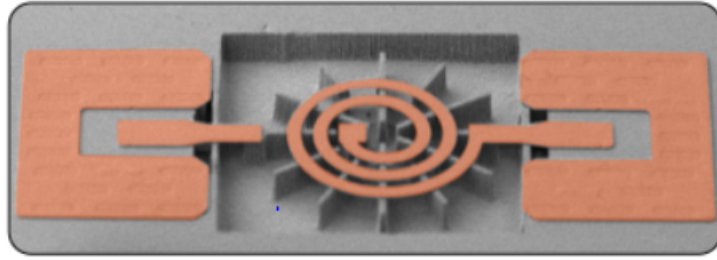


Figure 7.5: SEM of a planar spiral inductor from 3D Glass with a  $50\ \mu$  wide copper spiral supported by  $20\ \mu$  wide glass rails.

to take twice the bandwidth. Integration of circuitry that enables these functions along with a  $2f_0$  driver in the injection path would be interesting avenues for future. Furthermore, redesign of a harmonically-injected in a non- $50\ \Omega$  to reduce the required injected power, thereby improving overall efficiency.

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## APPENDIX A

# COMPACT HIGH-GAIN CUBESAT ANTENNA

The trend in increasing complexity and scope of CubeSat missions has driven a need for transmitters that enable greater link distances, higher data-rates, and more sophisticated modulation schemes. NASA's Space Network and Deep Space Network provide the communication infrastructure necessary to satisfy this trend, however CubeSats currently lack the capabilities to utilize this infrastructure. In order to enable CubeSat inclusion in space communication networks, this chapter discusses a solution to increase the effective isotropic radiated power (EIRP) of a CubeSat transmitter by way of increasing transmit antenna gain in a volume limited environment.

Maximizing antenna gain for CubeSats requires a large degree of innovation to depart from current antenna solutions such as tape-measure dipoles and microstrip patches. In a collaborative project between the University of Florida (UF), NASA Goddard Space Flight Center, and the University of Colorado at Boulder, the proposed antenna seeks to achieve an aperture with a diameter of 40 cm in order to sufficiently increase gain. This is large relative to the CubeSat, which has dimensions of 30 x 30 x 40 cm<sup>3</sup> (Fig A.1). In development by the UF collaborators is a self-deployable reflector using shape-memory alloys and a copper-coated polymer mesh.

The link budget of the mission demanded that the antenna have greater than 15 dB of gain, an RF bandwidth of 6 MHz. The antenna must also be circularly polarized according to the receiver



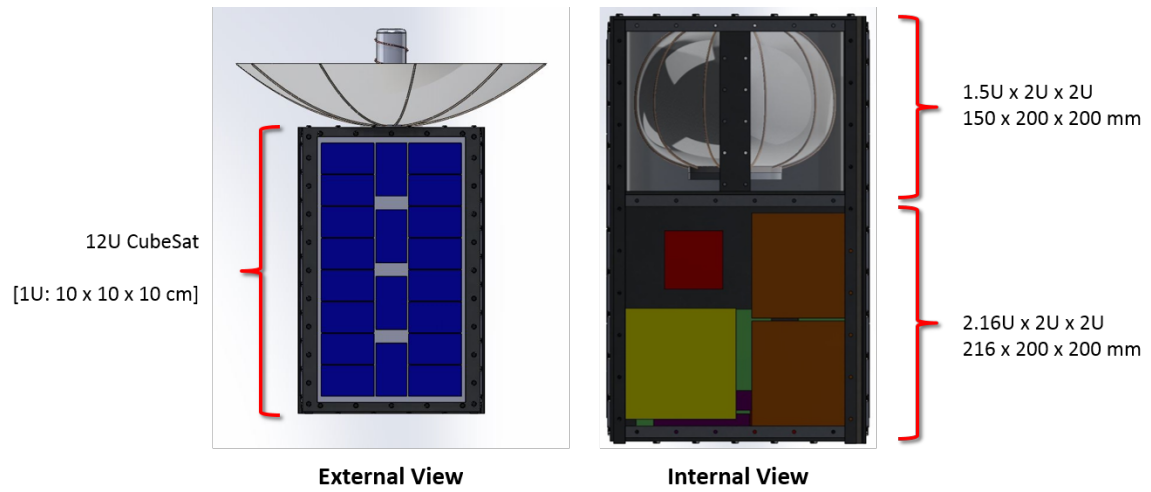


Figure A.1: The dimensions of the NASA CubeSat, with the reflector deployed (left) and stowed (right).

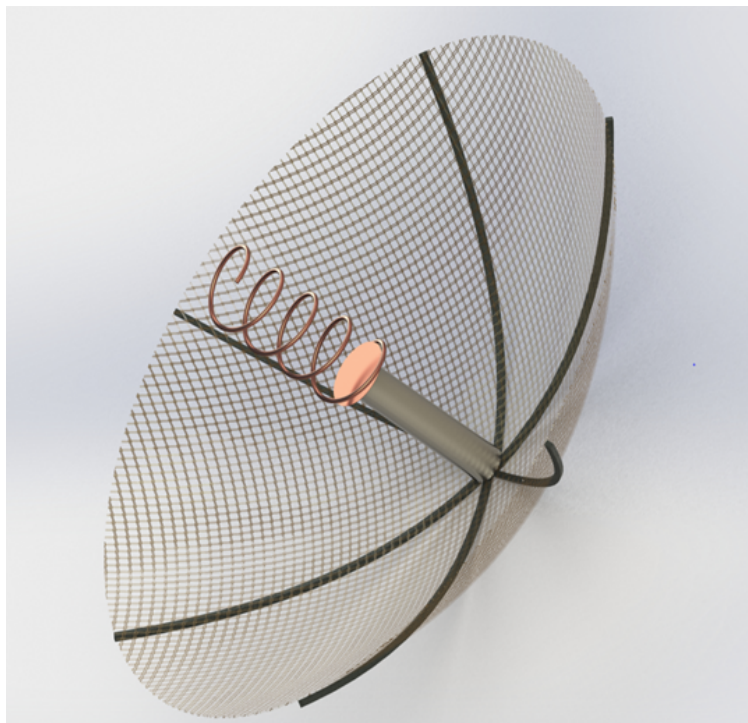


Figure A.2: Solidworks assembly of the initial backfire helix design with the curved mesh reflector. The reflector is 40 cm in diameter.

antennas in the Space Network.

Although the reflector is physically large, it is electrically small at the design frequency of 2.2875 GHz (corresponding to a diameter of approximately  $3\lambda$ ). Since traditional reflector-based antennas require a diameter of at least  $10\lambda$ , traditional feeds cannot be used. The reflector must instead be treated as a curved ground plane placed in the feed near-field. Additionally, the feed must be non-resonant since resonant feeds will be too large relative to the reflector.

A helix feed is chosen since it is compact, naturally circularly-polarized, collapseable/deployable, and eliminates the need for a subreflector. The geometry of the initial design of the helix is shown in Fig. A.2. By designing the helix to radiate in the backfire direction (Fig. A.3), the curved ground plane can be used to further increase gain. This is illustrated in Fig. A.4 where the gain of the helix is improved by 11.5 dB with the addition of the ground plane. The simulated radiation pattern of the helix was intentionally designed to have a 13 dB edge taper, considering the reflector diameter and the focal distance (10 cm).

The input impedance of the helix in Fig. A.2 is plotted in Fig. A.5 to show an inductive input impedance. In order better match the antenna to  $50\ \Omega$ , the characteristic impedance of the helix was reduced by increasing the conductor width as shown in Fig. A.6. A width of 5 mm was chosen.

## A.1 FEED MINIATURIZATION

Although the specifications are met with the current design, it is desirable in this application to further reduce the size of the antenna. This is achieved in simulation through dielectric loading within the helix. The effective wavelength is reduced for higher permittivities, thereby reducing the operating frequency of the antenna, as shown in Fig. A.7. By choosing Rogers RO3210 ( $\epsilon_r = 10.2$ ), an 84% reduction in volume is achieved with respect to the non-loaded helix, as illustrated in Fig. A.8. This is used to obtain an 84% reduction in volume. However by doing so, the axial ratio increased from 1.5 dB to 2.6 dB. Further work would be to improve the axial ratio of the loaded helix by redesign of the helix and the shape of the dielectric. The final radiation pattern, with

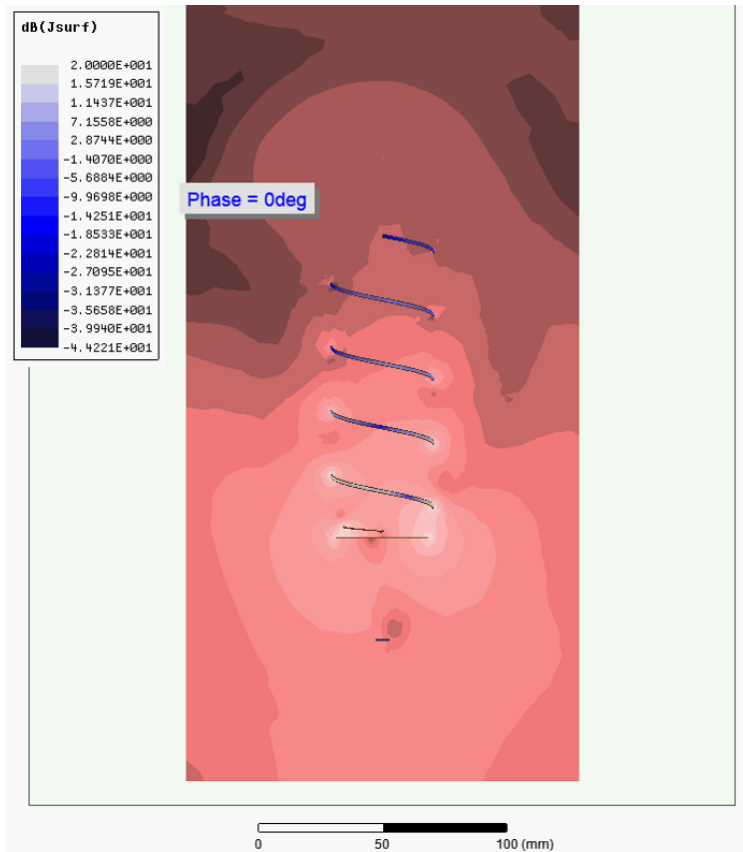


Figure A.3: The electric field plotted in red and surface current density along the helix shown in blue for the initial design of the monofilar helix, showing radiation in the backfire direction.

curved ground plane present, is shown in Fig. A.9. The simulated gain in the endfire direction is 16.4 dB, which is a 16.4 dB improvement relative to traditional patch antennas used on CubeSats at this frequency. On future CubeSats, this work provides a new type of compact, low-mass, antenna with good directivity.

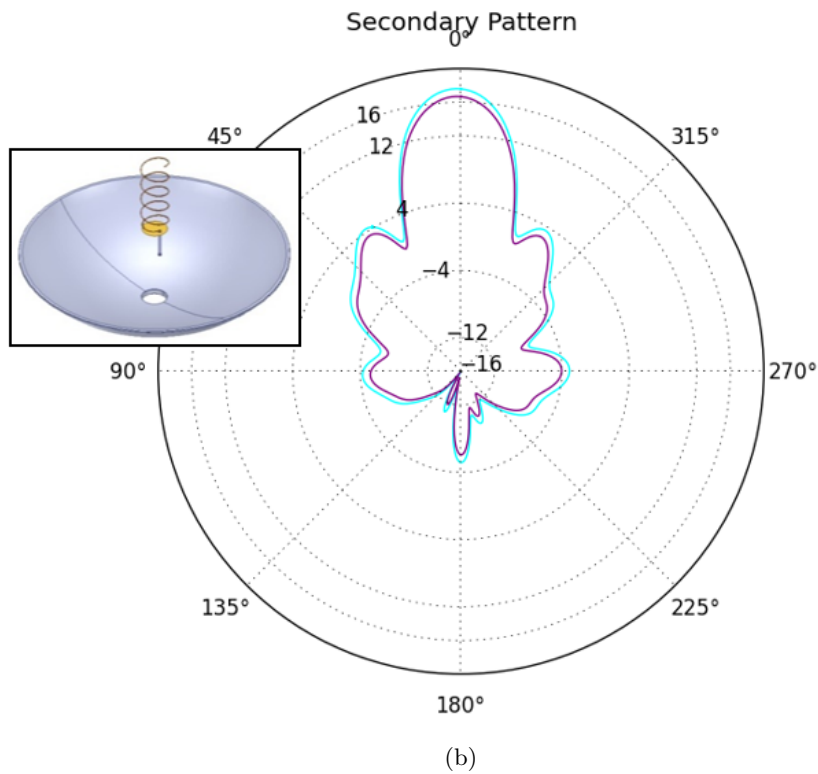
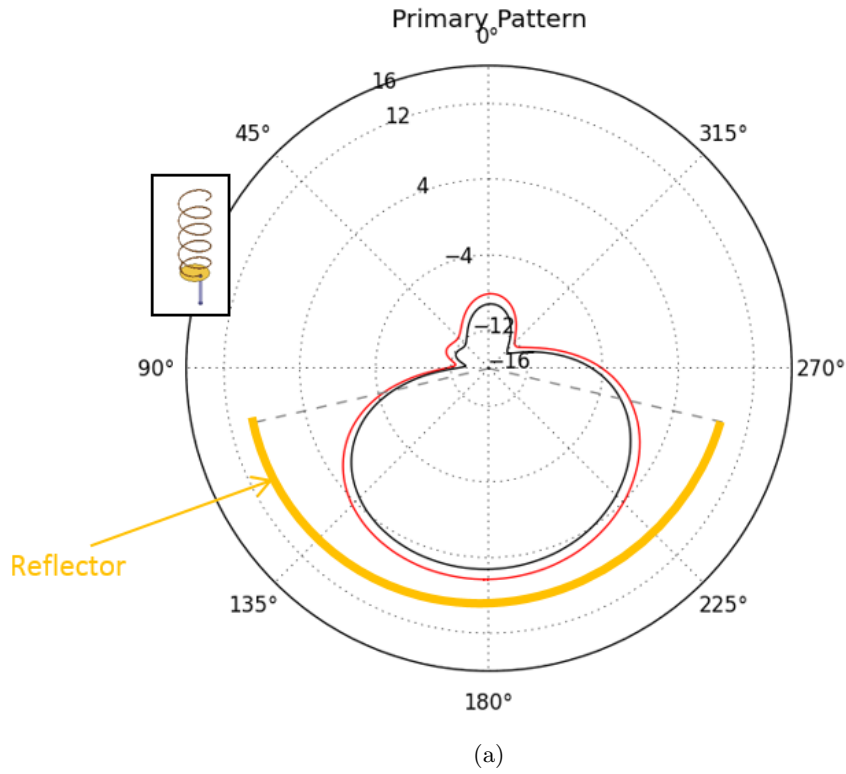


Figure A.4: HFSS-simulated gain pattern for the helix (a) without curved ground plane (reflector), and (b) with curved ground plane included. By designing the helix to radiate in the backfire direction with 13 dB edge taper to the ground plane located 10 cm below the helix, the curved ground plane improves the gain by 11.5 dB.

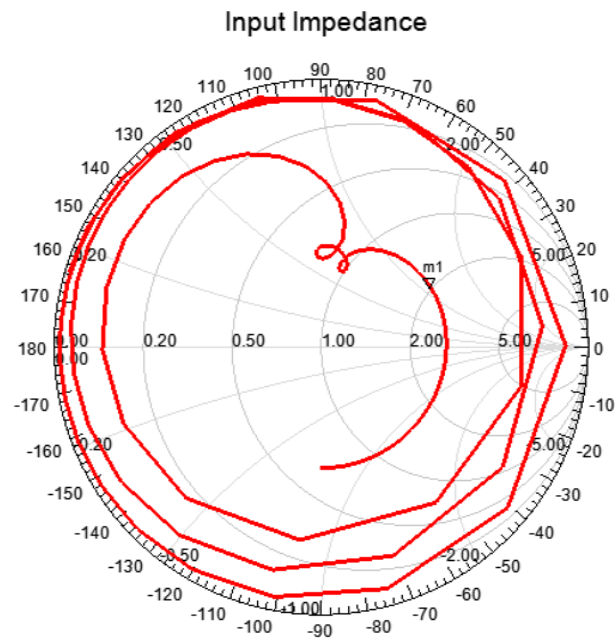


Figure A.5: The simulated input impedance of the helix feed in Fig. A.2, with marker indicating the impedance at 2.2875 GHz.

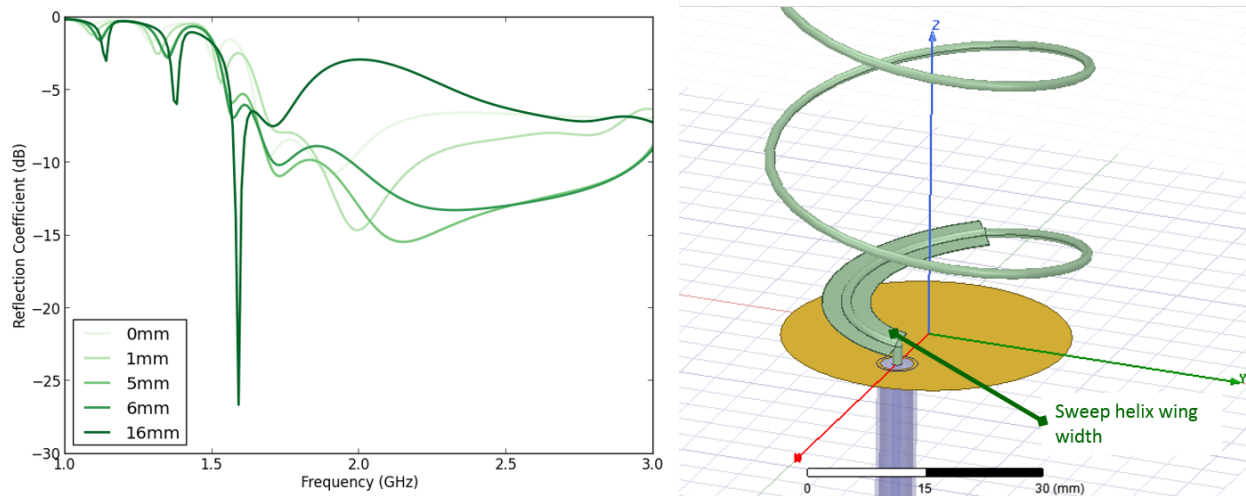


Figure A.6: The reflection coefficient of the feed as the conductor width is stepped in size.

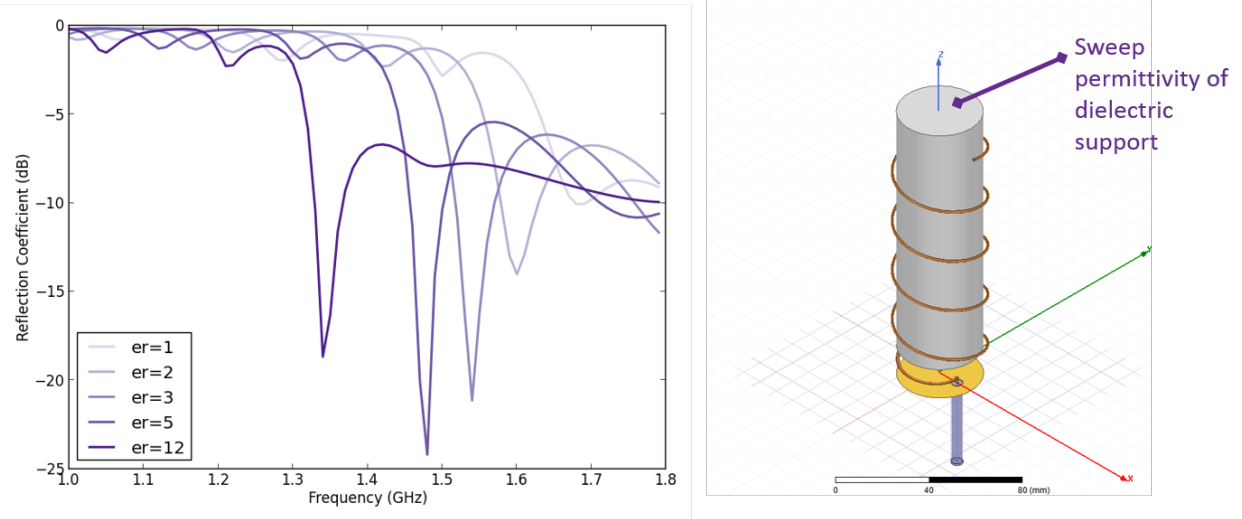


Figure A.7: The reflection coefficient of the feed as the conductor loading dielectric placed within the helix is increased in permittivity.

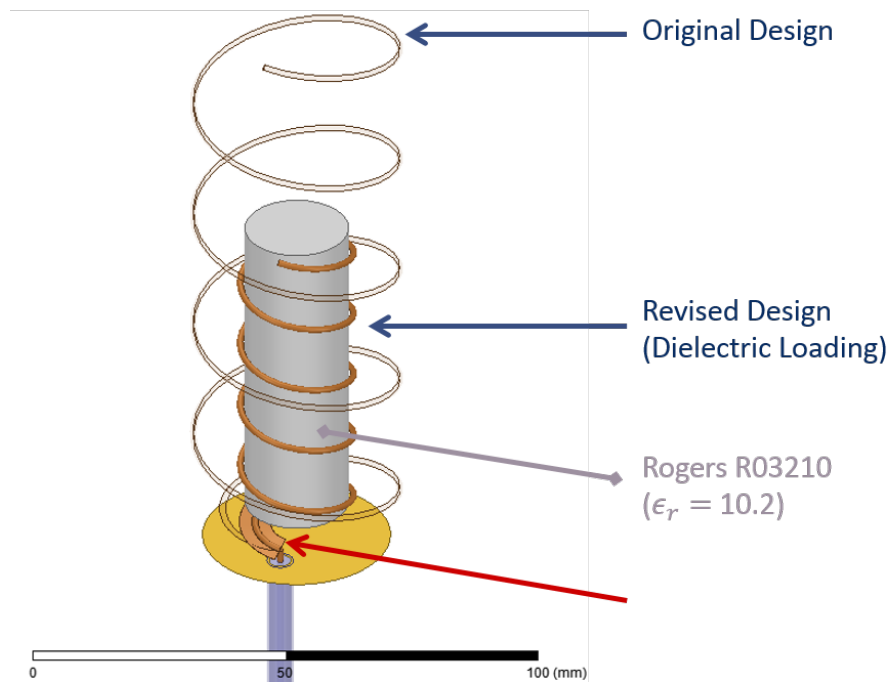


Figure A.8: The dielectric loaded helix compared to the unloaded helix, showing an 84% reduction in volume.

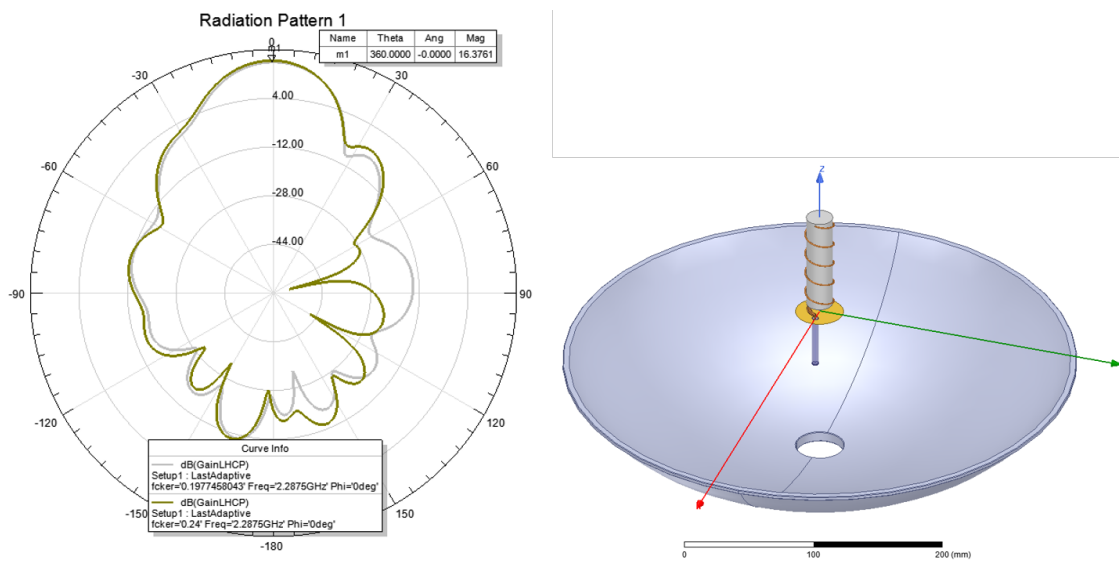


Figure A.9: HFSS simulated gain pattern (left) for the dielectrically-loaded backfire monofilar helix with curved ground plane (right).